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COLLECTIVE ACCELERATION WITH INTENSE ELECTRON BEAMS*

Craig L. Olson Sandia Laboratories Albuquerque, New Mexico

Summary

Collective acceleration methods that employ an intense relativistic electron beam (IREB) are discussed. A brief history and a classification of collective acceleration methods are given. Methods examined include IREB injection into neutral gas; IREB injection into vacuum; plasma-filled IREB diodes; and vacuum-filled IREB diodes. Accelerating fields of order 10° V/cm have been observed experimentally. The collective acceleration processes for IREB injection into neutral gas and vacuum are discussed. It is noted that the collective acceleration processes for IREB diodes have not been elucidated yet. A summary of present collective ion acceleration research areas that involve IREB's is given.

1. Introduction

Collective acceleration methods differ from conventional acceleration methods in that the main accelerating fields are not caused by externally applied potentials. Instead, the accelerating fields are caused by the collective effects of a large number of particles which impart acceleration to a smaller number of particles. In conventional accelerators, the effective accelerating field is ultimately limited by electrical breakdown at the accelerating gap. In collective-effect accelerators, the accelerating fields are not limited by breakdown, and accelerating fields much larger than those in conventional accelerators should ultimately be achievable. Other fundamental differences are that collective-effect accelerators can have net charge densities, and net current densities, directly in the acceleration region. In conventional accelerators, e.g., the applied accelerating fields are divergence-free in the accelerating gap region $(\nabla \cdot \mathbf{E} = 0)$, which means longitudinal phase stability and radial focusing in the gap may be mutually exclusive. In collective-effect accelerators which utilize a net charge density, the accelerating fields may have a divergence $(\nabla \cdot E \neq 0)$, and longitudinal phase stability and radial focusing may occur simultaneously.

Since the introduction of several basic ideas on collective acceleration by Veksler,¹⁻³ Budker,⁴ and Fainberg^{5,*} in 1956, research on collective acceleration has grown considerably. The electron ring accelerator (ERA) concept emerged from Dubna in 1967,⁷ and since that time it has enjoyed large-scale investigations at Dubna, Berkeley, Maryland, Garching, Karlsruhe, Nagoya and Moscow.⁸⁻¹⁷ At this meeting, the latest results from Garching concerning their successful acceleration of protons and He ions will be given;¹⁵ as will the latest results on the cusp injection ERA work at Maryland,¹⁷ and some ring compression work at Nagoya.²⁰ With these brief comments on the ERA, we shall now turn to collective acceleration with intense relativistic electron beams (IREE's), to which most of this paper will be devoted.

Intense relativistic electron beams had their origins in the pulsed power technology pioneered in the early 1960's by Martin²¹ A typical IREB today has electron energies from 100 keV to 10 MeV, currents from 10 kA to 1 MA, and pulse lengths from 10 nsec to 100 nsec. Because the IREB electron density is typically high (~ $10^{11}-10^{12}$ cm⁻³) it is ideally suited for collective acceleration research. Interest in IREB collective acceleration research grew in 1968 when

Graybill and Uglum discovered that injecting an IREB into a low pressure neutral gas could produce collectively accelerated ions with energies greater than the IREB electron energy.²² Since that time a considerable amount of experimental²³⁻³³ and theoretical³⁹⁻⁴⁸ work has been done to investigate this process,⁴⁹⁻⁵⁴ and recently a theory⁵⁵⁻⁵⁹ has been developed that has been able to explain the observed acceleration.²²⁻³⁸ Collective fields of order 10^5 V/cm have been inferred from the data; fields of this order are predicted by theory and are seen in numerical simulations⁵⁰ Collective acceleration with IREB's injected into vacuum has also been studied,^{30-32,51-53} and collective acceleration in the diode that generates an IREB has also been investigated.^{29,30,60,52,53,64-90}

In part 2, a brief classification of collective methods is given. In part 3, IREB collective acceleration is discussed in regard to IREB injection into neutral gas, vacuum, and plasma; and for plasma-filled diodes and vacuum-filled diodes. In part 4, present approaches to collective ion acceleration using IREB's are discussed, and in part 5, concluding comments are given.

2. Classification of Collective Methods

Collective acceleration research at present includes a rather large area of experimental data, theoretical concepts, and proposed acceleration schemes. A brief classification of these "methods" is given in Table 1, where they are categorized as to how the main accelerating field is produced; by net space charge (of an electron beam, or a bunch of charged particles), by waves and/or instabilities (excited, e.g., by

TAELE 1

Collective Acceleration Methods

(1)	<u>Net Space Charge</u> ERA IREB/gas IREB/vacuum HIPAC IREB/transverse sweep IREE/linear control	<u>References</u> : 7-20 22-60 30-32,61-63 91,92 50,53,59,93-101 59,101-102
(2)	Waves and Instabilities inverse coherent Cerenkov EM radiation acceleration plasma waveguide	1-3,48,56,103-105 1-3 5,6
	solitons and nonlinear waves stochastic acceleration e-e two-stream instability e-i two-stream instability IREB/diode (?) IREB/cyclotron mode electron autoacceleration (e)	106-112 113 114 76,115-118 29,30,64-90 119-121 53,99,122-125
(3)	Inductive Effects beam envelope motion electronic ram (?)(e)	44-47 ,5 6 126-130
(1,)	Impact Acceleration relativistic collision	1-3,101,131,132

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interactions between beams, plasmas, charged particle bunches and/or external structures), by inductive effects (such as those caused by envelope motion of a current-carrying beam), or by impact acceleration (a purely dynamic collisional effect). The listing is Table 1 is not meant to be exhaustive: it does, however, present a convenient summary of the major areas of collective ion acceleration research and collective electron acceleration research. In the later case, a large number of energetic electrons is used to accelerate a smaller number of electrons to higher energies; this includes electron autoacceleration effects⁵³,⁹⁹,¹²³-1²⁵ and the electronic ram effect.¹²⁶⁻¹³⁰ Erief comments about each of the four categories in Table 1 follow.

(1) By net space charge, we mean that ion accelerating fields are produced by a simple net charge density. It should be noted that this is the only category in which accelerated ions have been produced, and explained, to date (this includes the ERA, IREE into gas, IREB into vacuum, and HIPAC).

(2) Waves and instabilities have been frequently proposed as possible acceleration methods, and a considerable amount of theoretical work has been done in this area, especially in the Soviet Union. Note that the listing IREB/diode was only tentatively included here, because the collective acceleration process(es) involved are not sufficiently understood at this time; the two-stream e-i instability has been suggested as a possible explanation, ^{76,116-118} but so have several other wave-type schemes, and space-charge and inductive-type effects.^{64-72,62-90} Apart from this IREB/diode possibility, none of the wave schemes given here have been developed to date to the stage of producing accelerated ions in actual experiments.

(3) By inductive effects we mean induced fields that might be caused, e.g., by envelope motion of a beam with a net current (IdI/dt effect), or by the rise or fall of a net current (IdI/dt effect). This concept has arisen as a possible candidate for explaining certain experimental data.^{44-47,64-70,83} Here we note that recent theoretical results⁵⁶ indicate that these effects are typically not strong enough to produce useful collective ion acceleration. The electronic ram effect is tentatively included here because induced fields have been proposed¹²⁵⁻¹³⁰ to explain the observed collective electron acceleration; however, estimates we have made tend to indicate inductive effects should be negligible, and that the acceleration mechanism is still open for further investigation at this time.

(4) Impact acceleration refers to the purely dynamic effect caused by the collision of a relativistic (γ) heavy bunch (e.g., a dense electron bunch) with a light bunch (e.g., a small ion bunch).¹⁻³,131,132 Providing certain restrictions are met, each ion should receive the enormous energy $2\gamma^2 Mc^2$ (where M is the ion mass and c is the speed of light). However, the restrictions on the heavy bunch have been shown to be prohibitive¹⁰¹--the equivalent peak current I₀ of the heavy bunch must be I₀ > 23.4 BY MA. Since IREB peak currents today are only of the order of one MA, the impact acceleration method must apparently remain confined to the concept stage for now.

From this brief overview we note that "net space charge effects" appear to be the principal means of collectively accelerating ions to date. In regard to high energy ion acceleration in this category, we note that theoretical considerations limit the accelerating fields in an ERA to ≤ 0.45 MV/cm.¹⁷ The HIPAC configuration^{21,32} employs a stationary potential well, and it therefore cannot be used over and over again to produce very high ion energies (the HIPAC has merit principally as a high-Z ion source). IREB's, on the other hand, have already demonstrated ion accelerating fields of order 1 MV/cm, and there are at present no



Fig. 1 Basic IREB diode and drift tube configuration.

fundamental theoretical limitations on producing even higher fields. Collective ion acceleration research with IREB's will now be discussed.

3. IREB Collective Ion Acceleration

The basic configuration of an IREB diode and a drift tube are shown in Fig. 1. The IREB is created by a high voltage pulse from a Blumlein or transmission line which is applied across an anode-cathode gap. Cathode electrons are accelerated to the anode, which is a thin foil, and pass directly through it. Depending on what the drift tube contains (neutral gas, vacuum, or plasma), the IREB may or may not propagate efficiently in it. Collective ion acceleration has been observed in the drift tube (filled with neutral gas or with vacuum) and in the diode region (filled with plasma or with vacuum). Collective ion acceleration in a drift tube filled with plasma has not been reported.

IREB/gas: Collective ion acceleration for IREB injection into a neutral gas was discovered in 1968 by Graybill and Uglum.²² Subsequently, many more experi-Subsequently, many more experimental investigations were performed at Ion Physics Corporation (IPC),^{23,24} at Physics International (PI),²⁵⁻²⁸ at Sandia Laboratories²⁹⁻³² at the Air Corporation (IPC), at Physics inconnectional (PI), $^{25-28}$ at Sandia Laboratories, $^{29-32}$ at the Air Force Weapons Laboratory (AFWL), $^{35-35}$ at the Lawrence Livermore Laboratory (LLL), 36 at the Lebedev Physical Institute (Moscow), 37 , 53 and at the Physical Technical Institute (Kharkov).³⁸ In the basic experiment, the metallic guide tube is filled with a neutral gas at a pressure of the order of 0.1 Torr H2. Ions are observed to be accelerated in the same direction that the IREB propagates and to attain energies higher than the IREB electron energy. Ion detection may be accomplished by current screens, nuclear emulsions, activation analysis, and/or ion mass spectrometry. The ion energy, number of ions, and ion pulse length all have dependences on the neutral gas pressure, as well as on the electron beam energy and current. In fact, the process is controlled by at least eleven independent parameters; IREB (energy ϵ_{e} , peak current I_{o} , voltage risetime t_{v} , current risetime t_r , pulse length t_b , radius r_b), metallic guide tube (radius R, length L), and neutral gas (charge state Z_i, ion mass M, and pressure p). A summary of accelerated protons and related IREB and drift tube parameters is given in Table 2. For a summary of other accelerated ions (D, He, N, A), see ref. 32.

Originally, six theories were proposed to explain the data. These include the ong-dimensional electrostatic well models of Rostoker, ⁵⁹ Uglum et al., ⁴⁰, ⁴¹ Rosinskii et al., ⁴² and Poukey and Rostoker; ⁴⁵ the localized pinch model of Putnam; ⁴⁴⁻⁴⁷ and the inverse coherent Cerenkov radiation model of Wachtel and Eastlund, ⁴³ Thus concepts in each of categories (1) to (3) in Table 1 were originally employed to explain the data. However, in a detailed study, ⁵⁶ it was found that serious questions arise concerning the validity of some of these theories, and that major difficulties occur in trying to use any of these theories to explain the data. ⁵⁶ It was concluded that the mechanism responsible for the observed acceleration must be an electrostatic effect but that a new theory (different from the four earlier electrostatic theories) was needed to explain the data with all of its parametric dependences.

TABLE 2. Typical data for protons accelerated by IREB injection into neutral $gas(H_{2})$.

PROTONS				IREB				GUIDĘ TUBE			REFERENCES	
$\boldsymbol{\mathscr{E}}_{\mathtt{i}}(\mathtt{MeV})$	N	T(nsec)	$I_i(A)$	$\boldsymbol{\ell}_{\mathrm{e}}^{(\mathrm{MeV})}$	I _o (kA)	$t_r^{(nsec)}$	t _b (nsec)	$r_{b}(cm)$	p(Torr)	R(cm)	L(em)	REFERENCES
4-7 2-10 1-5 5-16 1-3,8	$ \begin{array}{c} \sim 4 \times 10^{12} \\ \sim 2 \times 10^{12} \\ \sim 10^{12} \\ \sim 10^{12} \end{array} $	3-10 3-5 5-15	~200	1.5 1 1.8 5 0.65	30 110 80 40 15-20	10 10 60 25 15	50 60 80 125 50	1.25 2.5 0.5 2*	0.05 -0.15 0.15 -0.65 0.015-0.15 0.05 -0.35 0.005-0.4	3.8 2.5	70	IPC ²⁴ PI ²⁷ Sandia ²⁸⁻³² AFWL ³⁸ Lebedev ³⁷ ,53

In a new theory developed by Olson, 5^{5-59} and substantiated by numerical simulations of Poukey and Olson, 6^{90} ion acceleration occurs in the electrostatic fields of a time-dependent two-dimensional potential well. The acceleration process is basically a zeroorder electrostatic effect, whose description depends on a complete knowledge of the ionization of the background gas and the self-consistent coupling of the beam dynamics to the ionization processes. Ion ionization and ion avalanching were shown to produce major effects while electron avalanching was shown to produce negligible effects. 5^{7-59} The theory contains dependences on all eleven parameters mentioned earlier, and we shall now briefly summarize the basic acceleration process and the predictions of this theory.

The acceleration process depends critically on the relation of the injected current I_0 to the spacecharge limiting current $I_\ell = \beta(\gamma-1) [mc^3/e]$. $[1 + 2\elln(R/r_b)]^{-1}$, f^{54} , f^{59} where $\beta = v/c$, v is the injected electron velocity, $\gamma = (1-\beta^2)^{-1/2}$, and m and e are the mass and charge of an electron. The current I_ℓ is that current for which the potential depression φ_0 caused by an unneutralized beam just equals the injected electron beam energy (i.e., $e\varphi_0 = \mathcal{E}_0$). For $I_0 \ge I_\ell$, the injected beam initially stops at the anode, and the collective ion acceleration process occurs. For $I_0 \ll I_\ell$, the beam is not slowed appreciably in the axial direction, it does not stop at the anode, and no accelerated ions should occur. For reference, the Alfvén-Lawson magnetic limiting current I_A for a charge-neutral, but not current-neutral, intense beam is $I_A = \beta \gamma mc^3/e^{1/3}$, 2^{-34} If there is charge neutrality, then magnetic stopping effects will occur if the net current exceeds I_A . Note that $I_\ell < I_A$ always, so whether or not collective ion acceleration can occur depends on the relative sizes of I_0 and I_ℓ .

For $I_0 \ge I_\ell$, collective ion acceleration may occur, and the resultant two-dimensional electrostatic well effects are indicated in Fig. 2. Initially the beam stops at the anode, and a deep potential well forms of depth $\varphi_0 = \alpha \zeta_0/e$, where $2 \le \alpha \le 3$.^{43,52} The background gas is ionized (by electron impact ionization and by ion avalanching) throughout the deep well





Fig. 2 Qualitative picture of 2-D potential well motion, chowing v(r = 0, z) at successive times.

(* annular beam, $\sim 2 \text{ mm thick}$)

region of axial length $\approx 2R$, although the stopped electron beam is confined to a much smaller axial region.⁵⁸ At roughly the charge neutralization time, a non-adiabatic transition occurs, the beam front begins propagation, and the self-consistent well depth drops to $\varphi_0 \leq \mathcal{E}_e/e$. Ion acceleration occurs during the deep well stage (which produces an ion distribution with energies up to $\mathcal{E}_i \approx \alpha Z_i \mathcal{E}_e$) and during the transition stage (where ions may be trapped in the propagating well). The final, propagating beam front equilibrium is shown in Fig. 3; the self-consistent front structure moves slowly ($\beta \sim 0.1$) while beam electrons stream through it ($\beta_e \sim 1$). The axial length of this structure is typically very long ($> r_b$).⁵⁸

The speed at which the beam front moves out depends on several parameters. At sufficiently low pressures, the front speed is determined by the fastest ions created during the deep well stage. At higher pressures, the front assumes a speed about equal to $2R/\tau_n^{e,1}$ where $\tau_n^{e,1}$ is the charge neutralization time including ion ionization effects. At still higher pressures, above some "runaway" pressure p_R , the beam becomes charge neutralized during its risetime before the current I_ℓ is reached; in this event, the beam never sees a large potential depression, never stops at the anode, and no accelerated ions should occur. Thus for $p > p_R$, ion acceleration is effectively precluded. For $p < p_R$, ion acceleration may occur, provided that certain trapping criteria are also satisfied.⁵⁸

A comparison of the theory, experiments, and numerical simulations (2-D) is given in Fig. 4, where the final ion velocity $\beta_1 c$ is plotted against p. Note that there is reasonably good agreement between all three, and that all three show the effects of roughly



Fig. 3 Moving, self-consistent, 2-D, beam front equilibria, showing the fractional space charge neutralization f_e , the beam profile, and the resultant potential z_{e}^{5+}



Fig. 4 Comparison of experiments (circles, shading), theory (lines),⁵⁸ and simulations (X's)⁶⁰ for proton acceleration by IREB injection into neutral gas (H₂). Data of (a) Graybill (IPC);²⁴
(b) Ecker and Putnam (PI);²⁷ and (c) Kuswa, Bradley, Yonas, Swain et al. (Sandia).²⁸⁻³²
[The notation (X) means very few ions were seen at the indicated pressures.⁶⁰]

constant ion energy at low pressure, increasing ion energy at moderate pressures, and beam front runaway (no ions) at higher pressures. Numerous further comparisons have also been made (concerning, e.g., beam front velocities, number of ions, etc.)^{58,60} and it appears that the theory offers a reasonably well substantiated explanation of the observed collective acceleration process. By keeping I₀ fixed and varying I₂ (from I₂ < I₀ to I₂ > I₀), Straw and Miller observed the ion acceleration threshold at I₀ \approx I₂, and they found ions only for I₀ \geq I₄. Their most recent studies with a larger IREB will be reported at this meeting.³⁵ Also, in earlier work recently brought to our attention, VanDevender³⁶ reported no ions in experiments with I₀ \ll I₄ (in agreement with the theory).

Alexander et al. have also recognized the importance of ion ionization effects and have applied them to a 1-D model.¹³⁵,¹³⁸ Elsewhere, Kolomensky and Novitsky have recently developed a l_2^1 -D computer model to study the collective acceleration process.¹³⁷ Their results tend to further substantiate the results of the 2-D theory and the 2-D simulations discussed above.

IREB/vacuum: Collective ion acceleration by injecting an IREB into a vacuum-filled drift tube has been reported by Kuswa,³⁰ Swain et al.,³¹ and Olson et al.³² The acceleration effect has been explained³¹ The acceleration effect has been explained 31,32 in reference to the theory described above. For $I_0 \ge I_2$, the beam remains stopped at the anode until a sufficient positive ion background can be created to provide some charge neutralization. In this case, the ions come from the anode foil plasma created by passage of the IREB through the foil. (The plasma may include alsorbed gas ions as well as other impurities.) When the dynamic ion background density is sufficient to provide approximate charge neutrality, the beam may begin a "quasi-propagating" stage in which "beam propagation" is consistent with the drawn-out. dynamic ion background. Ion energies up to $\alpha Z_i \epsilon_e$ $(2 \le \alpha \le 3)$ are predicted; ion energies up to $2Z_1 \in e$ have been seen experimentally, and ion energies up to $2Z_1 \mathcal{E}_e$ are seen numerically.^{31,32} Also, the transition between the effects of vacuum-filled and gas-filled drift tubes has been seen experimentally;³¹ below a certain low pressure, anode foil ions are accelerated before the neutral gas is sufficiently ionized, and the net effect looks like a typical "vacuum shot."

Nation³¹ has also reported studies on IREB injection into vacuum, as have Kim and Uhm.⁵² Zorn et al. have apparently converted the Maryland ERA injector to study vacuum injection, and their results will be reported at this meeting.⁵³ For $I_{\rm O} \ll I_{\ell}$, an IREB injected into vacuum will not stop at the anode, but will propagate with radial spreading. If an axial magnetic guide field is used, then an unneutralized, propagating IREB is possible. This, in fact, forms the basis for the cyclotron-wave auto-resonant accelerator concept^{119-121} to be discussed later.

IREB/plasma: For intense electron beam injection into a plasma, there have been no experimental reports of high-energy, collectively-accelerated ions to date. IREB injection into plasma is actively being studied as a means of plasma heating in relation to controlled fusion research, and the general goal is to efficiently utilize plasma instabilities to transfer beam energy to the plasma. For $n_p \ge n_b$ (where n_p is the plasma density and n_b is the beam density), charge neutrality occurs quickly and the collective acceleration process discussed above (for injection into gas) is precluded. However, many of the wave and instability concepts listed in Table 1 may, in theory, be applicable in this case. However, caution is needed in applying certain theoretical calculations to experimental situations; e.g., IREB pinching to the force-neutral condition, assumed in some e-i instability calculations, 17,110 violates known limiting current criteria⁵⁴ for typical beam parameters. Thus, for IREB injection into plasma, waves and instabilities may eventually be used to collectively accelerate ions (to $\mathcal{E}_i > \mathcal{E}_e$), although no such experimental results have been reported to date.

<u>IREB/diode (plasma-filled)</u>: Ions collectively accelerated in the diode region have been observed in many cases,^{20,50,64-90} as summarized briefly in Table 3. Categorically there are two classes of diodes-plasma-filled and vacuum-filled. In reality, vacuumfilled diodes develope moving anode and cathode plasmas, so they too are, in some sense, plasma-filled. The physics behind anode and cathode plasma production and motion is currently an active area of IREB diode research.¹³³

Collectively accelerated ions have been reported by Plyutto et al. of the Sukhumi Institute (USSR) for the plasma-filled diode configuration shown in Fig. 5a.⁶⁴⁻⁷⁰ A spark source is used to create a plasma, which then expands through a hole in the cathode; when the cathode-anode gap is appropriately filled with plasma, the diode potential U_0 is applied. A variety of phenomena are observed, including ions with energies up to many times eU_0 , electrons with energies up to several times eU_0 , transient current and voltage effects, and indications of time-dependent beam pinching. The process(es) responsible for the accelerated ions are apparently quite complicated. Suggested explanations have involved entries in each of the categories

TABLE 3. Typical data for protons accelerated in diodes.

PROTONS		ELECTRONS			DEPENDENCE			
$\boldsymbol{\mathcal{E}}_{\mathtt{i}}^{(\texttt{MeV})}$	N	$\boldsymbol{\epsilon}_{e}^{(MeV)}$	I _o (kA)	U _O (MV)	A-K gap (cm)	Configuration	REFERENCES	
4-5 0-2.5 0.7 2-7 2-3 0.08-3 0.1-3 5-13	$ \begin{array}{c} 10^{11} - 10^{12} \\ 10^{11} - 10^{12} \\ 10^{11} - 10^{12} \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ $	0-0.25 0.06 	1-2 1-3 5 50 100 30	0.2-0.3 0-0.1 0.02 0.2-1.0 0.2-0.3 5 2 2.5	1-10 1-5 2-7 1-2 1.8 0.6	Fig. 5a Fig. 5a Fig. 5a Fig. 5a Fig. 5c Fig. 5b Fig. 5c Fig. 5d	Sukhumi ⁶⁴ Sukhumi ⁶⁶ Sukhumi ⁷⁰ Sukhumi ⁷¹ AFWL ⁷⁶ Sandia ³⁰ LLL ⁸⁴ ,98,89	

(1) to (3) in Table 1; i.e., space charge effects, inverse coherent Cerenkov radiation effects, and inductive beam pinching effects. ⁶⁴⁻⁷⁰ The highest energies attained are $\mathcal{E}_{1}^{max} \approx 10$, and $\mathcal{E}_{1}^{max} \approx 3 \text{eU}_{0}$. In some instances \mathcal{E}_{1} does not depend on Z_{1} ; ^{64,985} in other instances \mathcal{E}_{1} scales directly as Z_{1} . A definitive explanation of the collective acceleration processes involved remains to be given.

IREB/diode (vacuum-filled):Collectively accelerated ions have also been seen in "vacuum-filled" diodes at the Sukhumi Institute, 71,772 at AFWL $^{73-77}$ at Sandia, $^{29,30}, ^{79-61}$ and at LLL. $^{82-90}$ A variety of configurations has been used, and the principal ones are summarized in Figs. 5b, c, d. The cathode usually has a small radius or is pointed. The anode is usually thick, may contain a central insert of a different material, and may have a hole on axis. Many materials (dielectrics, metal) and coatings (especially those bearing deuterium) have been used for the cathode and the anode, and frequently a CD₂ anode insert has been employed. It is evident that the time-dependent processes of the formation and motion of both anode plasmas and cathode plasmas play important roles in both the diode behavior and in the collective acceleration process. 29,30,78,e0,138

The purpose of most of the experiments in the U.S. has been to determine if thermonuclear processes were occurring. Hence the main diagnostic in the U.S. has been total neutron yield (and its isotropy or lack thereof), although in some cases ion mass spectrometry was also used.^{29,30,76,78-80} The overall consensus of this work is that collectively accelerated ions produce



Fig. 5 Diode configurations.

neutrons via beam-target interactions, and that thermonuclear effects (if any) are at least not the dominant effects.

The various phenomena observed include ion energies greater than the applied gap voltage, transient current and voltage effects, and time-dependent beam pinching effects.⁷¹⁻⁶⁰ At Sandia, \mathcal{E}_1 up to 3MeV has been reporte by Kuswa for $\mathcal{E}_{e} \approx 2 \text{ MeV}^{30}$ At LLL, \mathcal{E}_1 in the range 5-13 MeV (with a possible energy tail extending to somewhat higher energies) has been reported by Luce for $\mathcal{E}_{e} \approx 2.5 \text{ MeV}^{89}$ The e-i two stream instability has been suggested as a possible explanation of the observed phenomena.^{76,90,116-118} Several other possible explanations have been proposed by the LLL group, including inverse Cerenkov radiation, pinching effects, the electronic ram effect, the so-called Linhart effect, and several other wave-type effects.⁸²⁻⁹⁰ At present, however, a definitive explanation of the collective acceleration process(es) involved has not been established.

Present Approaches Using IREB's

A brief summary of continuing and proposed research areas involving IREB's for collective ion acceleration follows.

<u>IREB/gas/control</u>: Presumably more experiments will be done with IREB injection into neutral gas to further verify the acceleration mechanism, and to study even further parametric dependences (although all ll basic parameters have already been varied ^{22-34,36-38}). Kolomensky et al. (Moscow)³⁷ and Tkach et al. (Kharkov)³⁸ will apparently continue their experimental investigations. Straw and Miller (AFWL) will report new data at this meeting.³⁵ Also, some experiments should be forthcoming from Rostoker et al. (UCI).¹³⁹ Remaining experimental areas of interest include further studies of the effects of axial magnetic fields,^{27,56,360} and possibly studies of multiple pulse phenomena⁵⁸ (which have been observed only at PI, and only in some cases²⁵⁻²⁸).

In regard to extending the acceleration process, the first logical choice is to consider possible passive control methods. Suggestions include axial variation of the pressure, 85,52,53,9140,9142 or of the guide tube radius. However, these effects have been investigated in relation to the beam-front equilibria that occurs in Olson's theory. It was found¹⁴² that the self-consistent beam front "length," but not the beam front velocity, would vary if the pressure (or guide tube radius) varied axially. Thus adiabatic theory results indicate that gradients in p or R cannot be used to control the acceleration process. No enhanced ion energies were seen in pressure gradient experiments reported by Swain et al.³¹ Also in experiments reported by Tkach et al.³² an axial variation of the pressure by a factor of 10 produced only a factor of ~ 0.5 change in the beam front velocity (instead of a change of order 10). Thus it appears that simple passive control methods cannot be used to modify the existing collective acceleration process to achieve higher ion energies.

Recently, an active control method has been proposed by Olson, that may ultimately permit effective control of a steep beam front potential well over large distances.⁵⁹,¹⁰¹,¹⁰² In this scheme, the guide tube is In this scheme, the guide tube is filled with an appropriate working gas at a pressure lower than that used typically for ion acceleration, and low enough that ionization caused by the beam is negligible on the time scale of interest. An intense UV light source, e.g., a UV laser, is then used to photoionize the gas. By appropriately sweeping the UV laser, the beam front can be made to follow a predetermined motion. Estimates concerning laser powers required, and the expected ion output using modest IREB's, appear favorable.¹⁰¹

IREB/transverse sweep: A different concept is to transversely sweep an IREB so that ions will be accelerated by the net space charge density (of the IREB) in a direction essentially perpendicular to the IREB electron flow. Early suggestions involving highly-focused low current electron beams were given by Alfvén and Wernholm,³³ and by Johnson.⁹⁴ More by Alfven and Wernholm," recently, Kolomensky and Logachev have suggested schemes which include sweeping a long IREB "ray," and the "gyrotron."53,95-99 The gyrotron concept involves an IREB closed on itself (a large electron ring) that is to rotate about an axis which intersects the ring and its center. Ions injected near the axis are to slip out along the ring and gain kinetic energy as the ring rotates. At present, IREB's have not been successfully recirculated on themselves to form such an intense electron ring, although many studies of this problem have been made in the U.S. for other purposes. Even if such a ring could be formed, the idea of rotating it and keeping it intact appears formidable. A different idea, proposed by Olson, is to use a single controlled transverse sweep of an IREB that is injected transversely into a drift tube; the beam is transported to the tube (and deflected) in a region containing a charge-neutralizing plasma.^{53,100,101} Inside the tube, vacuum conditions permit the full space charge of the IREB to be used for collective acceleration. Estimates of the power required for the pulsed magnetic field for deflecting the beam, and accelerated ion estimates for existing IREB's appear favorable.¹⁰¹

<u>IRE3/vacuum</u>: As noted above, this case has already been investigated, 29-31,61,62 and recent results from Zorn et al.⁶³ will be reported at this meeting. Note, will be reported at this meeting. Note, however, that peak ion energies only of the order of a few times $Z_i \mathcal{E}_i$ appear possible with this method, and that it therefore does not appear to hold promise for accelerating ions to very high energies.

IREB/cyclotron wave: The autoresonant accelerator concept proposed by Sloan and Drummond¹¹⁹⁻¹²¹ is based on the assumption that a single, largeamplitude wave of the desired type (lower branch of the Doppler-shifted cyclotron mode) can be created when an un-neutralized IREB propagates in vacuum along a strong external magnetic field B2. The wave phase velocity is to be controlled by adiabatically decreasing B_Z axially. Basic problem areas include, e.g., studies of vacuum propagation of IREE's,¹⁴³ wave excitation methods, isolation of a single large-amplitude wave, stability studies, and studies of wave-trapping of ions. Some of these investigations are already in progress and results should be forthcoming soon. It should be noted, however, that a very large IREB is needed for this method to achieve the same accelerating fields that IREB space charge methods (discussed above) should achieve using a rather modest IREB.¹⁰¹

IREB/diode: A large amount of data now exists that indicates collectively accelerated ions occur in vacuum-filled and plasma-filled diodes.^{20,30,64-90} Mc More

diagnostics (such as time-resolved ion spectra) for various diode configurations would prove useful in isolating the acceleration mechanism(s). It should be noted that there is interest in understanding these collective acceleration phenomena in relation to controlled fusion studies using IREB diodes.¹³⁸ Also, since the "diode region" (i.e., the anode-cathode region) cannot be "extended" to a great length, it appears that IREB/diode configurations, in themselves, will not be useful for achieving very high ion energies. However, an IREB/diode configuration may prove useful as an ion source, or as an ion injector for other future collective-effect accelerators.

5. Conclusions

A summary has been given of collective ion acceleration research methods that involve intense relativistic electron beams (IREB's). Ion energies greater than the IREB electron energy have been observed (see Tables 2 & 3), and accelerating fields of order 1 MV/cm have been reported. An understanding now exists of the collective acceleration process for IREB injection into neutral gas or vacuum, whereas collective acceleration processes in IREB diodes are not currently understood. Present approaches to using IREB's for collective ion acceleration were discussed, and presumably one or more of these approaches may ultimately result in a viable working collective ion accelerator. The use of IREB's for collective ion acceleration research is still in its infancy.

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