

Understanding Q slope of superconducting cavity with magnetic defect and field emission

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Heetae Kim

**Rare Isotope Science Project, Institute for Basic Science, Daejeon 34000, Republic
of Korea**



- **Vertical test facility**
- **Magnetic heating and field emission**
- **Q slope measurement for QWRs and HWRs**
- **Magnetic heating effect for QWRs**
- **Field emission and x-ray effect for HWRs**
- **Summary**

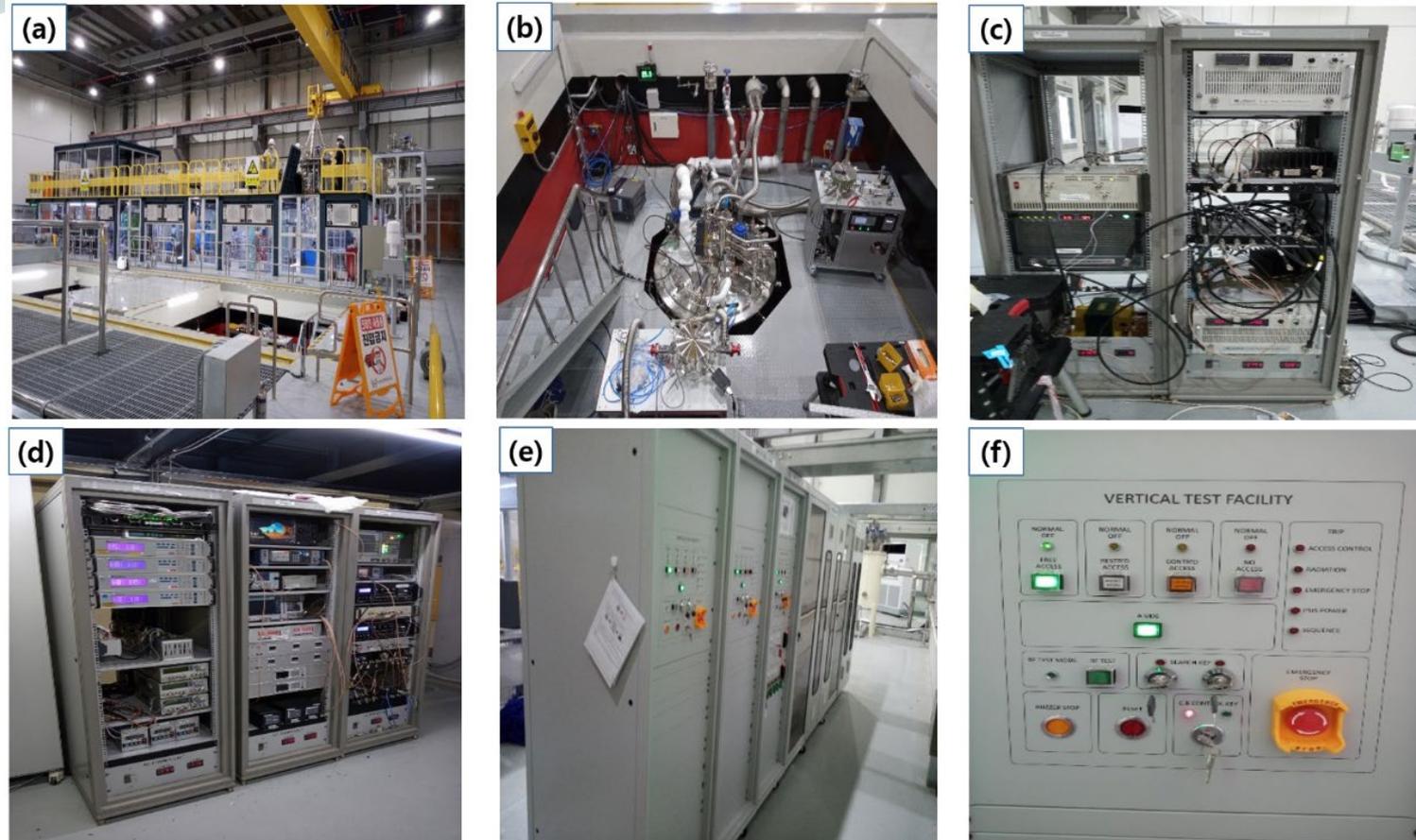


Figure 1: Pictures of the vertical test facility. (a) shows the overview of the vertical test site, (b) shows both the vertical test pit and the cryostat, (c) shows the solid state power amplifier (SSPA), (d) shows the control racks, (e) shows the personal safety interlock system (PSIS), and (f) shows the control panel for the PSIS.

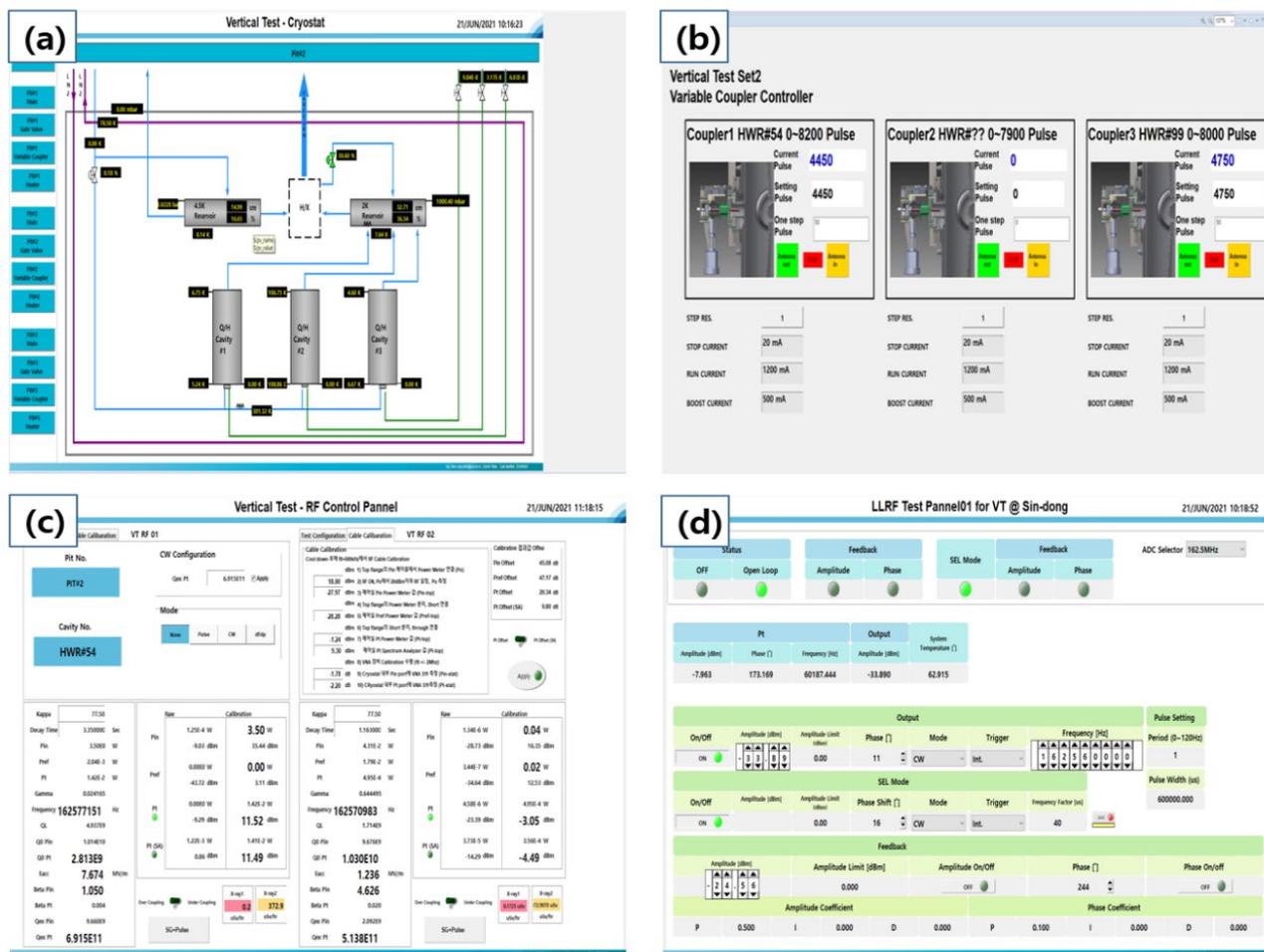


Figure 2: Pictures of the human-machine interface (HMI) for vertical test. (a) shows the control panel of the cryostat, (b) shows the control panel of the variable couplers, and both (c) and (d) show the control panels of the low-level radio frequency (LLRF).

● $Q_o = \frac{2\pi f \mu \int |H(r)|^2 dV}{\int R_{\text{Sur}} |H(r)|^2 dS}$: Quality factor is expressed with magnetic field

$Q_o = \frac{G}{R_{\text{Sur}}}$: Quality factor is expressed with surface resistance

$R_{\text{Sur}} = R_{\text{Res}} + R_{\text{BCS}}$: Surface resistance

$P_{\text{dis}} = \frac{1}{2} \int R_s |H(r)|^2 dS$: Dissipated power on cavity surface

$R_{\text{BCS}} = \frac{C_1 f^2}{T} \exp\left(-\frac{\Delta}{k_B T}\right)$: BCS resistance comes from AC current

$\Delta = \Delta_0 - \text{MB}_{\text{peak}}$: Band gap is reduced by magnetic defects

$R_{\text{Sur}} = \frac{C_1 f^2}{T} \exp\left(-\frac{\Delta_0}{k_B T} + \frac{\text{MB}_{\text{peak}}}{k_B T}\right) + R_{\text{Res}}$: Surface resistance is expressed with magnetic moment and residual resistance

Field emission and x-ray counting rate

Fermi energy of Nb : 5.3 eV

Work function of Nb : 4.3 eV

$$J = \frac{e\sqrt{E_F} F^2}{2\pi h(\Phi_W + E_F)\sqrt{\Phi_W}} e^{-4k\Phi_W^{1.5}/3F} \quad : \text{Field emission (FE) current density}$$

$$I = \frac{Ae\sqrt{E_F} F^2 \beta^2 \sin^2 \omega t}{2\pi h(\Phi_W + E_F)\sqrt{\Phi_W}} e^{-4k\Phi_W^{1.5}/3F\beta \sin \omega t} \quad : \text{Field emission current for AC}$$

$$\langle I \rangle = \frac{C_2 e\sqrt{E_F} F^{2.5} \beta^{2.5}}{h\sqrt{k}(\Phi_W + E_F)\Phi_W^{0.75}} e^{-4k\Phi_W^{1.5}/3F\beta} \quad : \text{Average FE current for AC}$$

$$I_{X\text{-ray}} = I_0 + \frac{\alpha_X S \sqrt{E_F} F^{2.5} \beta_X^{2.5}}{(\Phi_W + E_F)\Phi_W^{0.75}} e^{-4k\Phi_W^{1.5}/3F\beta_X} \quad : \text{X-ray counting rate with x-ray field enhancement factor}$$

- The field emission generates electrons from the surface of the superconducting cavity. The generated electrons and ionized ions are accelerated and eventually generate x-ray in the cavity, which is called bremsstrahlung radiation. It is expected that the generated x-ray is proportional to the current coming from the field emission.

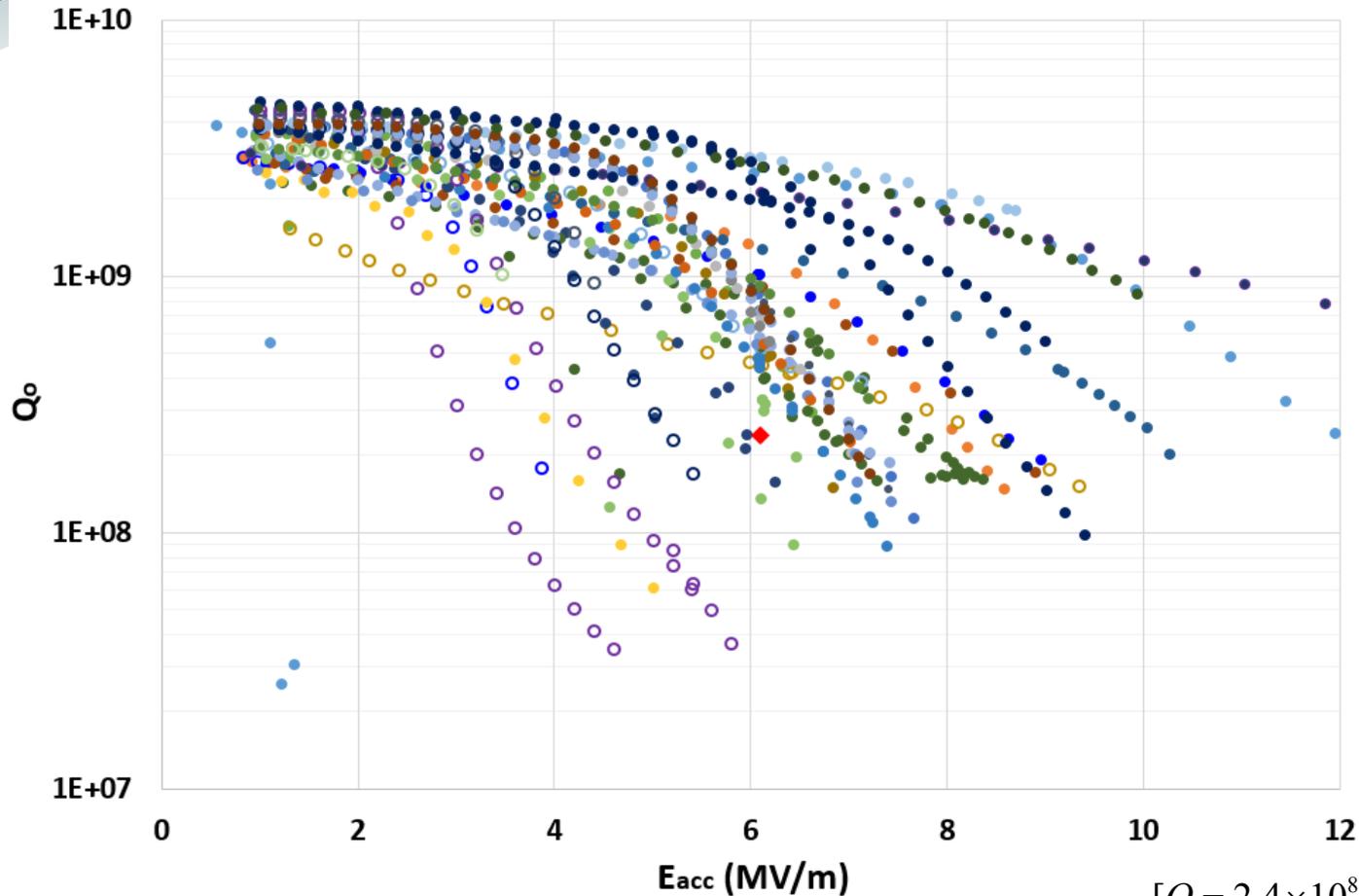


Figure 3: Q slope measurement as a function of accelerating electric field for the quarter-wave resonator (QWR) cavities at 4.2 K. This data shows the failed and passed QWR. The total number of the QWRs is 22 and all of them are passed.

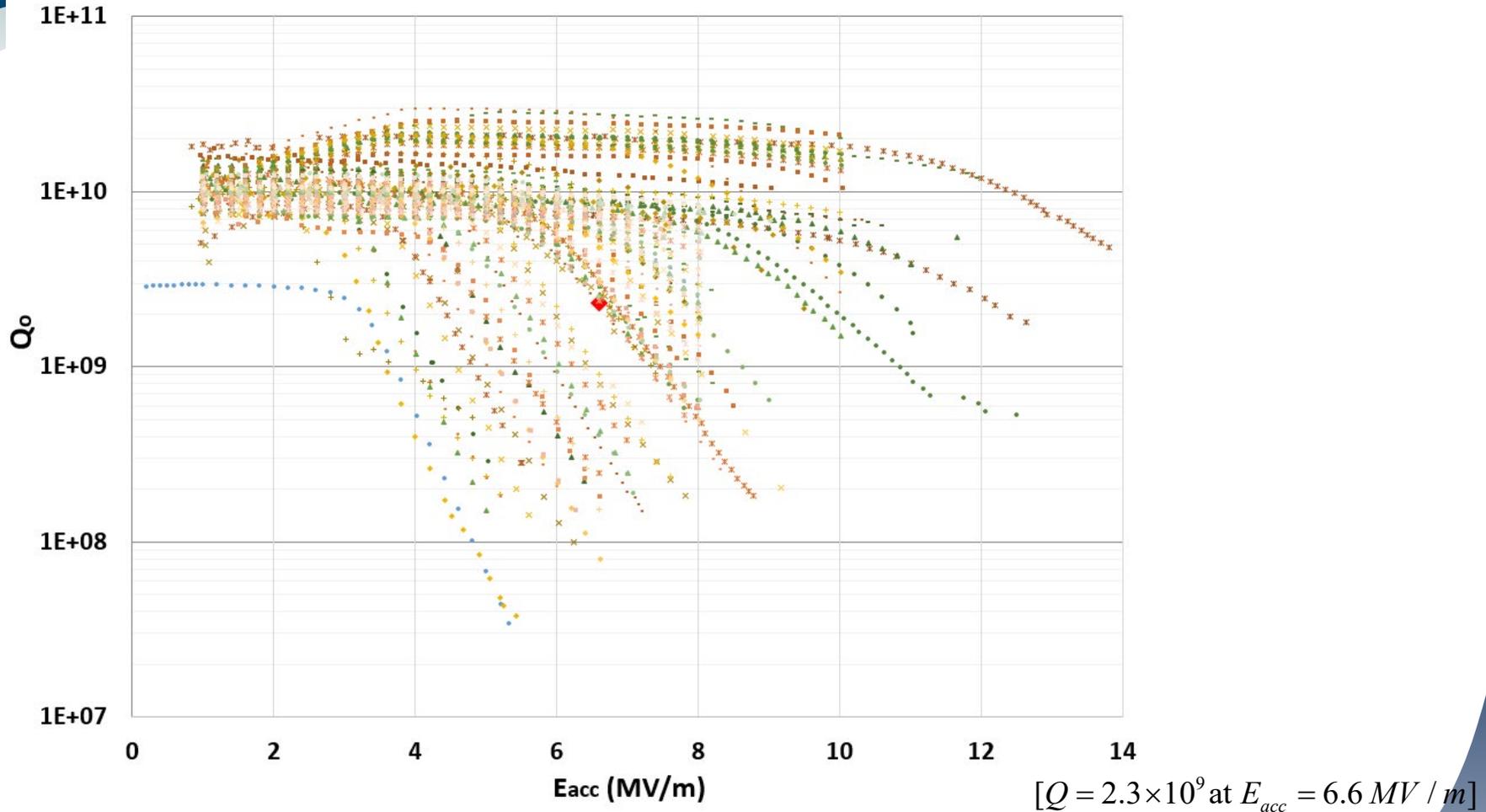
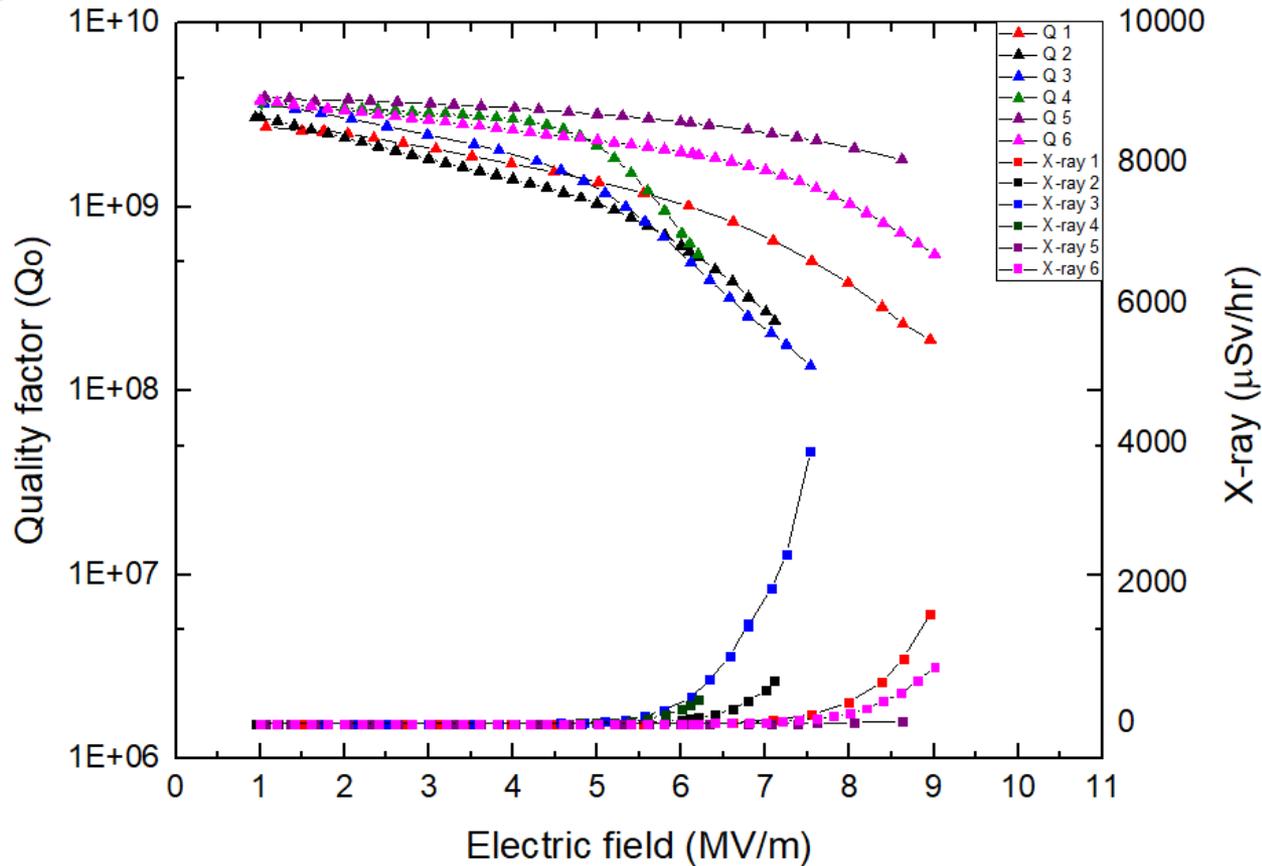


Figure 4: Q slope measurement as a function of accelerating electric field for the half-wave resonator (HWR) cavities at 2 K. This data shows the failed and passed HWR. The total number of the HWRs is 106 and all of them are passed.



Requirement for QWR :

$$Q = 2.4 \times 10^8$$

at $E_{acc} = 6.1 \text{ MV} / \text{m}$

at 4.2 K

$$f = 81.25 \text{ Mhz}$$

Figure 5: Q slope measurement as a function of accelerating electric field for the quarter-wave resonator (QWR) cavities.

The Q factor decreases as the accelerating electric field is increased.

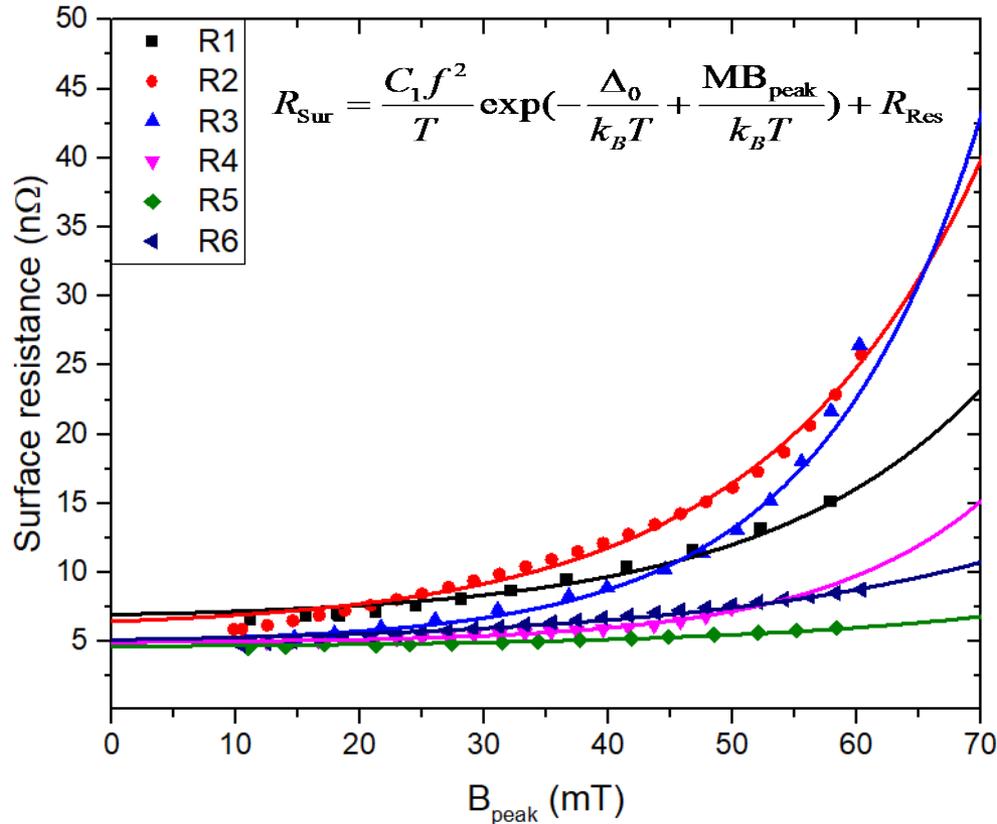
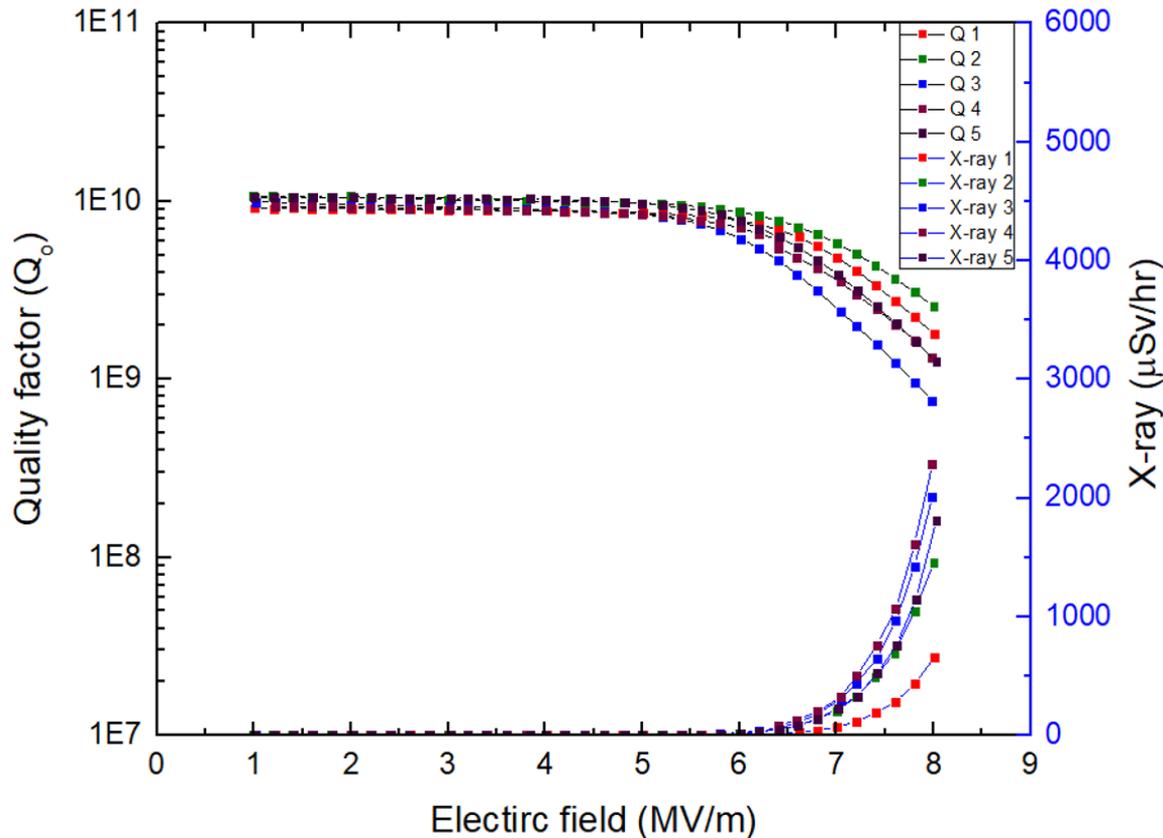


Figure 6: Magnetic heating effect of the surface resistances for quarter-wave resonator (QWR) cavities. The magnetic heating causes the quality factor decreases. The surface resistances for the QWR cavities are fitted with the magnetic heating equation.

Magnetic moments for QWR 1, 2, 3, 4, 5 and 6 are as follows:

$$M = 3.3 \times 10^{-21}, 3.4 \times 10^{-21}, 4.4 \times 10^{-21}, 4.3 \times 10^{-21}, 2.5 \times 10^{-21}, \text{ and } 2.3 \times 10^{-21} [\text{J/T}].$$

Surface resistance increases with the magnetic moment of QWR cavity.



Requirement for HWR :

$$Q = 2.3 \times 10^9$$

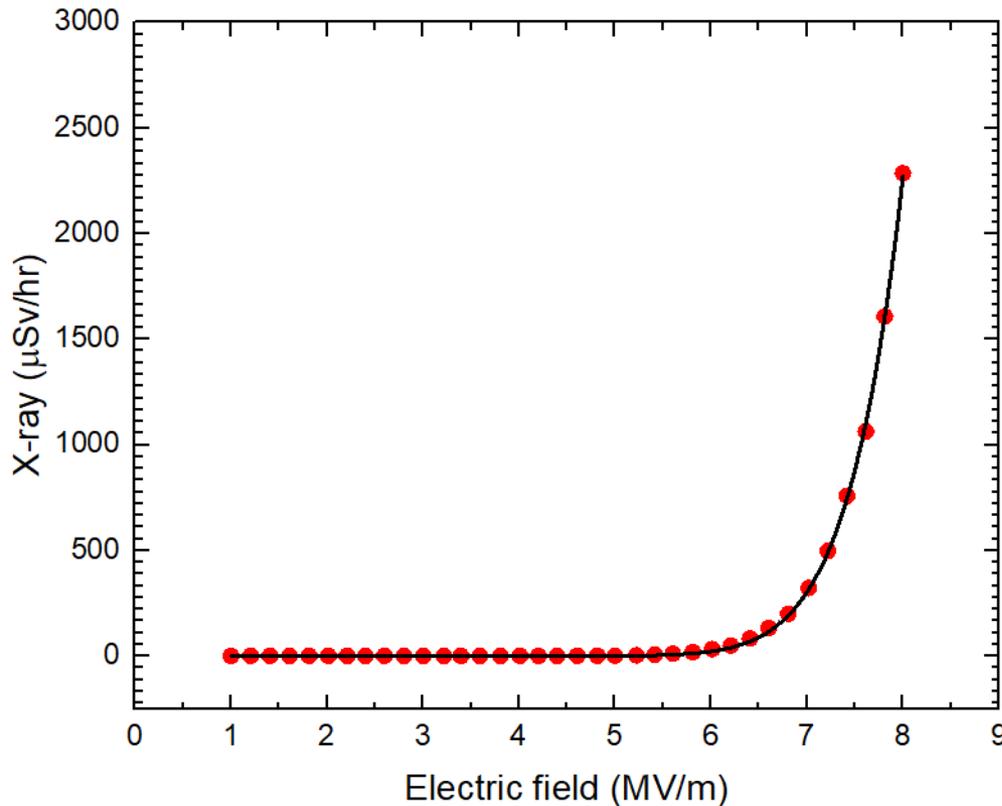
at $E_{acc} = 6.6 \text{ MV} / m$

at 2 K

$$f = 162.5 \text{ Mhz}$$

Figure 7: Quality factors shown as a function of electric field for five different half-wave resonator (HWR) cavities.

- The quality factors are almost constant in the range of low accelerating electric field below 5 MV/m and decreases as the x ray radiation is increased in the range of the accelerating electric field above 5 MV/m.



$$I_{X\text{-ray}} = I_0 + \frac{\alpha_X S \sqrt{E_F} F^{2.5} \beta_X^{2.5}}{(\Phi_W + E_F) \Phi_W^{0.75}} e^{-4k\Phi_W^{1.5}/3F\beta_X}$$

$$I_0 = 0.1 \mu\text{Sv} / h$$

$$\beta_X = 646$$

Figure 8: X-ray counting rate shown as a function of accelerating electric field for the half-wave resonator (HWR). The field emission increases as the accelerating electric field is increased. The x-ray is generated when the electrons emitted from the field emission and ionized gases are decelerated due to bremsstrahlung radiation.

The x-ray increases as the accelerating electric field is increased.

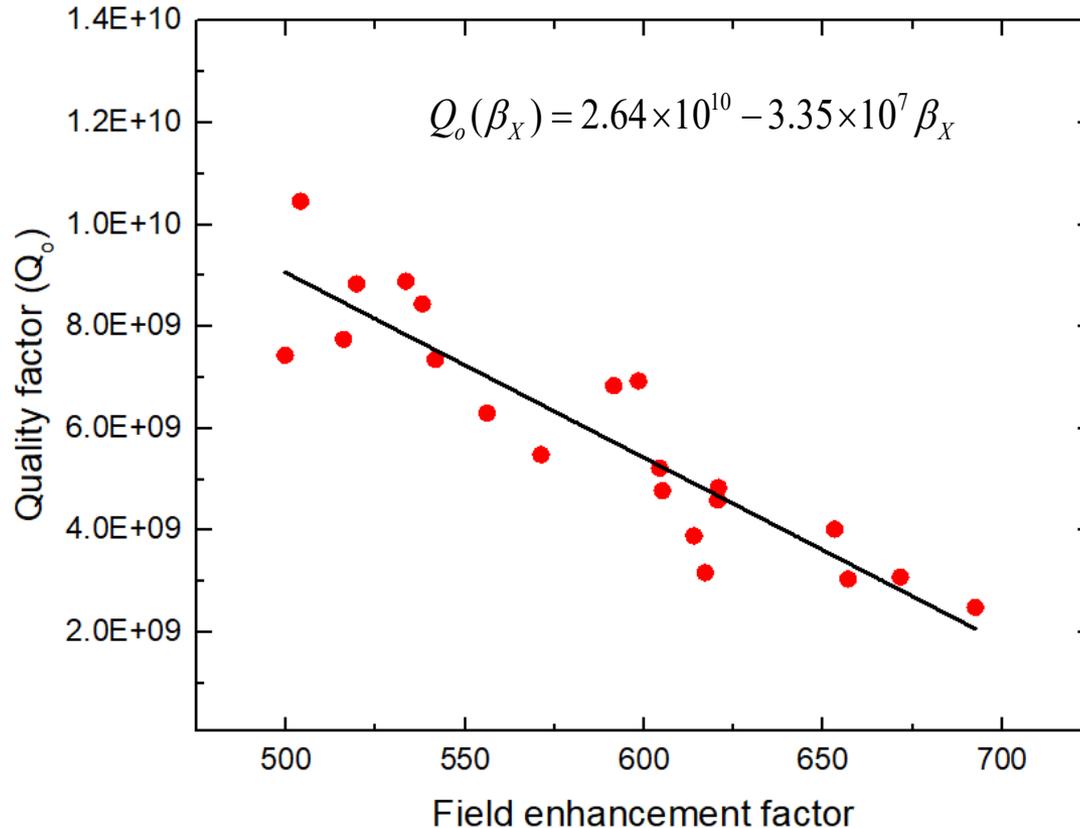


Figure 9: Quality factor of the half-wave resonators (HWRs) shown as a function of x-ray field enhancement factor.

- The quality factor for the half-wave resonators (HWRs) decreases linearly as the x-ray field enhancement factor is increased.

- **Magnetic heating and field emission are introduced.**
- **Vertical test is performed for the QWRs and HWRs.**
- **Q slopes for the QWRs and HWRs are measured.**
- **Magnetic heating effect for the QWRs is investigated.**
- **Field emission effect for the HWRs is studied.**
- **Quality factor of the HWRs decreases linearly with the x-ray field enhancement factor.**

Thank you for your attention

