

# 4D EMITTANCE DIAGNOSTIC FOR LOW ENERGY ION BEAMS



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## Abstract

Characterization of ion beams from an ion injector consisting of an electron-cyclotron-resonance (ECR) source in combination with a low-energy-beam-transport (LEBT) typically exhibits a complex four-dimensional transverse phase-space distribution. The importance of measuring the ion beam correlations following extraction and transport of the low-energy beam is critical to enabling optimization of beam transmission through downstream accelerating structures. A design for a transverse, four-dimensional emittance meter for low-energy protons from the Ion Linac Systems (ILS) ECR-LEBT ion injector is provided.

## Introduction

Detailed knowledge of the transverse beam parameters is essential to enable proper optimization of beam transmission in downstream accelerating structures. Procedures to measure the two-dimensional (2D) transverse beam parameters, where horizontal and vertical motions are separate, have been well established. However, various beamline elements such as skew quadrupole magnets, solenoids, and beamline element field asymmetries generate a correlation between the horizontal and vertical components. The purpose of this diagnostic is to characterize the four-dimensional (4D) beam phase space distribution by capturing multiple downstream transverse (xy) images allowing potential correction of transverse coupling from the source. There are two strategies to properly characterize the 4D emitted beam: the *single-optics/multiple-locations* strategy proposed by Woodley and Emma [1] and the *multiple-optics/single-location* strategy given by Prat and Aiba [2]. The first strategy proposes a long beam line of roughly 150 m consisting of six profile monitors and ~ 15 quadrupole magnets. The second involves having the 2D beam parameters measured at a single location and having quadrupole strengths change to generate the required optics for the 4D reconstruction. Due to the lack of 150 m of space required to perform the first method, the second method is used for this diagnostic.

## 4D Transverse Beam Characterization

The 4D beam matrix describes the transverse properties of the beam:

$$\sigma^{4D} = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle & \langle x'y \rangle & \langle x'y' \rangle \\ \langle xy \rangle & \langle x'y \rangle & \langle y^2 \rangle & \langle yy' \rangle \\ \langle xy' \rangle & \langle x'y' \rangle & \langle yy' \rangle & \langle y'^2 \rangle \end{pmatrix} = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{xy}^T & \sigma_{yy} \end{pmatrix} \quad (1)$$

The matrices  $\sigma_{xx}$  and  $\sigma_{yy}$  describe the 2D horizontal and vertical motions, and  $\sigma_{xy}$  describes the cross-plane coupling. The transport of the 4D beam matrix from  $s_0$  to  $s$  can be calculated as follows:

$$\sigma_s^{4D} = R \sigma_{s_0}^{4D} R^T \quad (2)$$

Where R between  $s_0$  and  $s$  is:

$$R = \begin{pmatrix} R_{11} & R_{12} & R_{13} & R_{14} \\ R_{21} & R_{22} & R_{23} & R_{24} \\ R_{31} & R_{32} & R_{33} & R_{34} \\ R_{41} & R_{42} & R_{43} & R_{44} \end{pmatrix} = \begin{pmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{pmatrix} \quad (3)$$

According to Eqs. (1), (2), and (3), when the lattice between  $s_0$  and  $s$ , the elements  $R_{yx}$  and  $R_{xy}$  are zero allowing the beam sizes and x-y correlation to be expressed in terms of the matrix elements of  $\sigma^{4D}$  as follows:

$$\langle x^2 \rangle_s = R_{11}^2 \langle x^2 \rangle_{s_0} + R_{12}^2 \langle x'^2 \rangle_{s_0} + 2R_{11}R_{12} \langle xx' \rangle_{s_0},$$

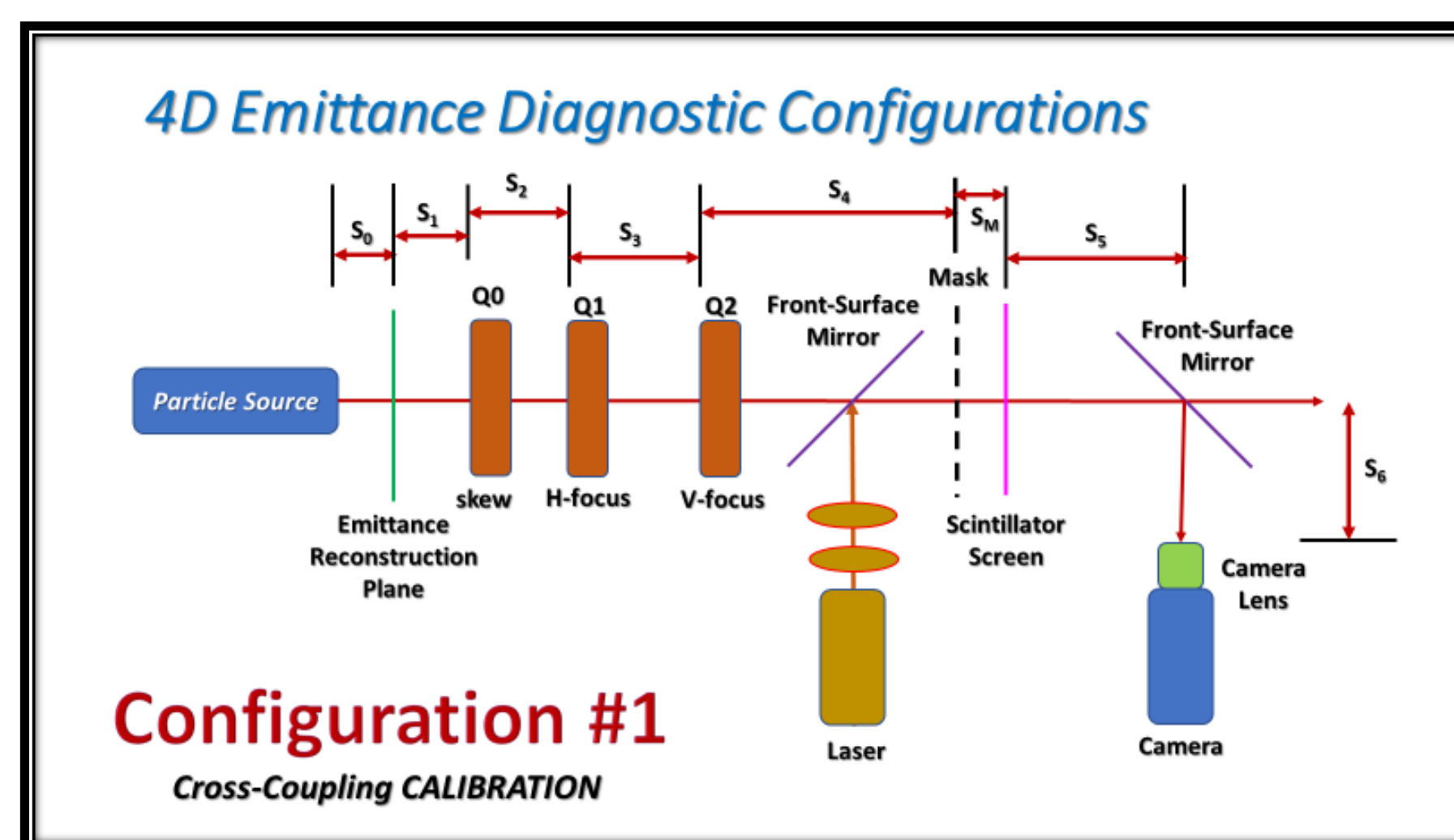
$$\langle y^2 \rangle_s = R_{33}^2 \langle y^2 \rangle_{s_0} + R_{34}^2 \langle y'^2 \rangle_{s_0} + 2R_{33}R_{34} \langle yy' \rangle_{s_0},$$

$$\langle xy \rangle_s = R_{11}R_{33} \langle xy \rangle_{s_0} + R_{12}R_{33} \langle x'y \rangle_{s_0} + R_{11}R_{34} \langle xy' \rangle_{s_0} + R_{12}R_{34} \langle x'y' \rangle_{s_0}.$$

Assuming the transport matrix elements are known, the 10 independent elements of  $\sigma^{4D}$  at  $s_0$  can be computed by measuring beam sizes and x-y correlations at the point  $s$ . The initial simulation considered 8 captured images. Future simulations will map out the emittance sensitivity as a function of the number and quality of capture images.

## Simulation of Diagnostic

Presently we plan to validate the 4D emittance diagnostic using the Ion Linac Systems (ILS) Electron Cyclotron Resonance (ECR) 30 keV ion source. The initial layout of the 4D emittance diagnostic is depicted below including a pepperpot 4D emittance diagnostic for cross-checking:



The system length is 1m long in total and follows the ProLAB build below (Fig. 1). The quadrupoles themselves are 0.1 m in length separated by 0.1 m with an aperture radius of .1m. For the initial emittance, 3 main values were used in order of complexity (Fig. 1 -3). Using PRO Lab, simulations at 8 different quadrupole strengths ranging from 0 to 20 kG/m for the H-focusing quadrupole, and 0 to -20 kG/m for the V-focusing quadrupole in steps of 2.5 kG/m (example shown in Fig. 4) for a total of 8 unique emittances.

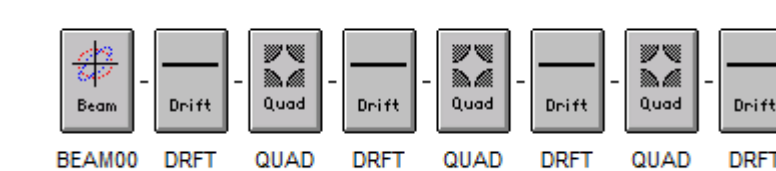


Fig:1

Sigma Matrix (ij) (mm & mrad)		2		3		4		5		6	
j=1		j=1		j=1		j=1		j=1		j=1	
1	4.000000	-0.323676	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
2	-0.323676	1.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
3	0.000000	0.000000	4.000000	-0.097883	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
4	0.000000	0.000000	-0.097883	1.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
5	0.000000	0.000000	0.000000	0.000000	8.544068	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000
6	0.000000	0.000000	0.000000	0.000000	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

Fig:2

Sigma Matrix (ij) (mm & mrad)		2		3		4		5		6	
j=1		j=1		j=1		j=1		j=1		j=1	
1	4.000000	-0.323676	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
2	-0.323676	1.000000	2.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
3	0.000000	2.000000	4.000000	-0.097883	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
4	0.000000	0.000000	-0.097883	1.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
5	0.000000	0.000000	0.000000	0.000000	8.544068	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000
6	0.000000	0.000000	0.000000	0.000000	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

Fig: 3

Sigma Matrix (ij) (mm & mrad)		2		3		4		5		6	
j=1		j=1		j=1		j=1		j=1		j=1	
1	4.000000	-0.323676	0.400000	0.200000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
2	-0.323676	1.000000	2.000000	0.100000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
3	0.400000	2.000000	4.000000	-0.097883	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
4	0.200000	0.100000	-0.097883	1.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
5	0.000000	0.000000	0.000000	0.000000	8.544068	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000
6	0.000000	0.000000	0.000000	0.000000	73.001096	-0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

Fig: 4

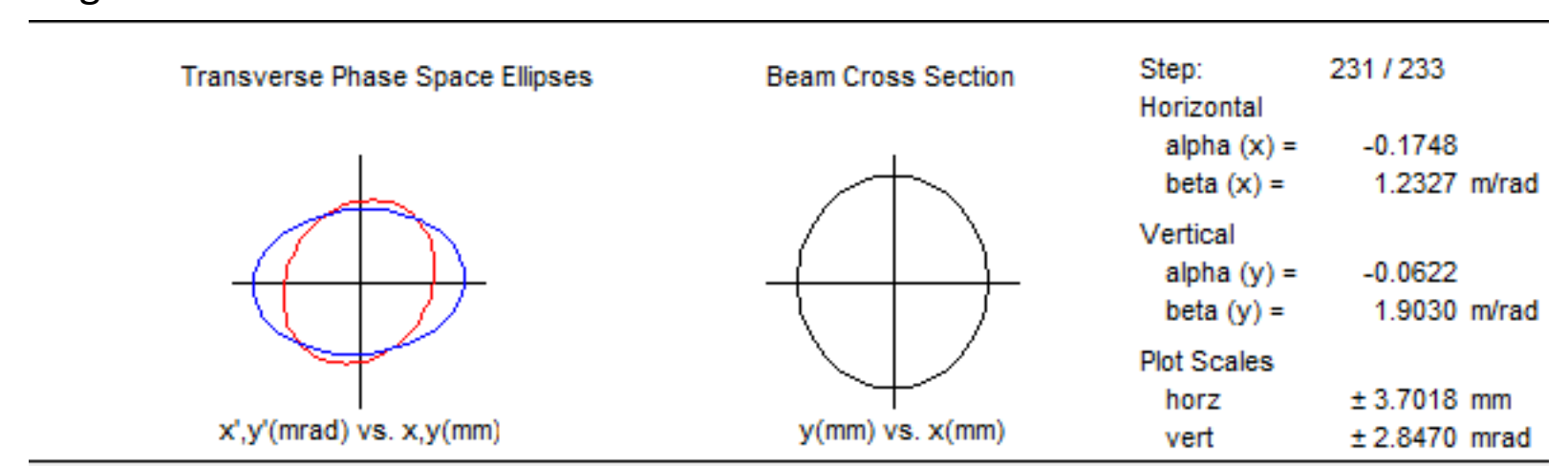


Fig: 5

Using the alpha and beta values given at the profile monitor allows for the reconstruction of the 4D matrix using the math described previously.

## Next Steps

Four-dimensional measurements are needed to understand the emittance increase due to cross-plane coupling. The simulations run in ProLAB show that the use of this diagnostic will allow for the reconstruction of the 4D beam matrix. The next steps are first to do a comprehensive sensitivity analysis to quantify the emittance uncertainty as a function of the number of captured images and reconstruction analysis. Next steps also include developing the hardware components needed for the diagnostic (Bill of Materials (BOM)), detailed layout, procurement packages, image capture and analysis software. Although the diagnostic is specifically planned for factory acceptance testing (FAT) of the proton ion source for the ILS Hungary project we also wish to quantify how modifications to the design would enable characterization of electron beams.

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2. E. Prat and M. Aiba, Four-dimensional transverse beam matrix measurement using the multiple-quadrupole scan technique, Paul Scherrer Institute, CH-5232 Villigen PSI, Switzerland (Received 10 July 2013; published 19 May 2014)