

# DESIGN CONSIDERATION OF A LONGITUDINAL KICKER CAVITY FOR COMPENSATING TRANSIENT BEAM LOADING EFFECT IN SYNCHROTRON LIGHT SOURCES\*

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## Abstract

In ultra-low-emittance synchrotron light sources, bunch-lengthening using the combination of main and harmonic cavities is limited by the transient beam-loading (TBL) effect. To manage this effect, we proposed a TBL compensation technique using a wide-band longitudinal kicker cavity. In this paper, we reported our conceptual design of the kicker cavity. We considered the cavity design by assuming the beam parameters of the KEK-LS. We employed the single-mode (SM) cavity concept so that harmful HOMs were damped by rf absorbers on beam pipes. Using this kicker cavity with a double rf system, bunch lengthening by a factor of 4.3 (i.e., 40.9 ps) was expected for the KEK-LS case.

## INTRODUCTION

Ultra-low-emittance synchrotron light sources aim at achieving the horizontal beam emittance of less than sub nm-rad. This ultra-low-emittance causes the intra-beam scattering (IBS) which increases the emittance and shortens the Touschek lifetime. To mitigate the IBS, bunch-lengthening using the combination of main and harmonic cavities [1] is an effective solution.

In such a double rf system, the bunch-lengthening performances were limited due to the transient beam-loading (TBL) effect when the large bunch gaps were introduced [2]. To manage this effect, we proposed a TBL compensation technique using a wide-band longitudinal kicker cavity [3]. In this paper, we discuss critical issues concerning the kicker cavity design, and propose a 1.5 GHz, single-mode-type cavity as a promising solution.

## TBL COMPENSATION TECHNIQUE USING A KICKER CAVITY

In the previous study and this study, we set our goal to compensate the TBL effect in a planned KEK Light Source (KEK-LS). Parameters assumed in the studies were shown in Tables 1 and 2. Without the compensation, the bunch lengthening using the double RF system was limited by the TBL voltages induced in the main and harmonic cavities. The bunch length was estimated to be 30.5 ps while that without

the TBL effect was estimated to be 42.5 ps [3]. To compensate the TBL voltage, we proposed a TBL compensation technique using a wide-band longitudinal kicker cavity [3,4]. In this study, we assumed the kicker cavity having a 3-dB bandwidth of 5 MHz as a time response. The 3-dB bandwidth ( $\Delta f$ ) was defined as  $\Delta f = f_a/Q_L$ . Here,  $f_a$  was the resonance frequency and  $Q_L$  was the loaded  $Q$  of the kicker cavity. The parameters of the kicker cavity assumed in the previous work were shown in Table 3. Assuming these values, the bunch length with the compensation scheme was estimated to be 40.9 ps.

Table 1: Beam Parameters of the KEK-LS without Losses of Insertion Devices [5]

Parameters	Value
Beam energy	3 GeV
Momentum compaction factor	$2.2 \times 10^{-4}$
Average beam current	0.5 A
RF frequency (fundamental)	500.07 MHz
Harmonic number	952
Number of bunch gaps	2
Number of buckets in a gap	30
Revolution frequency	525 kHz
Synchrotron frequency	2.65 kHz
Longitudinal radiation damping time	22.63 ms
Horizontal radiation damping time	29.25 ms
Vertical radiation damping time	38.28 ms
Natural bunch length	9.5 ps

Table 2: Parameters of the Double RF System [3]

Parameter	Main RF	Harmonic RF
RF Voltage	2.5 MV	777 kV
Synchronous phase	1.178 rad	-1.708 rad
Tuning angle	-0.962 rad	1.433 rad
Total $R/Q$	875 $\Omega$	386 $\Omega$
Cavity coupling coefficient	3.5	0.27

## DESIGN CONSIDERATION OF THE KICKER CAVITY

We investigated a realistic cavity design which could provide the same compensation performance as the previous

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Table 3: Parameters of the Kicker Cavity Assumed in the Previous Work [3]

Parameter	Value
Resonance frequency	500 MHz
Cavity voltage	45 kV
-3 dB bandwidth	5 MHz
Loaded $Q$	100
$R/Q$	175 $\Omega$
Coupling coefficient	399

study. In addition, we had two concerns : cost of the cavity and the higher-order-modes (HOMs) in the kicker cavity. The cost should be as low as possible and the HOMs should be damped sufficiently in order to avoid coupled-bunch instabilities (CBIs).

The considered parameters were listed in Table 4. The kicker cavity should generate the RF voltage which was comparable to the TBL voltages induced in the main and harmonic cavities. The resonance frequency of the kicker cavity should be harmonics of the fundamental radio frequency. We investigated suitable radio frequency among the 1st to 3rd harmonics of the fundamental frequency. The bandwidth of the kicker cavity should be wide enough to compensate a fast variation of the TBL voltage.  $\Delta V_b$ , which was the subtraction between the maximum and minimum TBL voltage induced in the kicker cavity, should be enough lower than the generator voltage. The above four parameters were essential to achieve the same compensation performance as the previous study.

The cavity input power should be as low as possible for the cost reduction. The low  $R/Q$  was essential to employ the single-mode (SM) cavity concept [6]. The SM cavity has a large beam hole so that the HOMs are damped by rf absorbers on beam pipes. Since the SM cavity had no HOM dampers in its outer periphery, this concept enabled us to realize a very compact cavity. In this section, we examined an optimum resonance frequency and  $R/Q$  to satisfy the requirement of  $\Delta V_b$  and input power.

Table 4: The List of Parameters Should be Considered in the Design

Parameter	Value
Generator voltage	50 kV
Resonance frequency	$0.5 \times n$ GHz
3 dB bandwidth	5 MHz
$\Delta V_b$	$\leq 5.5$ kV
Cavity input power	Minimize
$R/Q$	$\leq 80 \Omega$

### Examine of the $\Delta V_b$

When the TBL voltage was semi-analytically calculated [3], the  $\Delta V_b$  was approximated to be

$$\Delta V_b \sim \frac{\{1 - \exp(-N_g \alpha)\} \{V_0(N_b) - \frac{V_{b0}}{2} \exp(-N_g \alpha)\}}{1 - \exp\{-(N_g + N_b) \alpha\}}, \quad (1)$$

where

$$\alpha = \pi \Delta f T_b (1 - j \tan \psi), \quad (2)$$

$$V_{b0} = \pi f_a \frac{R}{Q} q \quad (3)$$

and

$$V_0(N_b) = -\frac{V_{b0}}{2} + V_{b0} \sum_{m=0}^{N_b} \exp(-m\alpha). \quad (4)$$

Here,  $N_g$  was a number of buckets in a single gap and  $N_b$  was a number of buckets in a single bunch train.  $T_b$  was a bunch interval,  $q$  was a charge of a single bunch.  $\psi$  was a tuning angle of the kicker cavity and set to be 0 in this study. From Eqs. (1)-(4),  $\Delta V_b$  was proportional to  $f_a R/Q$ . Figure 1 showed the correlation between  $\Delta V_b$  and  $R/Q$ . To make  $\Delta V_b$  less than the upper limit shown in Fig. 1,  $f_a R/Q$  should be smaller than  $87.5 \text{ GHz} \cdot \Omega$ .

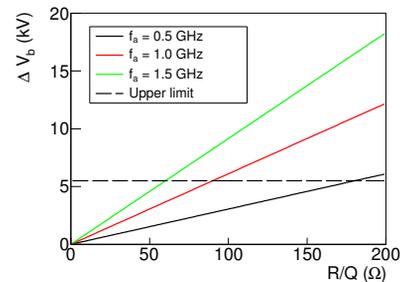


Figure 1: The correlation between  $\Delta V_b$  and  $R/Q$  with 50 kV of  $V_g$  and 5 MHz of  $\Delta f$ .

### Examine of the Input Power

The input power of the cavity was described as

$$P_g = \frac{(1 + \beta^2)}{4\beta R} V_g^2 \sim \frac{\Delta f}{4f_a} \frac{1}{R/Q} V_g^2 \quad (5)$$

[7] since RF coupling of the kicker cavity, which was defined as  $\beta$ , was large as shown in Table 3. Here,  $V_g$  represented the generator voltage of the kicker cavity. From Eq. (5),  $P_g$  was inversely proportional to  $f_a R/Q$  while  $\Delta V_b$  was proportional to  $f_a R/Q$ . Figure 2 showed the correlation between  $P_g$  and  $R/Q$ .  $R/Q$  should be as small as possible to reduce the cost. Hence,  $f_a R/Q$  should be equal to  $87.5 \text{ GHz} \cdot \Omega$ .

The best values of  $R/Q$  for each resonance frequency was shown in Table 5. Only at the resonance frequency of the 1.5 GHz, the value of  $R/Q$  was smaller than  $80 \Omega$ . We decided to employ 1.5 GHz as the resonance frequency of the kicker cavity.

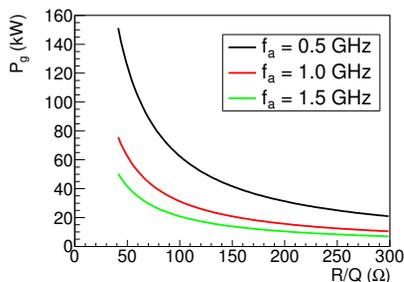


Figure 2: The correlation between  $P_g$  and  $R/Q$  with 50 kV of  $V_g$  and 5 MHz of  $\Delta f$ .

Table 5: The Best Values of the  $R/Q$  for Each Resonance Frequency

Resonance frequency	Value of $R/Q$
500 MHz	175 $\Omega$
1.0 GHz	88 $\Omega$
1.5 GHz	58 $\Omega$

## DESIGN OF THE KICKER CAVITY

We scaled down the original shape of the SM cavity at first. Then, we optimized the shape of the kicker cavity using 3D electromagnetic simulation (CST [8]). Figure 3 showed the 3D view of the kicker cavity after the optimization. The TM010 mode was resonated as the longitudinal kick field and the kicker cavity was a normal conducting cavity. We employed the Pillbox shape of the cavity to reduce the  $R/Q$  from the original paper. We also optimized the shape of waveguides, the position and material of the absorber. At the top and bottom of the cavity had large through hole (48 mm×55.7 mm) to realize large RF coupling. The absorber was made of ferrite (IB-004). The power loss at the absorber was estimated to be 250 W with 50 kV of  $V_g$ . We estimated the parameters of the cavity using eigenmode and frequency domain solver as shown in Table 6 and compared two results. Two results agreed well each other and satisfied our requirements of the TBL compensation.

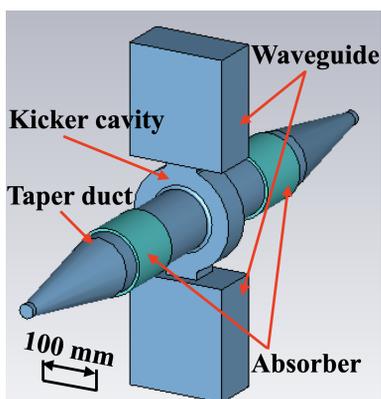


Figure 3: 3D view of the kicker cavity.

Table 6: Parameters of the Designed Kicker Cavity Under  $V_g = 50$  kV

Parameter	Eigenmode	Frequency domain
Frequency	1.50001 GHz	1.50003 GHz
$R/Q$	59.23 $\Omega$	59.54 $\Omega$
$Q$	16853	16814
$Q_L$	296	291
$P_c$	2.52 kW	2.53 kW
Max power density	26.6 W/cm <sup>2</sup>	25.1 W/cm <sup>2</sup>

We also evaluated the coupling impedance of the kicker cavity using the CST. Figure 4 showed the frequency dependence of the coupling impedance. Left figure showed the coupling impedance in the longitudinal direction and right figure showed that in the transverse direction. Red lines showed the threshold of the coupled bunch instability calculated from the radiation damping ratio shown in Table 1. In the left figure, the coupling impedance of the TM010 mode was bigger than the threshold. This peak could not become a problem since a growth rate calculated from this peak was almost zero. The residual peaks were smaller than the threshold and the kicker cavity was expected to work stably.

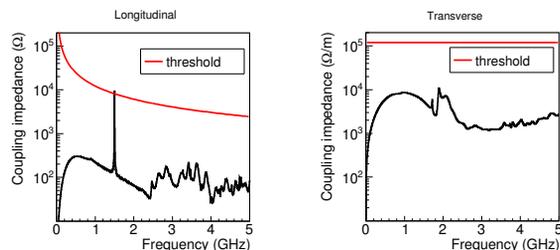


Figure 4: Frequency dependence of the coupling impedance.

## CONCLUSION

We designed a wide-band longitudinal kicker to compensate the TBL voltage induced in the main and harmonic cavity. In the consideration of the design, we investigate the requirements of the resonance frequency and the  $R/Q$  against the  $\Delta V_b$  and the  $P_g$ . We employed the single-mode cavity concept so that harmful HOMs were damped by rf absorbers on beam pipes. At the KEK-LS case, the resonance frequency of 1.5 GHz was found to be suitable in order to satisfy our requirements and employ the single-mode cavity concept. We optimized and evaluated the design of the kicker cavity using 3D electromagnetic simulation. The designed cavity satisfied our requirements and the coupling impedance of the cavity was estimated to be enough small at the KEK-LS case.

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