



known resistivity in the bore of the magnet thereby acting as a shorted secondary during a magnet cycle.

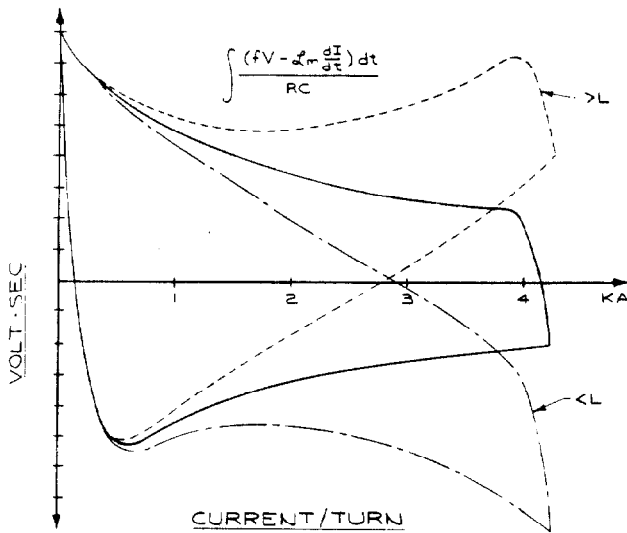


Fig. 2. Schematic drawing of various parameters' effect on the magnetization curve. (Note solid curve is magnetization as calculated from E/S Doubler Conductor.)<sup>2</sup>

The iron shield, which while in the infinite " $\mu$ " magnetic field range acts as a mirror for the coil package, will cause a decrease in inductance as the Fe becomes saturated (i.e.,  $\mu$  becomes finite).

The loss as a function of frequency can be formulated in two forms; first, the total loss as a function of  $\dot{B}$  and, second, parametrically the loss as a function of  $\dot{B}$  for a given current.

These loss data can be analyzed to provide a determination of the effective transverse resistivity of the cable.

The magnetization of a "Rutherford style" compacted cable conductor such as the one used is given by:

$$M = \frac{2\mu_0 \lambda J_c d}{3\pi} \left\{ 1 + \frac{1}{\lambda J_c d} \left( \frac{\dot{B} L^2}{\rho_e} + \frac{\dot{B}_a L^2}{\rho_c} \left( \frac{2\pi d^2}{5} + \pi/2 \right) + \frac{\dot{B}_a L^2}{\alpha^2 \rho_c} \cdot \frac{3\pi}{8} \right) \right\}$$

$$\frac{2\mu_0 \lambda J_c d}{3\pi} = \text{filament magnetization}$$

$d \equiv$  filament diameter

$J_c \equiv$  critical current density

$\lambda \equiv$  filling factor

$\rho_e \equiv$  transverse composite resistivity

$\dot{B} \equiv$  applied magnetic field

$L \equiv$  1/4 composite stand transposition (twist rate)

$L \equiv$  1/4 cable transposition (twist rate)

$\rho_c \equiv$  average effective transverse cable resistivity

Experimentally, it is possible to determine when the cable magnetization is comparable to that of the basic filament loss. These data will determine the effective transverse resistivity of the cable for cross strand coupling. It is also possible with the above expression to analyze the magnetization data to determine various  $\dot{B}$ 's at which the filament to filament and strand to strand coupling losses become comparable to the basic superconductor filament volume.

magnetization loss.

## EXPERIMENTAL RESULTS

Data as received and plotted on a graphics terminal is shown in Figure 3. These data are for a typical Energy-Saver doubler cycle to 4.4 T on a 22 second ramp to full energy. This Magnet #384 represents a higher loss magnet with a more typical energy being 550 j/s but is a good example to use to illustrate variations in the ramp rate dependences and the variations of the coupling term parameters. The droop of the hysteresis curve in Figure 3 has been analyzed with the results given in Table 1.

### MAGNET 384 - 4409 AMPS - V-OUT

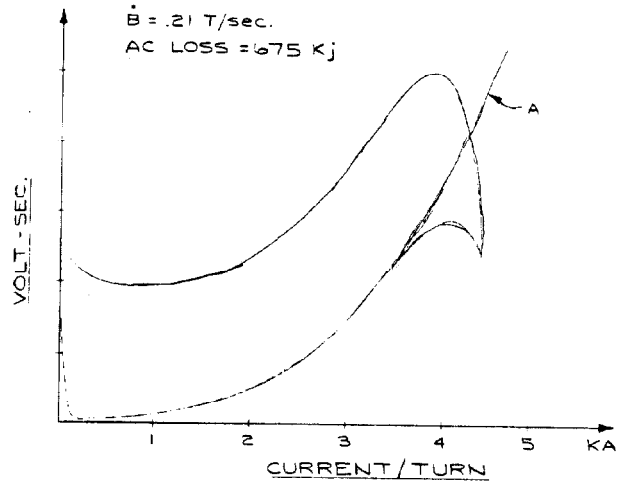


Fig. 3. Energy in minus energy out graphical plot of integrator output signal.

Table I

Inductance Changes  
Magnet #384

$L$  (Nominal) = 42 mH

Current Turn (kA)	Field T	$\Delta L$ (mH)
1.25	1.250	0.02
2.0	2.000	0.076
3.0	3.000	0.266
4.0	4.000	0.621
4.4	4.399	0.819

Figure 3 also clearly shows the effect of iron saturation distorting the magnetization above 3.8T.

Figure 4 represents the data as seen after the deflection of the magnet has been removed. These data were taken from the test of Magnet #417. It can be seen that a cross coupling of strands in this magnet becomes apparent about 0.9T (9kA). At 2.8T the coupling losses are already equal to the basic filament loss. The effective transverse resistivity of the cable would be  $3 \times 10^{-4} \Omega\text{-m}$  at that point.

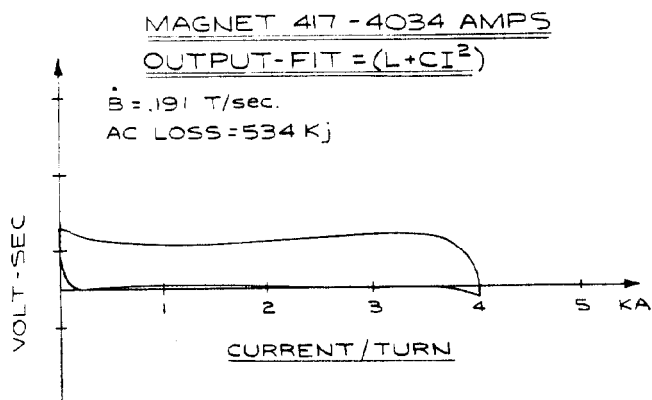


Fig. 4. Energy in-energy out with the average curvature (due to inductance change) removed.

In Figure 5 it is apparent that the 20% increase in losses in Magnet #384 versus Magnet #417 is attributable to the field at which the onset of the coupling occurs. With the exception of the field onset, the behavior of both magnets seems identical.

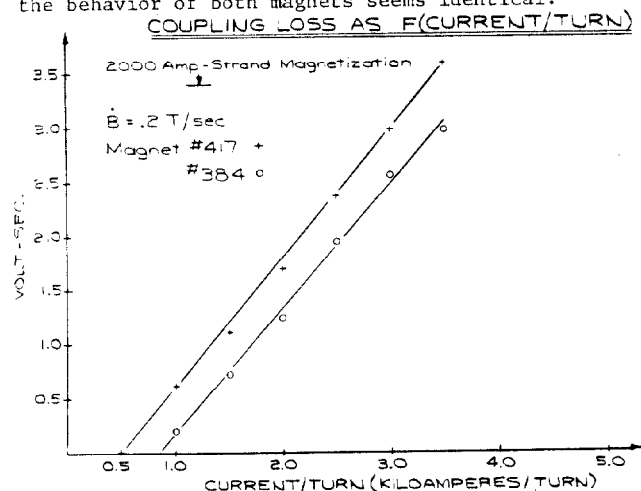


Fig. 5 is a plot of the energy loss in excess of the Conductor Magnetization (filament) loss as calculated. A relatively higher loss magnet is compared to an average loss one.

Table II gives the loss at 3.3T as a function of  $\dot{B}$  for the two magnets (numbers 384 and 417).

Table II  
Magnetization of Magnets As Function of Ramp (J/φ)  
Peak Field = 3.3T

$\dot{B}$ T/sec	Magnet # 384	417	267	Quad
.099		333		94
.121			446	
.153	434		467	
*→ .195		366		
*→ .224			462	
.308		423	462	94
.488	533			
.733	604			

\*Near Operational Ramp E/S Doubler

Table III shows the threshold effect for the coupling loss, that is to say, there is a minimum rate at which the field may be ramped that below which the losses are essentially constant. This level commonly referred to as the basic superconductor filament loss.

Table III  
Magnetization of a Magnet as a Function of Ramp  
Peak Field - 2T  
\*E/S Doubler Ramp

$\dot{B}$ T/sec	Joules Cycle	Dipoles	Quad
.055	196	247	55
.103	192	241	
.159	210		
*→ .202	229	260	60
.320	233	270	
.390			65
.510	261	300	

These data indicate that a half ramp rate would lower the refrigeration load to ~40% of that of the standard cycle.

Utilizing the parameters of the cable strand, the estimated  $\dot{B}$  that the strand coupling loss becomes comparable to the basic filament magnetization is 0.6T/sec, while that for strand to strand coupling at 4.T is 0.2T/sec.

## CONCLUSIONS

It is possible to now routinely obtain data that enables all of the aforementioned parameters to be determined in the same amount of time on the test stand that the old A.C. loss data was taken at the FNAL Magnet Test Facility. According to the specific model taken, the changes of inductance found would indicate a deflection of the coil of 60\*100 micron during the ramping of the magnetic field.

## ACKNOWLEDGMENTS

The authors would like to express their appreciation to K. Ishibashi for his calculations of the magnetization curves.

## References

- <sup>1</sup>M.N.Wilson, CRYOGENICS, June, 361, (1973).
- <sup>2</sup>K.Ishibashi, private communication, 1980.