# DAMPING RATE MEASUREMENTS IN THE SLC DAMPING RINGS\*

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# Abstract

The transverse damping rates of the SLC electron and positron damping rings have been measured during the high current physics run at,  $I = 3.5 \times 10^{10}$  particles per bunch. The measurements, done over a period of two months, show large fluctuations exceeding the statistical uncertainty of each measurement. The longitudinal damping rate of the positron damping was also measured.

# I. DESCRIPTION OF THE OPTICS

The synchrotron light produced in a bend magnet is reflected by a water cooled molybdenum mirror which resides inside the vacuum chamber. The light exits the vacuum chamber through a synthetic fused silica window. Subsequently it is collected by an achromatic lens of focal length f=1.33 m which functions as the objective lens of the optical system. The objective is located 1.47 m away from the emission point. The light is transported outside the ring vault by a succession of mirrors and through an evacuated pipe which is terminated on both ends by two synthetic fused silica windows. Finally the light reaches the fast gated camera lens [1], which was used in the transverse damping times measurements, and the image of the beam is formed on the photocathode. In order to increase the field of view and prevent vigneting by the camera lens a large field lens of 1.5 m focal length and 10 cm diameter was placed 1.5 m in front of the camera lens. The total distance between the objective and field lens was 13.4 m. The camera was focused on the field lens which, within 1 m, was also the position of the image of the beam formed by the objective. In the horizontal plane, the aperture was limited by a mask, 2 cm wide, placed in front of the objective. In the vertical direction the opening angle of synchrotron radiation determines the aperture. The focal length of the camera lens in the electron damping ring was chosen to be 300 mm and the whole system provided an overall magnification of 1:2.5. The positron damping ring camera lens had a focal length of 100 mm and the system provided a magnification of 1:1. The smaller magnification of the positron damping ring system was necessitated by the bigger size of the injected positron beam.

For the longitudinal damping time measurement a streak camera was used [2]. The optics configuration for the streak camera differed because the small slit width required that the light was focused to a smaller spot. The f=1.5 m lens was removed and an f=50 cm lens was placed in front of the streak camera at a distance which provided the maximum illumination on the slit. The slit is imaged onto the photocathode of the streak camera by a pair of f=50 mm lenses which provide 1:1 magnification.

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The resolution of the system in the horizontal plane is 13  $\mu$ m determined by depth of field [3]. The depth of field depends on the beam trajectory curvature and the horizontal aperture of the optical system, which is approximately 13.7 mrad. The diffraction limited resolution, using Raleigh's criterion, is 68  $\mu$ m determined by the natural opening angle of 4.0 mrad at a wavelength of 550 nm [4]. The rms contribution due to diffraction is therefore estimated to be 34  $\mu$ m. The critical wavelength for a 1.19 Gev beam and bending radius 2.04 m is 0.68 nm. The resolution in the vertical plane due to depth of field is determined by the length of the portion of orbit observed and the opening angle of synchrotron radiation in the vertical plane. The rms contribution is estimated to be 27  $\mu$ m. The resolution due to the gated camera CCD pixel size is 13  $\mu$ m for the electron damping ring setup and 45  $\mu$ m for the positron damping ring. Adding all these contributions in quadrature the horizontal rms resolution is 18  $\mu$ m and 47  $\mu$ m for the electron and positron rings respectively. The rms contribution to the width in the vertical plane is 45  $\mu$ m and 64  $\mu$ m.

## II. DATA ANALYSIS

# A. Transverse

The data were acquired in a random sequence of intervals of the time elapsed between injection and the gated camera trigger. This was done so that the data would not be biased by slow variations of the transverse beam size, during the data acquisition time, which was 20 min for 300 frames. Each frame of the beam image represents a different injected bunch. The electron bunch is stored for 8 msec and the positron bunch is stored for 16 msec. The video signal of the gated camera was digitized by a transient waveform digitizer. The projections on the horizontal and vertical axes were fitted to a function of the form

$$f(x; A, B, C, \sigma, x_0) = \frac{A}{\sqrt{2\pi\sigma}} e^{-\frac{1}{2}\left(\frac{x-x_0}{\sigma}\right)^2} + B + Cx.$$

The pedestal term was not constant because of the electrically noisy environment in the building where the camera was located. A  $\chi^2$  minimization was performed for each frame with

$$\chi^{2} = \sum_{i}^{n} \frac{(f(x_{i}; A, B, C, \sigma, x_{0}) - v_{i})^{2}}{v_{i}}$$

Where  $v_i$  is the rescaled digitized video signal so that the  $\chi^2$  per degree of freedom distribution would peak around one. The statistical error on the measured sigma was determined from the correlation matrix derived from the minimization of the  $\chi^2$ . The square of the width was plotted against the time the bunch has spent circulating in the ring and the data was fitted to a curve of the form

$$\sigma\left(t\right)^{2} = \left(\sigma_{inj}^{2} - \sigma_{eq}^{2}\right)e^{-\frac{2t}{\tau}} + \sigma_{eq}^{2}$$



Figure 1. Sample of data for the electron damping ring. The vertical scale represents the size of the bunch image on the photocathode. The bunch itself is 2.5 times smaller

The fitted parameters are  $\sigma_{inj}$  the width of the injected bunch,  $\sigma_{eq}$  the equilibrium width of the bunch, and  $\tau$  the damping time, see figures 1, 2 for a sample of data and fits.

#### B. Longitudinal

The analysis of the longitudinal damping time is similar. The projection of the image of the bunch on the time axis was fitted to a function of the form

$$\frac{A}{\sqrt{2\pi}\sigma}e^{-\frac{1}{2}\left(\frac{x-x_0}{\sigma(1+S)}\right)^2}+B$$

Where  $S = |S| \frac{x - x_0}{|x - x_0|}$  representing the asymmetric shape of the bunch. The damping time is derived by a nonlinear exponential fit. The data consist of ten measurements of bunch length at each store time. The ten measurements at each point are averaged. The standard deviation of the ten measurements divided by  $\sqrt{10}$  is used to weight the contribution of each point to the  $\chi^2$  in the exponential fit, see figure 3.

# **III. ERROR ANALYSIS**

## A. Transverse

The uncertainty in the transverse measurements has statistical as well as contributions due to systematic errors. Despite the large contribution from resolution to the width measurements the damping time determination is not affected. The resolution adds in quadrature to the width, therefore the square of the width still follows an exponential damping law. However if the resolution depends on the transverse dimensions of the beam then the above statement is no longer true. In principle there is a dependence due to the fact that the depth of field decreases as the horizontal dimension of the beam decreases but the variation is smaller



Figure 2. Sample of data for the positron damping ring. The vertical scale represents the real size of the bunch.



Figure 3. Longitudinal damping time data. The origin of the horizontal axis represents injection time.

than 1% due to the small angular acceptance of the optical system and the small angular spread of the synchrotron radiation in the vertical plane. Effects due to the damping of the angular divergence of the beam are also small since in the worst case of the injected positron bunch the angular divergence is 1.5 mrad , which is small compared to the light angular divergence.

The dynamic range for linear operation of the gated camera was rather limited. Even with the optimum amount of filtering, the photocathode showed signs of saturation as evidenced by the decreasing amount of light detected for increasing store time. The dependence of the width with intensity was measured and no clear plateau was found. Filtering was chosen so that the overall width variation due to this effect would stay below 10%. From simulated data, this effect tends to decrease the measured damping times by 3%.

The horizontal damping time can be influenced by the presence of dispersion which at the emission point is  $\eta$ =5 cm. The energy spread of the injected beam is  $1 \times 10^{-2}$  which rapidly



Figure 4. The horizontal damping times are represented by triangles and the vertical damping times by circles. The statistical error for each measurement is comparable to the size of the symbols

damps to the equilibrium energy spread  $7 \times 10^{-4}$ . In order to determine whether this effect is significant, the data were fitted to the sum of two exponentials where the damping time of one of the exponentials was fixed to be equal to 1.8 msec, the longitudinal damping time. The fits preferred a small negative weight for the second exponential. This indicates that any effect due to dispersion was masked by the nonlinear behavior of the gated camera and the low statistical weight of the points near injection.

In figure 4 the measurements are shown ordered in time. There is a large variation not explained by statistical errors indicating an additional unknown time dependent source of systematic error. Statistical errors are determined by the exponential fits, with properly weighted  $\chi^2$ , and on the average are 0.06 msec. For reasons of comparison with calculations of damping times [5] the measurements are averaged and summarized in the table above. The error quoted is the standard deviation of the corresponding set of measurements.

## B. Longitudinal

Systematic errors due to photocathode saturation were eliminated by attenuating the light enough so that the camera was operated in the linear regime. The use of an interference filter centered at 500 nm and with a 40 nm bandwidth, ensured that the contribution to resolution from dispersion in the glass optics was negligible. There was only one measurement of the longitudinal damping time and the error quoted is the statistical uncertainty.

# **IV. CONCLUSIONS**

It is impossible on the basis of these measurements alone to distinguish whether the damping time fluctuations are due to instrumental effects or to orbit changes, or beam excitation from

Damping time measurements (msec)

Ring	$ au_x$	$ au_y$	$ au_z$
Electron	$3.32\pm0.28$	$4.11 \pm 0.31$	-
Positron	$3.60\pm0.15$	$4.17\pm0.14$	$1.87\pm0.13$
Calculation	3.52	3.56	1.79

the extraction kicker magnets or interaction between the two bunches in the rings.

In order to understand the origin of the large fluctuations in the damping time measurements, and the discrepancy with the calculations, the orbit, tune and pressure in the vacuum chamber dependence should be studied.

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