COMPARISON OF PROFILE MEASUREMENTS AND TRANSPORT BEAM ENVELOPE PREDICTIONS ALONG THE 80-m LANSCE pRad BEAMLINE*

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Abstract

Here we report a comparison between the simulation of beam phase-space and profile distributions with diagnostic measurements. TRANSPORT, a particle transport code, was used for the prediction of a 800 MeV proton beam envelope from the end of the linac to the proton radiography (pRad) facility (a total length of 80 meters). The beam profile was measured at key positions along the beamline using wire scanners and gated CCD camera systems. These measurements were compared to their respective points along the simulated beamline. The predicted beam envelope and measured data correspond within expected errors.

INTRODUCTION

The Proton Radiography (pRad) [1,2] experimental facility is one of six user facilities at the Los Alamos Neutron Science Center (LANSCE) [1,3]. An H⁻ beam is accelerated using a Drift Tube Linac (DTL) and a Couple Cavity Linac (CCL) to an energy of 800 MeV and transported to pRad. The beam transport line, starting at the end of the 800 MeV linac, is composed of many bending and focusing elements before it reaches the pRad beam optics system. The beam spot size requirement is nominally 2 mm (RMS). Small field variations of the beamline quadrupoles and/or bending magnets from the standard tune can lead to unwanted radiation spill, and potential beamline elements damage. Therefore, simulation of the beam envelope throughout the beamline is crucial in understanding the beam bunch distribution during transport. Good agreement with diagnostics measurements significantly improves our ability to predict beamline performance under various beam conditions.

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In this report, we present the beam sizes obtained using the Fermilab modified version of the TRANSPORT [4] beam envelope code, as well as size measurements along the beamline. The input beam parameters for the code were extracted from emittance measurements at the end of the linac. The longitudinal input beam parameters were extrapolated from lower-energy data. New length and magnetic field measurements of the beamline elements were also incorporated.

LINE XC BEAMLINE

The Line XC, referred to as the pRad beamline, starting at the end of the Linac to pRad entry point (LCTV4), consists

05 Beam Dynamics and EM Fields

D01 Beam Optics - Lattices, Correction Schemes, Transport

of 15 quadrupoles, 15 bending magnets, 9 wire scanners for beam profile measurements, 6 gated CCDs for imaging, current monitors, vacuum system, and associate mechanical and electrical systems. The effective lengths of the each quadrupoles varying from 0.17 m to 0.77 m with bore radius from 0.025 m to 0.077 m. Magnetic fields in these magnets range from 0.08 kG to 4.46 kG field. Details of the Line XC is not addressed in this report.



Figure 1: Measurement of phase-space parameters at the end of 800 MeV linac.

TWISS PARAMETERS AND BEAM PROFILE

The Twiss parameters are defined in terms of the phasespace ellipse of a beam. Figure 1 shows measured emittance data at the end of 800 MeV linac. The first three lines in Table 1 show measurements of the Twiss parameters α , β , and RMS emittance (ε) for 800 MeV beam. These measurements were used to extract the input beam parameters (x, x', y, y') for the TRANSPORT code. The longitudinal beam parameters were also necessary for the simulation. The momentum spread ($\Delta p/p_0$) was calculated from the same measured emittance used for the transverse input, but also used previously measured moment spread and beam dispersion.

A well known relation between the Twiss parameters of an ellipse is [5]

$$\gamma = \frac{1 + \alpha^2}{\beta} \tag{1}$$

The maximum width of the beam envelope in the x-plane

$$x_{max} = \sqrt{\sigma_{11}} = \sqrt{\beta\varepsilon} \qquad (cm) \qquad (2)$$

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3323

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where, σ_{11} is an element of the beam matrix σ [4]. The publisher, square roots of the diagonal terms of the sigma matrix provide the beam size in each coordinate of the ellipsoid. Thus, the maximum angular divergence of the beam envelope in the x-plane work,

$$\theta_{max} = x' = \sqrt{\sigma_{22}} = \sqrt{\gamma \varepsilon}.$$
 (mrad) (3)

From Eqs. (2), and (3), we find, respectively,

$$\beta = \frac{\sigma_{11}}{\varepsilon} \tag{4}$$

$$\gamma = \frac{\sigma_{22}}{\varepsilon} \tag{5}$$

By using Eqs. (4) and (5) in Eq. (1), the dimensionless Twiss parameter, α , can be written as,

$$\alpha = \sqrt{\frac{\sigma_{11}\sigma_{22}}{\varepsilon^2} - 1} \tag{6}$$

maintain attribution to the author(s). title of the Therefore, Eqs. (6), (4) and (5) provide α , β , and γ ; once, σ_{11}, σ_{22} are known by execution of TRANSPORT. The must emittance, ε , fixed in TRANSPORT.

Additional input parameters such as: (1) longitudinal work beam extend, (2) momentum, and (3) the momentum spread of this are also required to execute TRANSPORT. These are calculated using the following methods.

Longitudinal Beam Extent (L)

distribution The longitudinal beam extent is related to the velocity factor, $\beta_{(E)}$, RF wavelength of the cavity (λ), phase width $rac{2}{r}(\Delta \varphi)$ and finally a factor (F) which approximate the effect of phase damping. The longitudinal beam extent is given by © 2018).

$$L = \beta_{(E)} \lambda \frac{\Delta \varphi}{360^{\circ}} \times F, \tag{7}$$

where $\Delta \varphi$ is the beam phase width in degrees. The wave-in length, $\lambda = c/f$, is 37.267 cm, for the RF frequency (f) of 805× 10^{6} Hz and usual value of velocity of light (c). The factor, F, a ratio of an initial phase width $(\Delta \phi_1)$ to the width at some З

$$F = \frac{\Delta\phi_2}{\Delta\phi_1} = \left(\frac{\beta_1\gamma_1}{\beta_2\gamma_2}\right)^{3/4} = \left(\frac{\beta_{(121)}\gamma_{(121)}}{\beta_{(800)}\gamma_{(800)}}\right)^{3/4}$$
(8)

F = $\frac{\Delta\phi_2}{\Delta\phi_1} = \left(\frac{\beta_1\gamma_1}{\beta_2\gamma_2}\right)^{3/5} = \left(\frac{r_{\chi}}{\beta_{(800)}\gamma_{(800)}}\right)^{3/5}$ where, $\beta_{(121)}$ is the relativistic velocity factor, and $\gamma_{(121)}$ is the energy factor at 121 MeV; and $\beta_{(800)}$ is a relativistic $\Gamma_{(121)}$ and $\gamma_{(800)}$ is an energy factor at a higher $\Gamma_{(121)}$ is the relativistic velocity factor at a higher

$$\beta_{(E)} = \frac{\sqrt{(\gamma_{(E)})^2 - 1}}{\gamma_{(E)}}$$
(9)

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$$\gamma_{(E)} = 1 + \frac{T}{E_0} \tag{10}$$

where, T is the beam energy (in MeV), and $E_0=938.3$ MeV (rest energy of a proton). Using these equations to estimate the phase-damping at 800 MeV gives F=0.441.

Content THPAK047



05 Beam Dynamics and EM Fields



Figure 2: Measurement of RF phase at 121 MeV.

Figure 2 shows a phase scan data at 121 MeV. For a phase width, $\Delta \varphi = 25^{\circ}$, the estimated beam extent at 800 MeV is

$$L = \beta_{(121)} \lambda \frac{\Delta \varphi}{360^{\circ}} \times F \sim 0.52 \ cm \tag{11}$$

Momentum (p_0) *in GeV/c*

The beam momentum, (p_0) , of a 800 MeV beam is given by

$$p_0 = \beta_{(800)} \gamma_{(800)} \frac{E_0}{c} = 1.463 \; GeV/c \tag{12}$$

Momentum Spread The spread in the beam momentum is defined by

$$\frac{\Delta p}{p_0} = \frac{\sqrt{(R_x)^2 - \beta_x (4\epsilon_{x-rms})}}{\eta}$$
(13)

where, R_x is the 2RMS horizontal beam size (cm) at a location of wire scanner LDWS3X; β_x is the horizontal betafunction (cm/mrad) at the LDWS3X; ϵ_{x-rms} is the unnormalized horizontal rms beam emittance (π -mm-mrad), and η is the dispersion function at the LDWS3X (cm/%). If $R_x=0.5793$ cm, $\beta_x=1.11236$ cm/mrad, $\epsilon_{x-rms}=0.04 \pi$ -cmmrad, and η =4.8798 cm/%, the beam momentum spread is

$$\frac{\Delta p}{p_0} = \frac{\sqrt{(0.58)^2 - 1.112 \times 4 \times 0.04}}{4.88} = 0.0816\% \quad (14)$$

TRANSPORT AND MEASUREMENTS

Table 1 summarizes the necessary TRANSPORT input beam phase-space parameters obtained by emittance measurements at the end of the linac and as calculated in the previous section. Updated measurements of drift spaces, magnet fields and diagnostics locations were also used.

Figure 3 shows calculated beam envelopes using TRANS-PORT. The beam size at the pRad entrance is $\simeq 2$ mm radius (2RMS). A few examples of beam profile measurements are shown in Fig. 4. Figure 5 shows measured beam profiles at diagnostics locations (black dots in solid line) and the predicted envelope (hollow circles in dotted line) using

α -0.656 -1.014 β 1.814 $\frac{cm}{mrad}$ 2.087 $\frac{cm}{mrad}$ ε 0.040 cm(mrad) 0.04 cm(mrad) $4 \times \varepsilon$ 0.16 cm(mrad) 0.16 cm(mrad) γ (Eq.1) 0.788 $\frac{mrad}{cm}$ 0.972 $\frac{mrad}{cm}$ x_{max} (Eq. 2) 0.538 cm 0.577 cm x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	Items	X vs XP	Y vs Yp
β 1.814 $\frac{cm}{mrad}$ 2.087 $\frac{cm}{mrad}$ ε 0.040 cm(mrad) 0.04 cm(mrad) 4×ε 0.16 cm(mrad) 0.16 cm(mrad) γ (Eq.1) 0.788 $\frac{mrad}{cm}$ 0.972 $\frac{mrad}{cm}$ x_{max} (Eq. 2) 0.538 cm 0.577 cm x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	α	-0.656	-1.014
ε 0.040 cm(mrad) 0.04 cm(mrad) $4 \times \varepsilon$ 0.16 cm(mrad) 0.16 cm(mrad) γ (Eq.1) 0.788 $\frac{mrad}{cm}$ 0.972 $\frac{mrad}{cm}$ x_{max} (Eq. 2) 0.538 cm 0.577 cm x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	β	1.814 $\frac{\text{cm}}{\text{mrad}}$	2.087 $\frac{\text{cm}}{\text{mrad}}$
$4 \times \varepsilon$ 0.16 cm(mrad) 0.16 cm(mrad) γ (Eq.1) 0.788 $\frac{\text{mrad}}{\text{cm}}$ 0.972 $\frac{\text{mrad}}{\text{cm}}$ x_{max} (Eq. 2) 0.538 cm 0.577 cm x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	ε	$0.040 \mathrm{cm}(\mathrm{mrad})$	0.04 cm(mrad)
$\begin{array}{cccc} \gamma \ (\text{Eq.1}) & 0.788 \frac{\text{mrad}}{\text{cm}} & 0.972 \frac{\text{mrad}}{\text{cm}} \\ x_{max} \ (\text{Eq. 2}) & 0.538 \ \text{cm} \\ y_{max} \ (\text{Eq. 2}) & 0.577 \ \text{cm} \\ x'_{max} \ (\text{Eq.3}) & 0.355 \ \text{mrad} \\ y'_{max} \ (\text{Eq.3}) & 0.304 \ \text{mrad} \\ \end{array}$	$4 \times \varepsilon$	0.16 cm(mrad)	0.16 cm(mrad)
x_{max} (Eq. 2) 0.538 cm y_{max} (Eq. 2) 0.577 cm x'_{max} (Eq.3) 0.355 mrad y'_{max} (Eq.3) 0.304 mrad	γ (Eq.1)	$0.788 \frac{\text{mrad}}{\text{cm}}$	$0.972 \frac{\text{mrad}}{\text{cm}}$
y_{max} (Eq. 2) 0.577 cm x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	<i>x_{max}</i> (Eq. 2)	0.538 cm	
x'_{max} (Eq.3) 0.355 mrad 0.304 mrad	y _{max} (Eq. 2)		0.577 cm
v' (Eq. 2) 0.304 mrsd	x'_{max} (Eq.3)	0.355 mrad	
y_{max} (Eq.3) 0.594 III au	y'_{max} (Eq.3)		0.394 mrad

Table 1: TRANSPORT Input Parameters at 800 MeV

TRANSPORT. The top and bottom graphs represent horizontal and vertical profiles along the pRad beamline. Variations of up to 30% were observed between simulation and measurements. We used many legacy diagnostics and accurate resolution of each of the diagnostics were unknown. In addition, there might be some analysis error due to low-level signal. Therefore, variation between measurements and predictions at the beginning or at the end of the beamline stands for uncertainty of measurements.



Figure 3: TRANSPORT calculated beam envelope.

CONCLUSION

The beam emittance measured at the end of the 800 MeVlinac was used as a part of the required input data for TRANS-PORT. The beam profile was measured at various locations using wire scanners and gated cameras. Measured data and TRANSPORT predictions were directly compared and found in reasonable agreement. These results will be used to improve our tuning of the pRad beamline.

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05 Beam Dynamics and EM Fields

D01 Beam Optics - Lattices, Correction Schemes, Transport



Figure 4: The beam profile at the end of linac a) horizontal and b) vertical, measured using a wire scanner; and (c) the beam profile at the end of the transport section using a gated CCD (LCTV4).



Figure 5: Measured (black dots in solid line) and calculated (hollow circles in dotted line) profiles along the beamline. (a) A horizontal profile and (b) a vertical profile.

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