

# Self-Consistent Injection Painting for Space Charge Mitigation

HB 2023

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# Outline

- Danilov Distribution
- Space Charge Mitigation
- Painting Requirements
- The Spallation Neutron Source
- Experiments to date

# {2,2}-Danilov\* Distribution is Self-Consistent

1. Uniform real space distribution (linear space charge)
2. Elliptical envelope
3. Maintains (1),(2) under any linear transport (including space charge)

A uniformly filled circular mode is a Danilov distribution. By (3) we can match this to any linear optics and maintain a Danilov distribution.

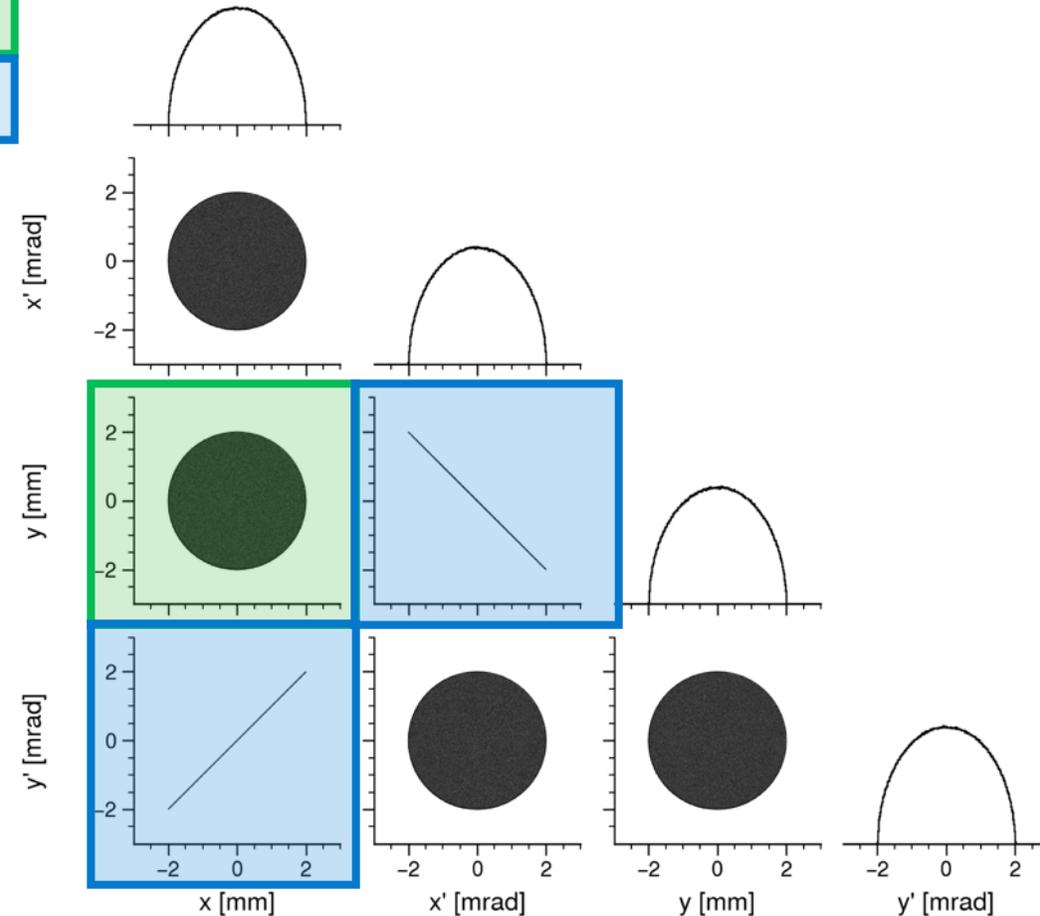
\* We call the {2,2} *the* Danilov distribution

PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS, VOLUME 6, 094202 (2003)

**Self-consistent time dependent two dimensional and three dimensional space charge distributions with linear force**

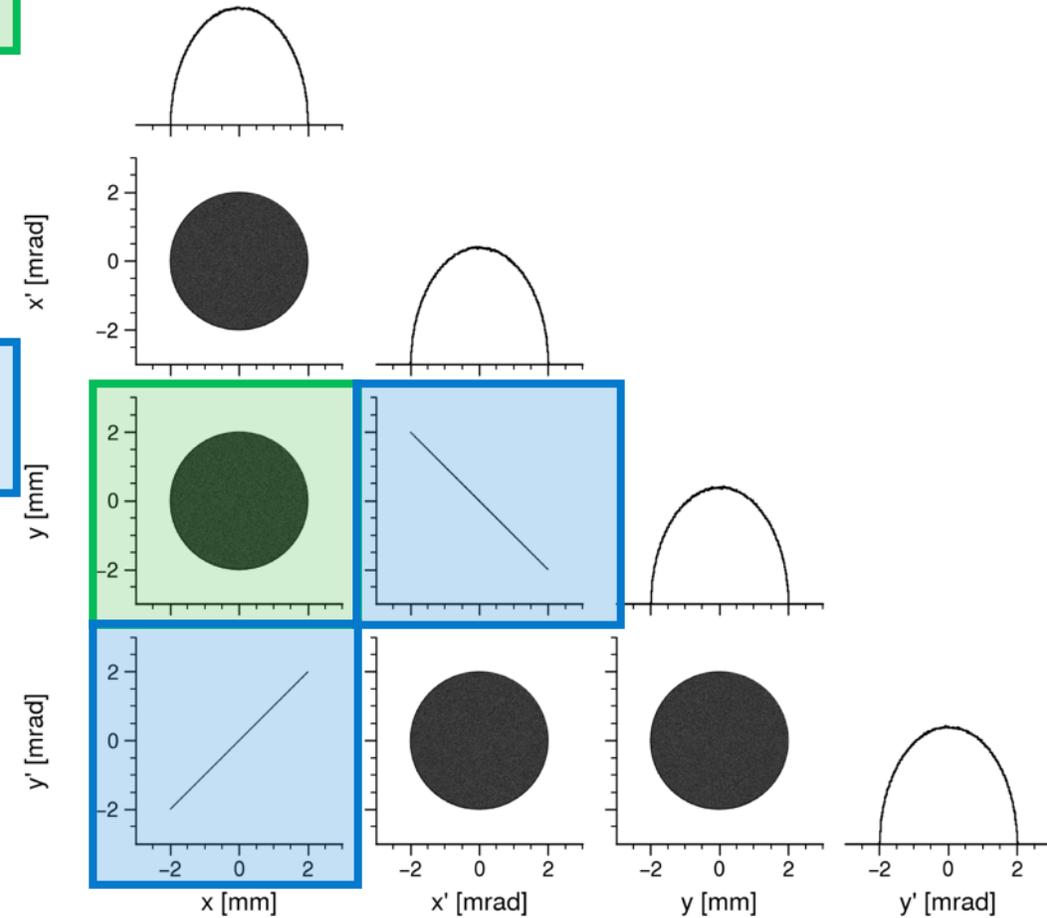
V. Danilov, S. Cousineau, S. Henderson, and J. Holmes

{2,2} Danilov Distribution



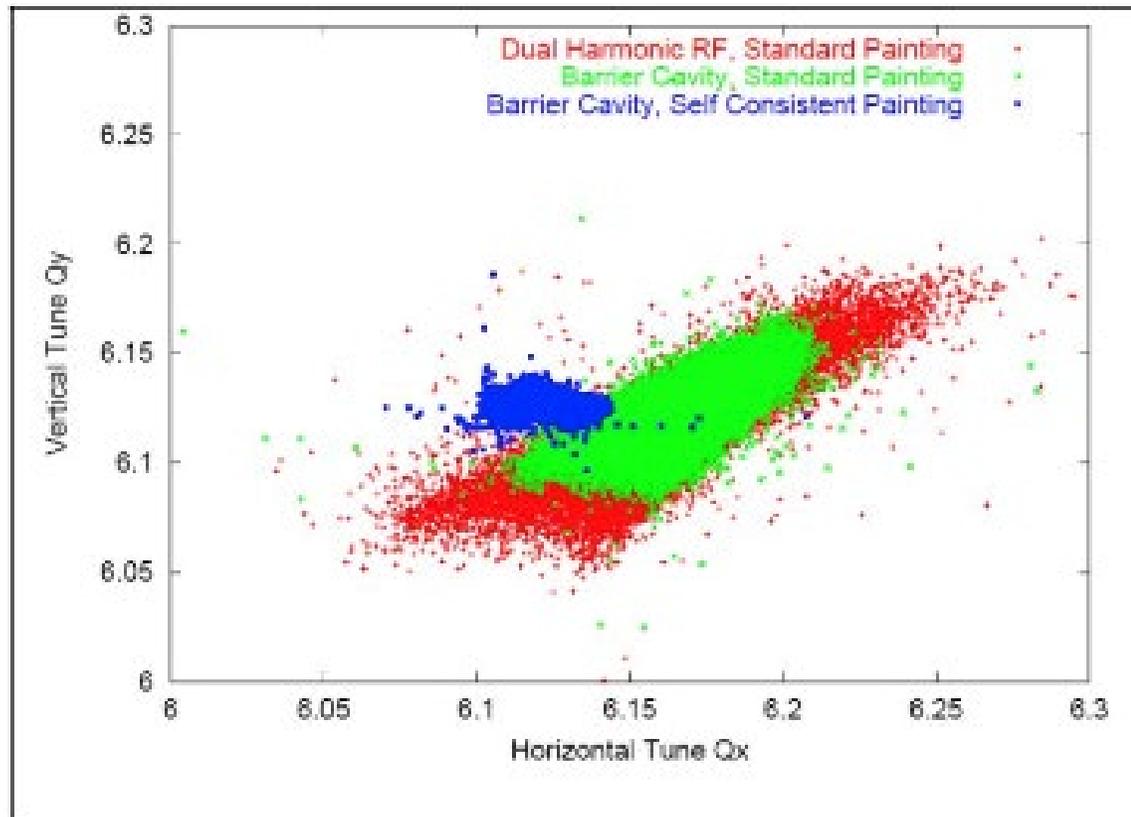
# Danilov Distribution Key Features

- Uniform space charge implies reduced tune shift, and minimal spread
- When matched to a coupled ring elliptical envelope means distribution is uniform over a mode – (could use equal tunes, but then modes are degenerate)
- eigenmode implies vanishing 4D emittance
- ***Invariant proportional to real space radius meaning we can add more beam at the edges, painting beam while maintaining self-consistency*** – this is a scalable procedure



# Space Charge Mitigation

- Footprint is much smaller than standard SNS tune footprint
- Low 4D emittance implies brighter with same physical size (many benefits of circular modes apply) (Burov et al. PR.E 2002, Burov PRAB 2013 )



Relevant blobs are blue and green – same RF, different painting

Blue footprint covers ~30% of tune space occupied by green

THAW03

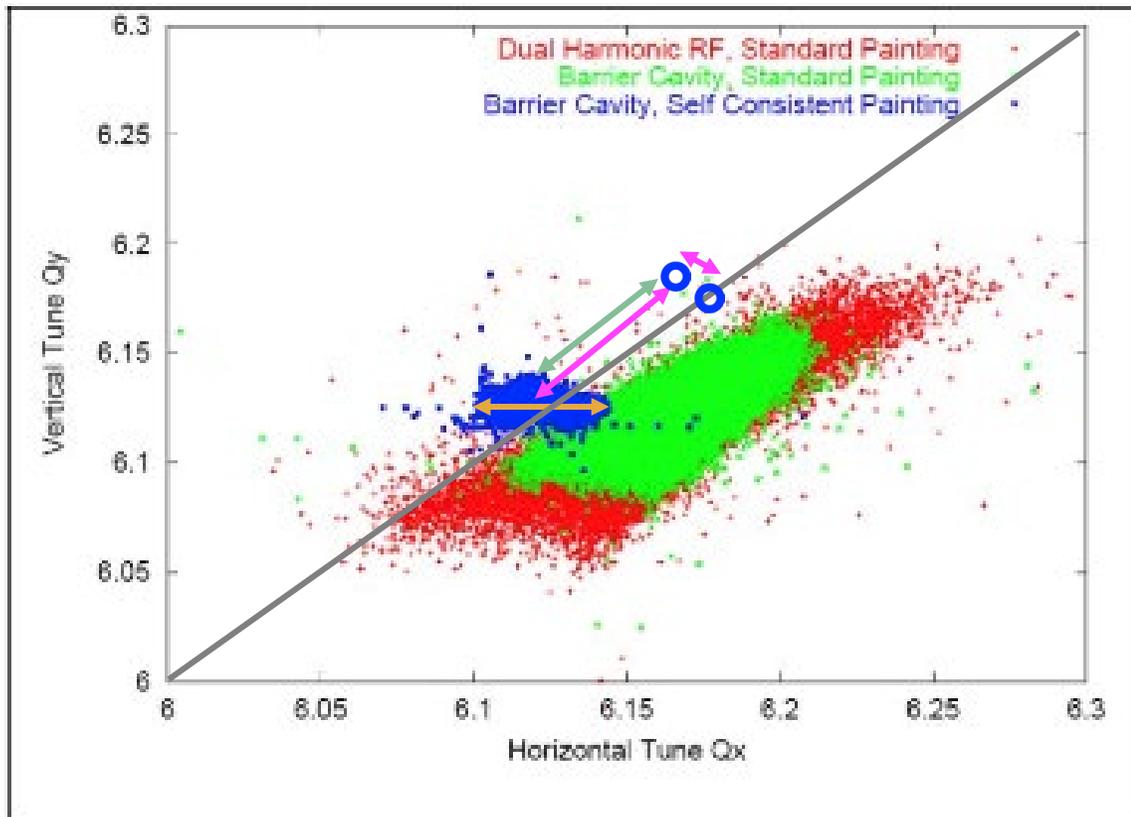
Proceedings of HB2006, Tsukuba, Japan

RF BARRIER CAVITY OPTION FOR THE SNS RING BEAM POWER UPGRADE

J.A. Holmes, S.M. Cousineau, V.V. Danilov, and A.P. Shishlo, SNS, ORNL, Oak Ridge, TN 37830, USA

# Space Charge Mitigation

- Decoupling tune shift and spread opens possibility for intense space charge



This tune shift is partly due to solenoid breaking degeneracy, need to isolate space charge tune shift.

- Bare lattice tunes Self-consistent
- ↔ Tune Spread
- ↔ Tune Shift
- Sparse tail

THAW03

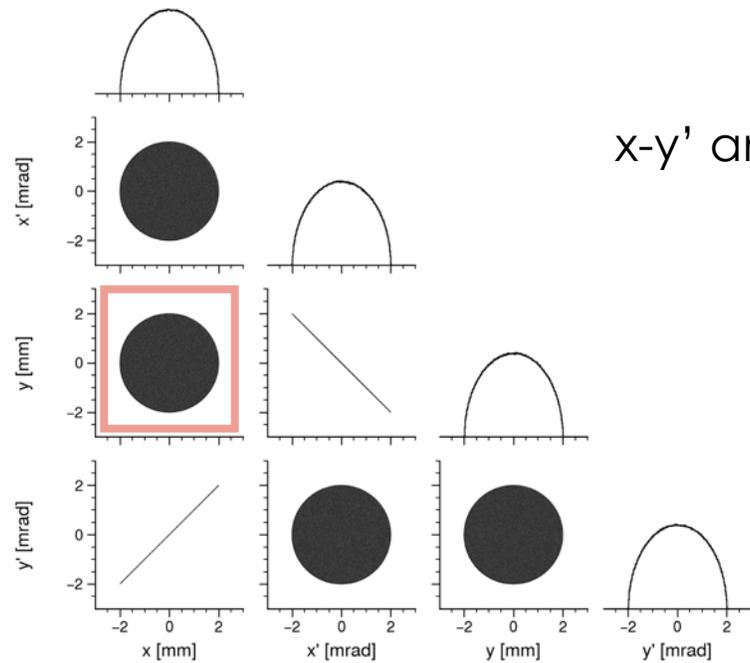
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RF BARRIER CAVITY OPTION FOR THE SNS RING BEAM POWER UPGRADE

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# SNS Project Goals

- Proof-of-principle painting of a uniformly filled, elliptical bunch in the SNS ring (approx. {2,2}-Danilov distribution, *the Danilov distribution*)
- Study evolution of the Danilov dist. during painting and storage

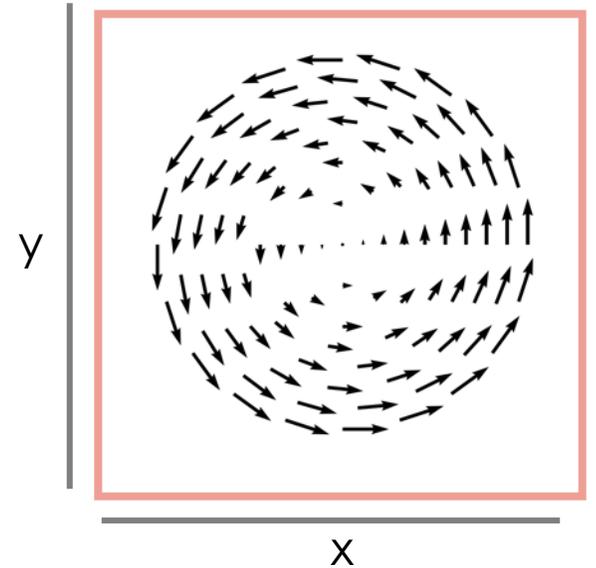


$x-y'$  and  $y-x'$  correlations give a rotating beam



This is a uniformly filled circular mode

Arrows indicate  $x', y'$



# Painting Requirements\*

Low 4D emittance

1. Small injected emittance relative to larger of final emittances
  - Initial emittance (size of the paintbrush) defines the achievable 'emittance ratio'
2. Non-planar modes
  - either through equal tunes or lattice coupling
  - Correlated closed orbit paths in x and y planes in time
3. Amplitude of injection should increase as  $\sqrt{t}$  along well-defined path in 4D phase space

Uniformity

Detailed feasibility study:

PHYSICAL REVIEW ACCELERATORS AND BEAMS **21**, 124403 (2018)

## Injection of a self-consistent beam with linear space charge force into a ring

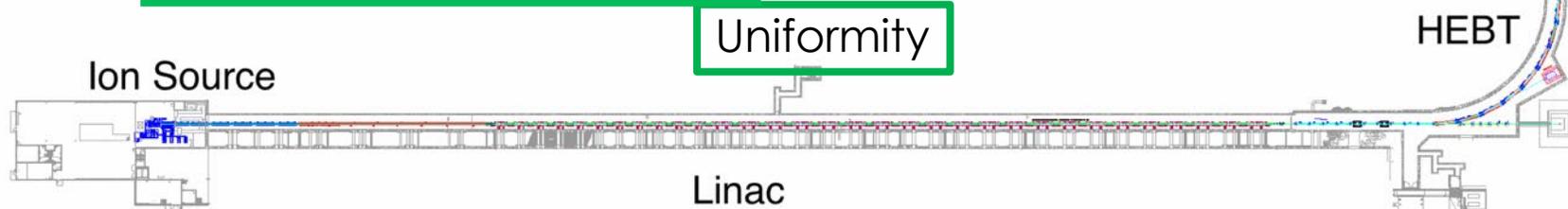
J. A. Holmes, T. Gorlov, N. J. Evans, M. Plum, and S. Cousineau  
*Oak Ridge National Laboratory, One Bethel Valley Road, Oak Ridge, Tennessee 37831, USA*

 (Received 15 May 2018; published 17 December 2018)

\*Painting into one plane in the 'flat' portion of a round-to-flat transformer (Derbenev, 1993), then transforming to round would eliminate 2,3. Would it work as well, better?

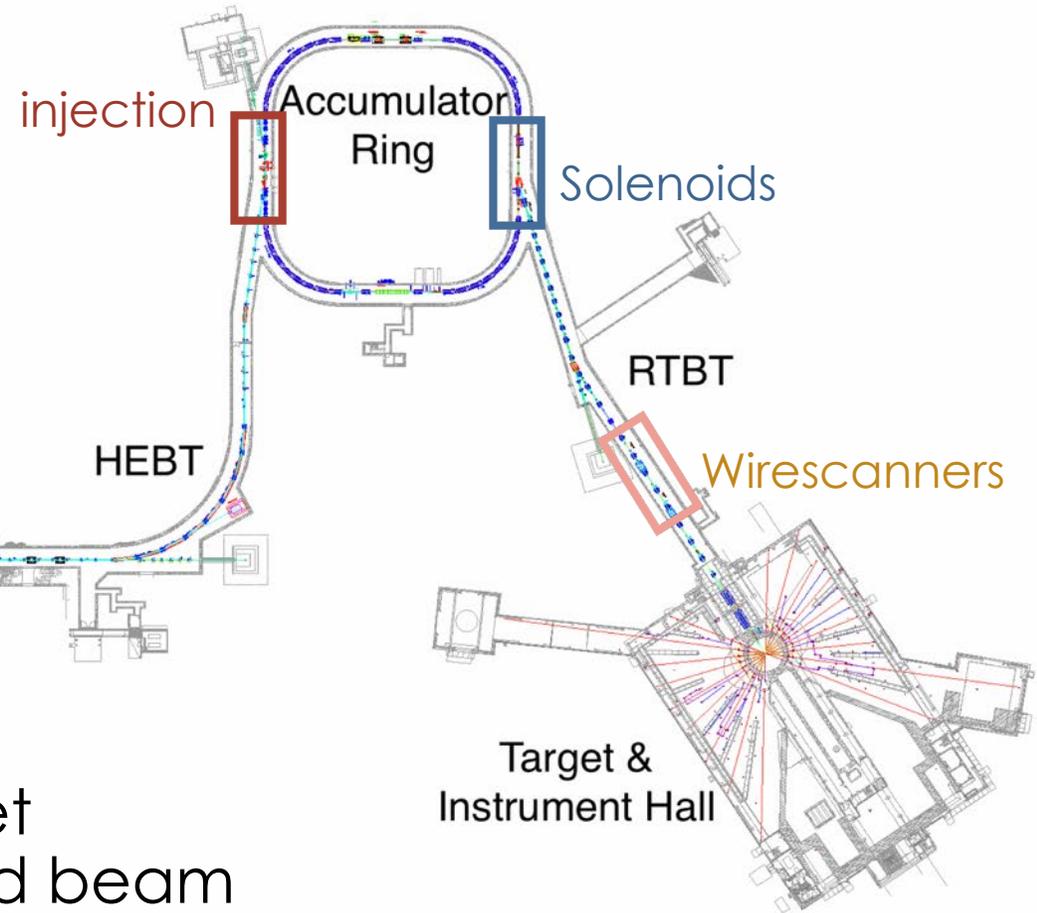
# The Spallation Neutron Source

- 1 GeV H- linac
  - Norm RMS emit = 0.46 mm · mrad (design)
- 1 GeV, C=248m Ring (~1 us)
  - 2 Solenoids, 1.2m each, 0.6 T-m total
  - 1.5E14 ppp at 1.4 MW
  - Norm RMS Emittance = 44 mm · mrad (design)
  - Trans. Acceptance = 480 mm · mrad
  - Flexible painting system



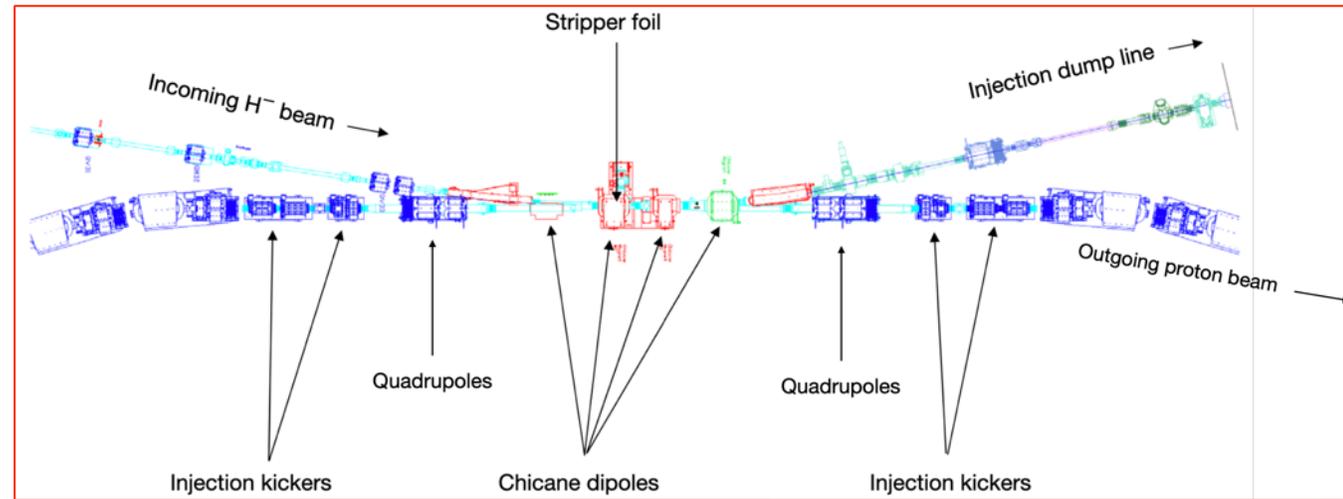
- Ring-Target Beam Transport (RTBT)
  - 5 wire scanners, BPMs, BLMs, Harp, Target Imaging System for inspecting extracted beam

Operational Parameters give:  
Space charge tune shift: 0.15  
Uniform beam tune shift: 0.1



# SNS Painting System

- 4 time varying magnets in each plane to create closed bumps with offset at foil
- Time varying position and angle of ring closed orbit at injection point



	Max Kick*	
	1 GeV	800 MeV
H/V kickers 1&4	15.4 mrad	17.8 mrad
H/V kickers 2&3	8.5 mrad	9.9 mrad

\*Numbers after kicker upgrade – original simulations done at 600 MeV with old kicker limits, identical to current 800 MeV operation

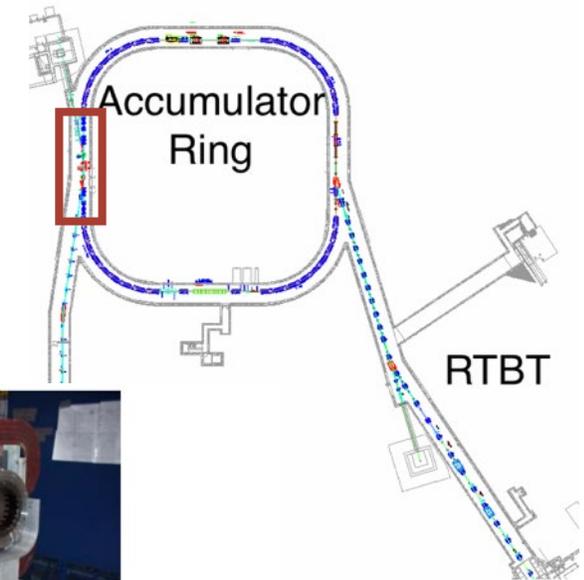


Figure 8: Long Injection dynamic bump magnets with Beam Pipe and Bellow.

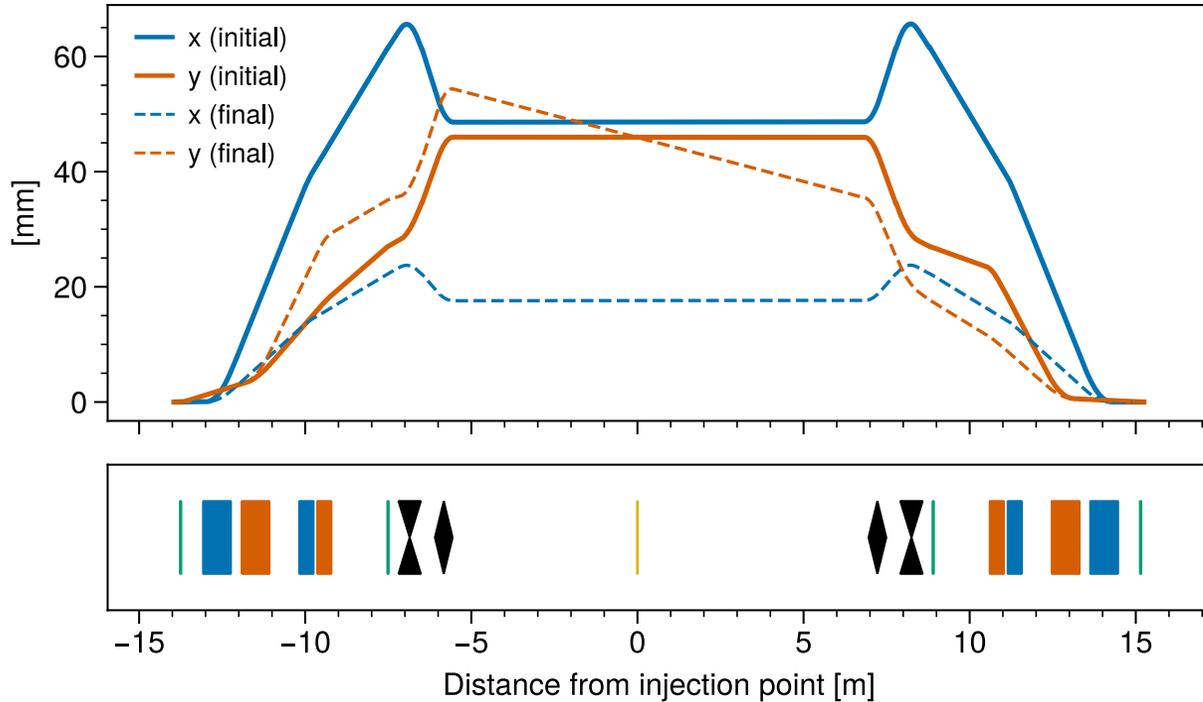
Raparia, 2005

Evans - HB 2023

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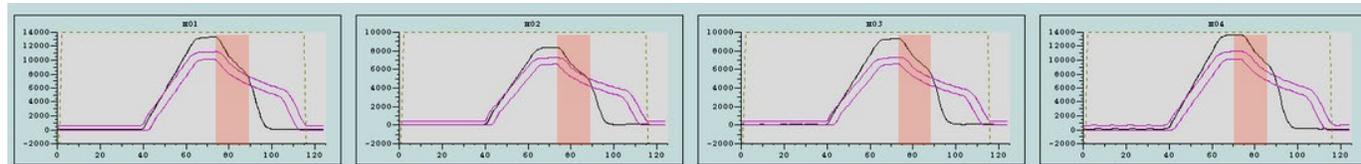
# Painting Trajectory

Fixed chicane bump not shown



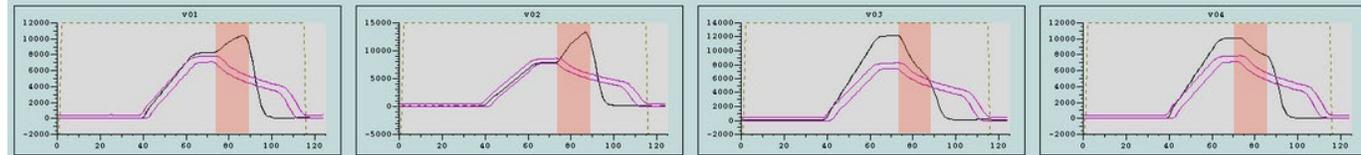
- Pure x bump
  - all kickers decrease with time
  - injecting on closed orbit is only kicker limitation
- Pure y' bump
  - some kickers kick more some less than position bump
- We can ease kicker limitations by:
  - biasing the closed orbit with correctors
  - has to be determined on-line
  - Reducing beam energy – 800 MeV is lower limit because of timing system\*

Horizontal Kickers



— Experiment WF  
— Production WF

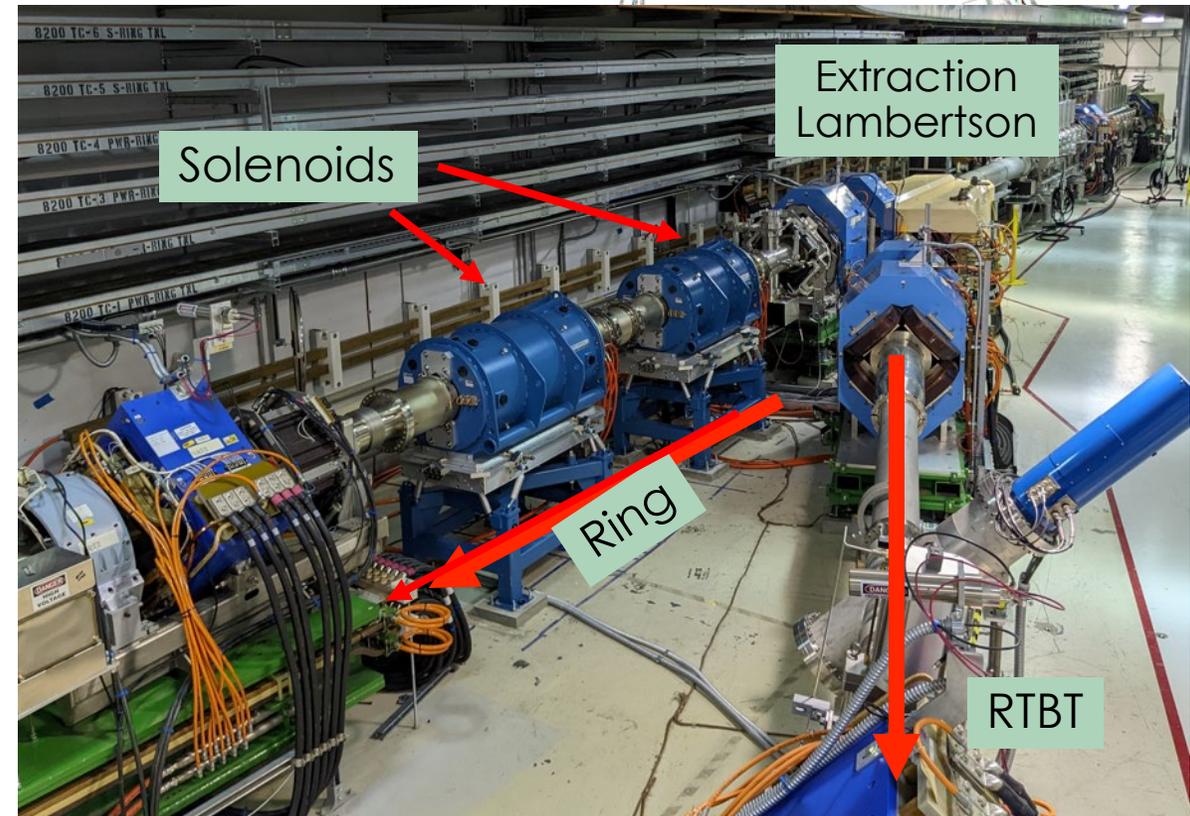
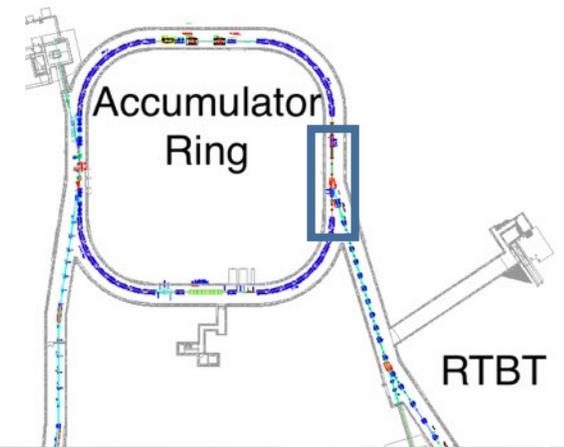
Vertical Kickers



\*we've gone to 600 MeV, but it's very tough, not necessary

# SNS Solenoids

- Solenoids were designed and built by Stangenes Industries
- Installed late Nov. 2022
- Solenoids ( $0.6 \text{ T} \cdot \text{m}$ , peak  $B_{||} = 0.26 \text{ T}$ ) split equal tunes



# RTBT Diagnostics

Four RTBT wire scanners allow measurement of 4D emittance (requires slight mod of RTBT optics to avoid poorly conditioned matrix\*)

\* Nuclear Inst. and Methods in Physics Research, A 1041 (2022) 167376

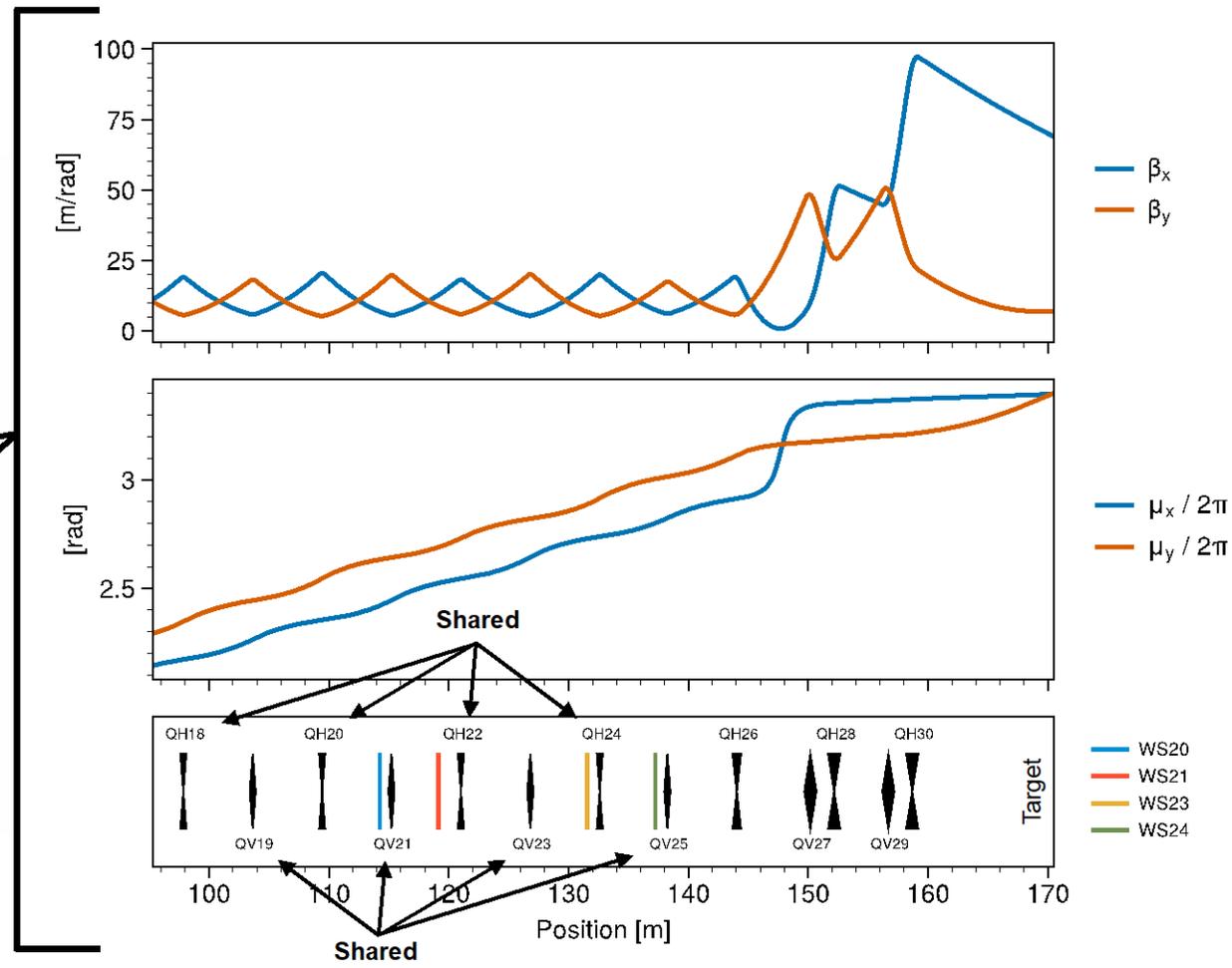
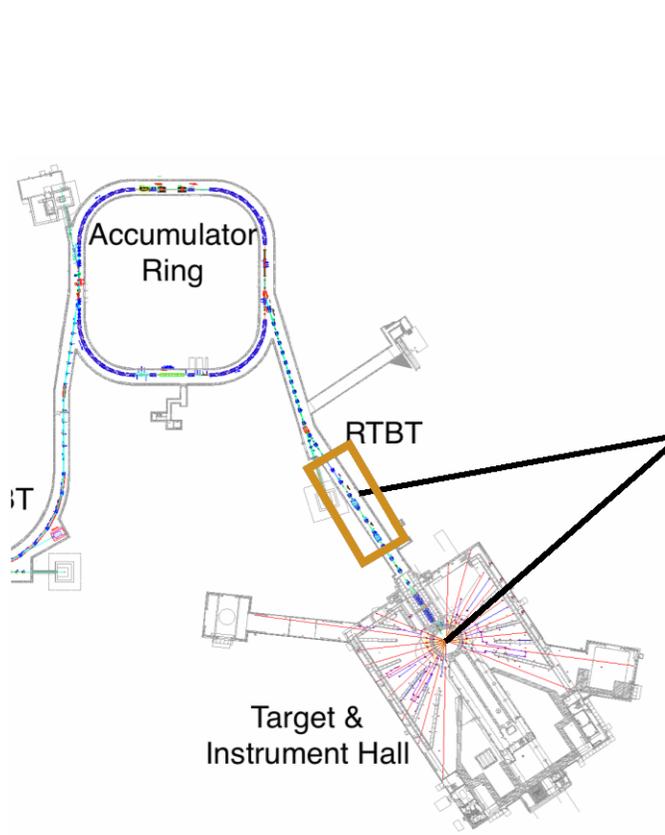
Contents lists available at ScienceDirect

**Nuclear Inst. and Methods in Physics Research, A**

journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)

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Four-dimensional emittance measurement at the Spallation Neutron Source  
 A. Hoover\*, N.J. Evans  
 Oak Ridge National Laboratory, One Bethel Valley Road, Oak Ridge, TN, 37831, USA

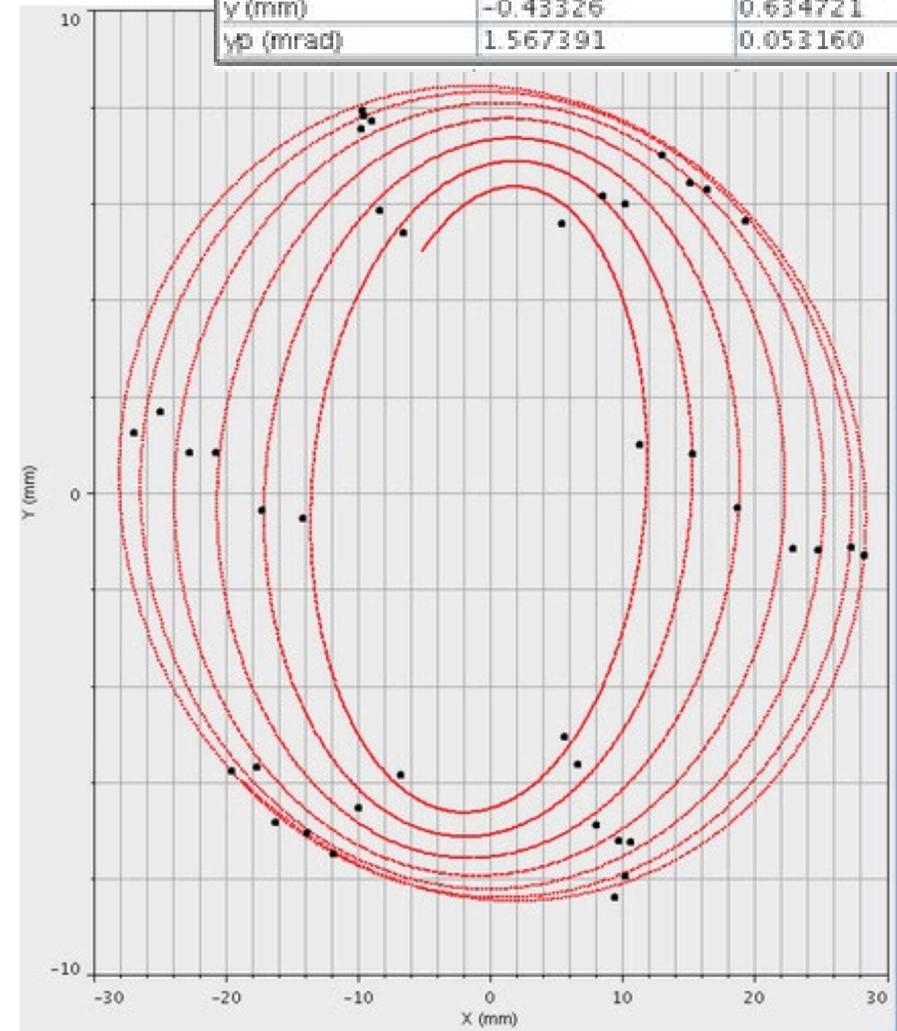


X

# Procedure for Eigenpainting

1. Setup ring with equal tunes ( $\sim 6.177$ )
2. Inject single pulse off closed orbit
3. TBT BPM data to + linear model to establish injection parameters ( $x, x', y, y'$ )
4. Find kicker settings to inject on closed orbit these are  $t_0$  kicker settings
5. Energize solenoids to split tunes
6. Fit coupled tunes
7. Inject on eigenvector coordinates\*:
  1.  $A\mathbf{v} = A^*(v_x, v_{x'}, v_y, v_{y'})$  these are  $t=t_{\max}$  kickers
8. Draw waveforms –  $\mathbf{v} * A * \text{Sqrt}(t_0/t_{\max})$
9. Paint

Measured phase space parameters at the foil		
	average	sigma
x (mm)	26.62396	0.819318
xp (mrad)	0.096851	0.136217
y (mm)	-0.43326	0.634721
yp (mrad)	1.567391	0.053160

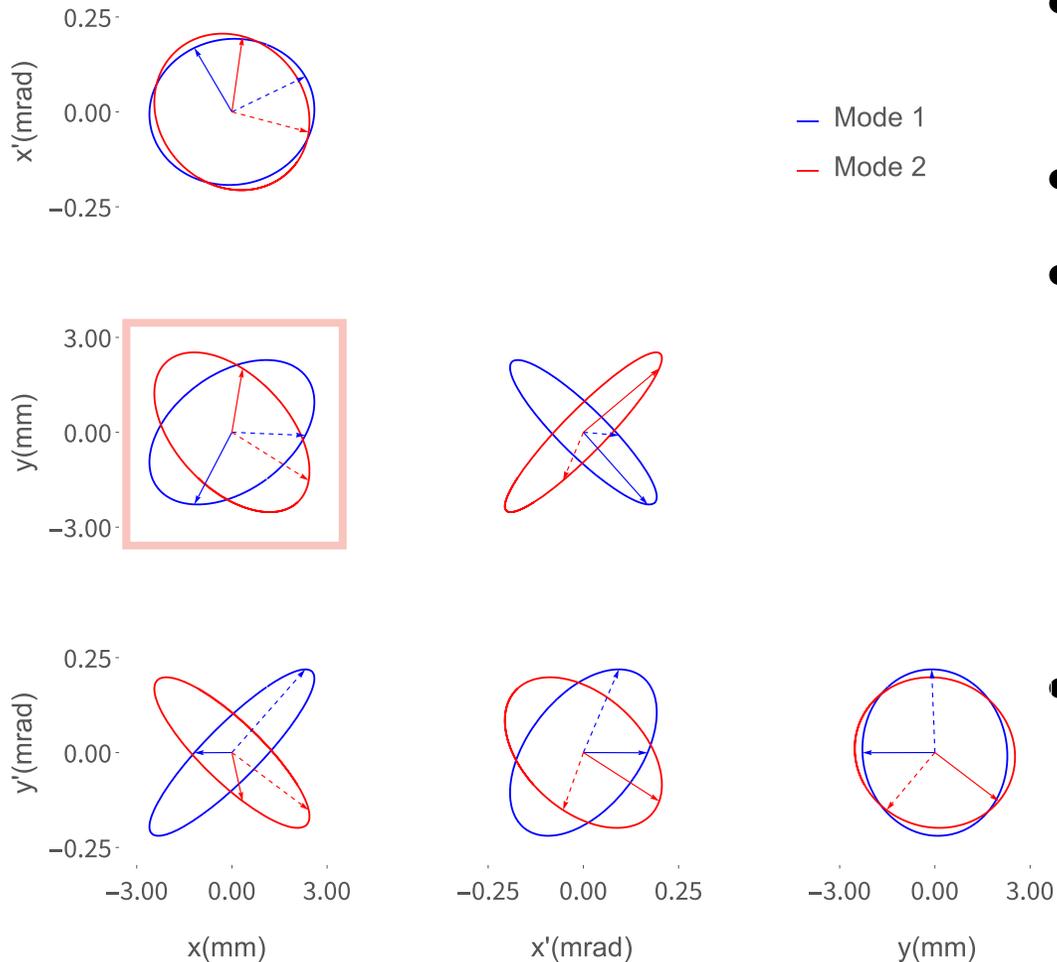


Turn-by-turn BPM data for a single pulse injected with final kicker settings

Online model doesn't have solenoids – we can turn them off for

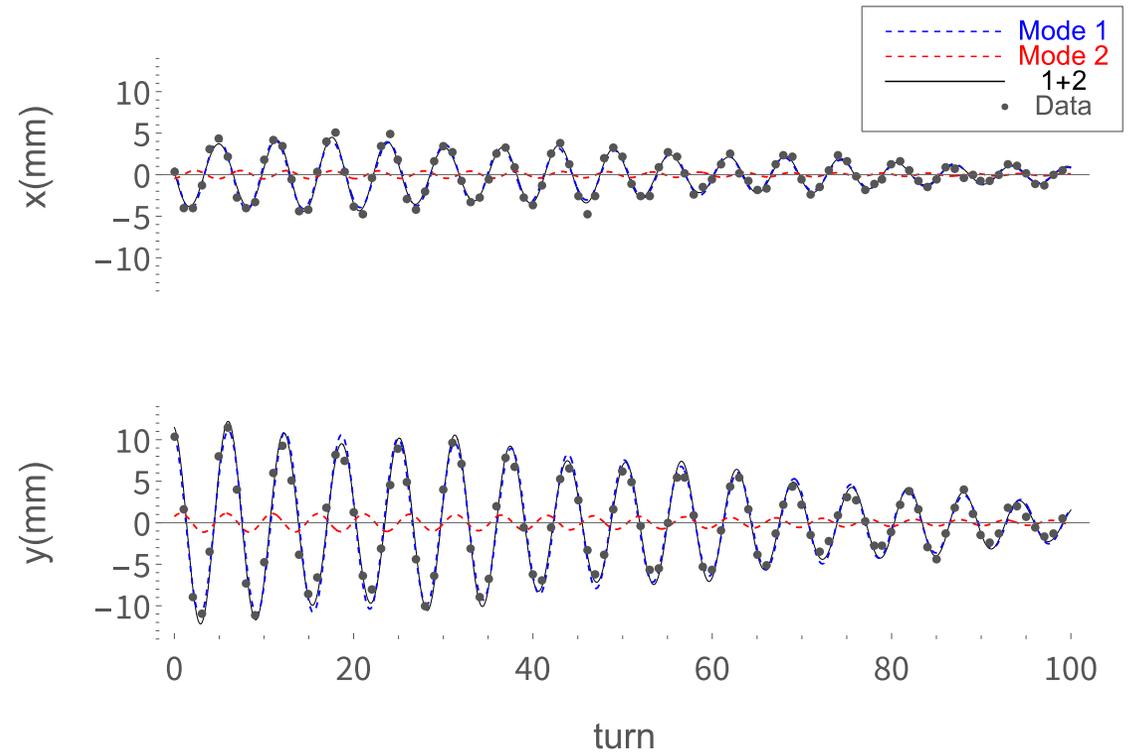
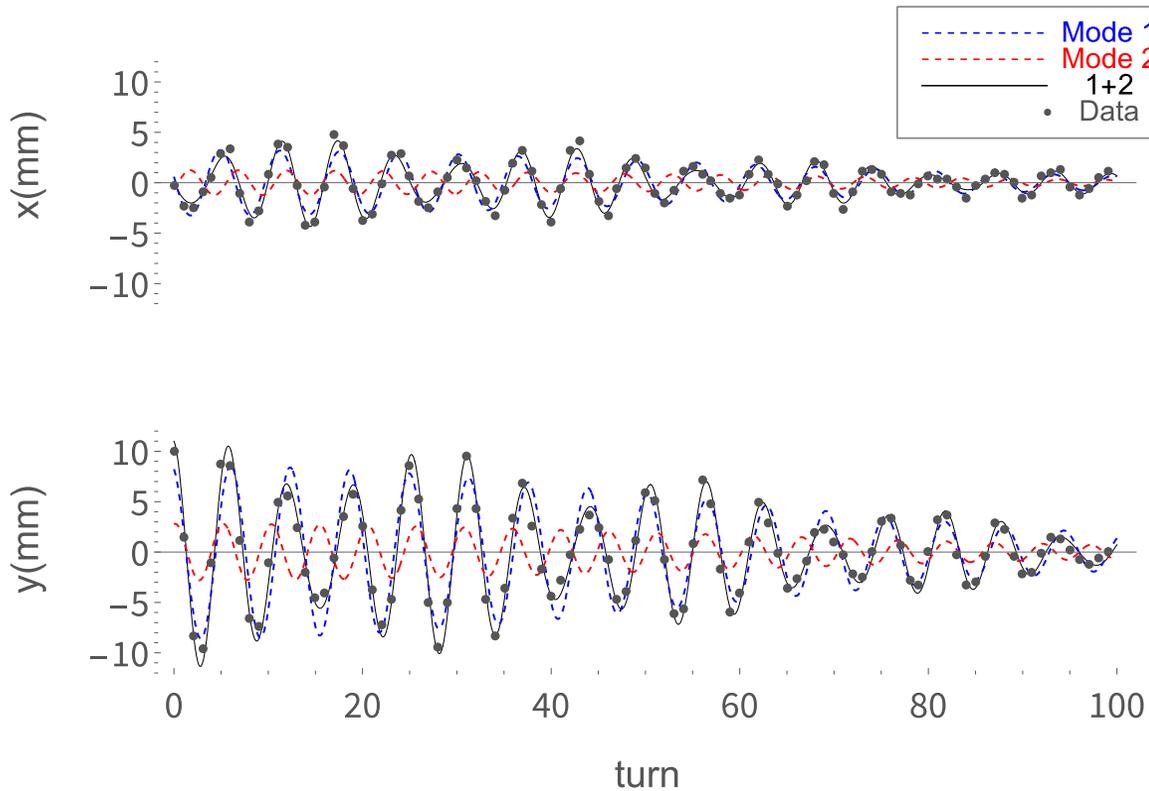
# Modes with Solenoids

Modes at Injection Location



- Equal tunes  $\nu_x = \nu_y = 6.1754$
- Solenoids on at full power for tunes of  $\nu_1=6.1584$ ,  $\nu_2=6.1956$
- Tune split 0.0372
- Tunes calibrated to measured TBT data using two free parameters:
  - solenoid strength
  - equal tune value used to match observed tunes
- We will inject on dashed blue line

# TBT data fit with calibrated model



Parameter	Arbitrary Inj.	Single Mode
$A_1(\sqrt{mm \cdot mrad})$	$3.22 \pm 0.010$	$4.19 \pm 0.012$
$\theta_1$	$0.150 \pm 0.0005$	$0.148 \pm 0.0004$
$A_2(\sqrt{mm \cdot mrad})$	$1.16 \pm 0.010$	$0.46 \pm 0.012$
$\theta_2$	$0.432 \pm 0.001$	$0.320 \pm 0.004$
$\frac{\epsilon_1}{\epsilon_2} = \left(\frac{A_1}{A_2}\right)^2$	$7.71 \pm 0.14$	$80.37 \pm 4.00$

Single turn injection off-axis  
Performance here defines  
upper limit on painting

# Measurement without Solenoids

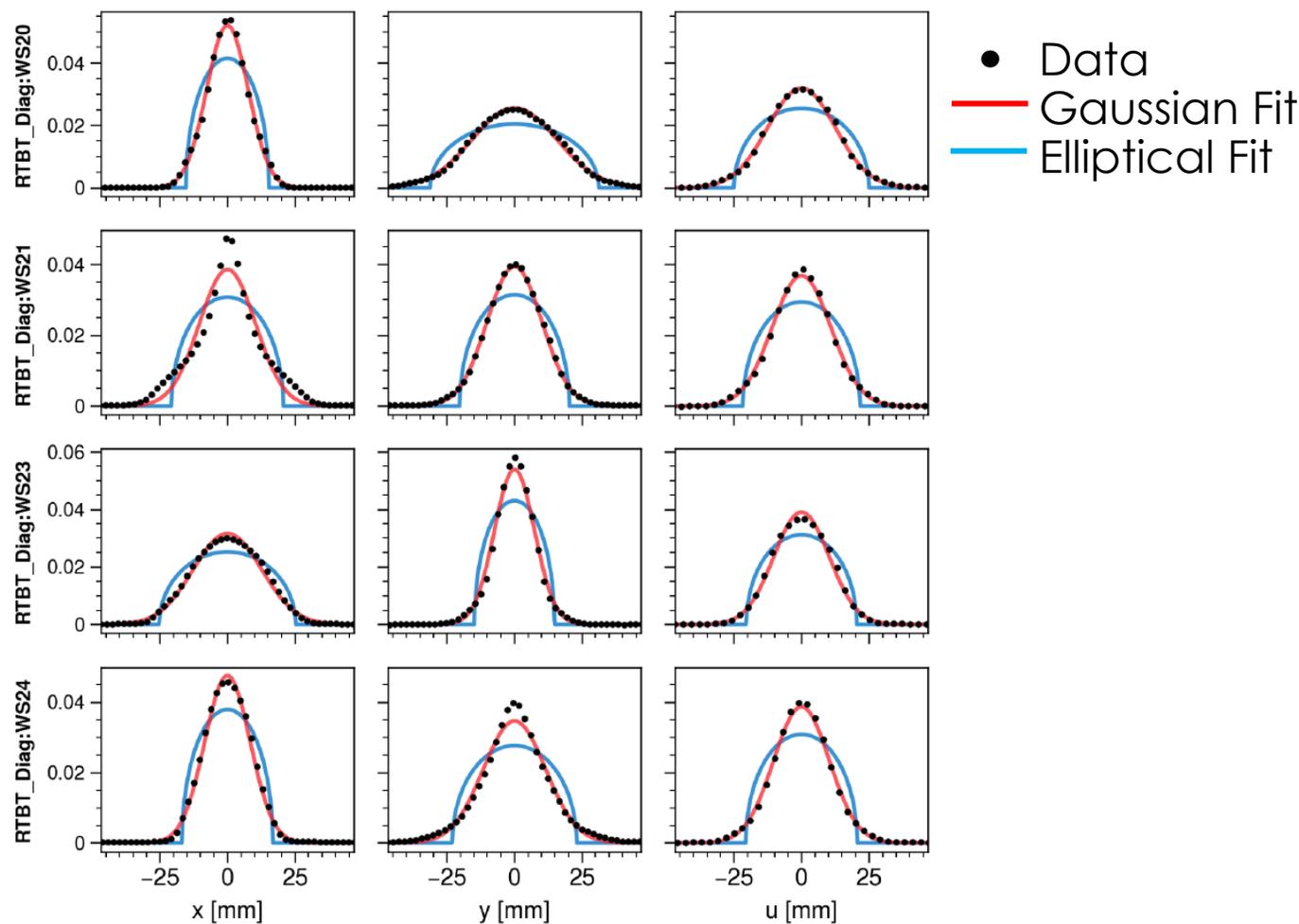
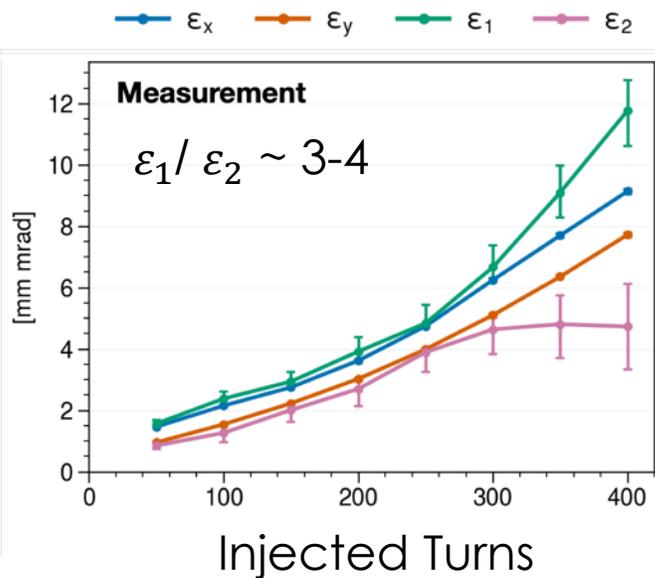
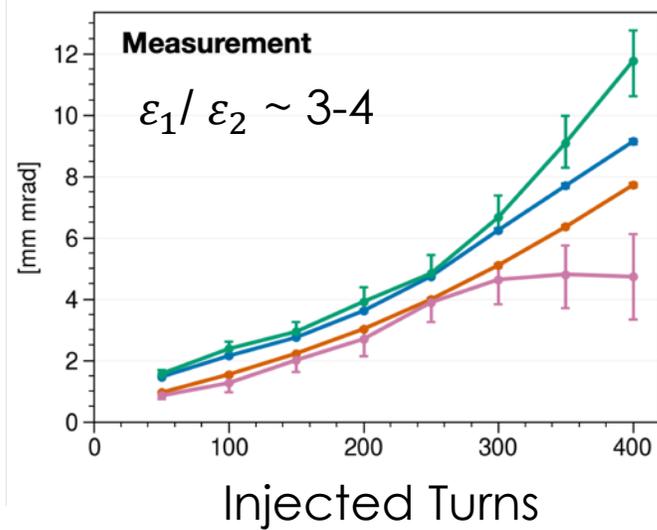
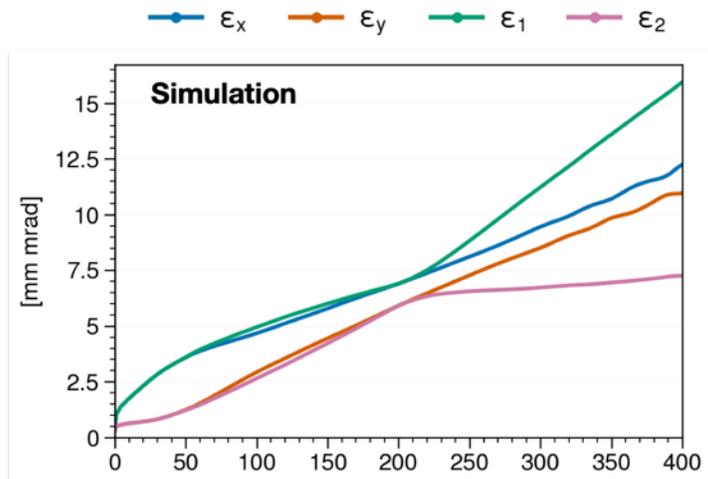


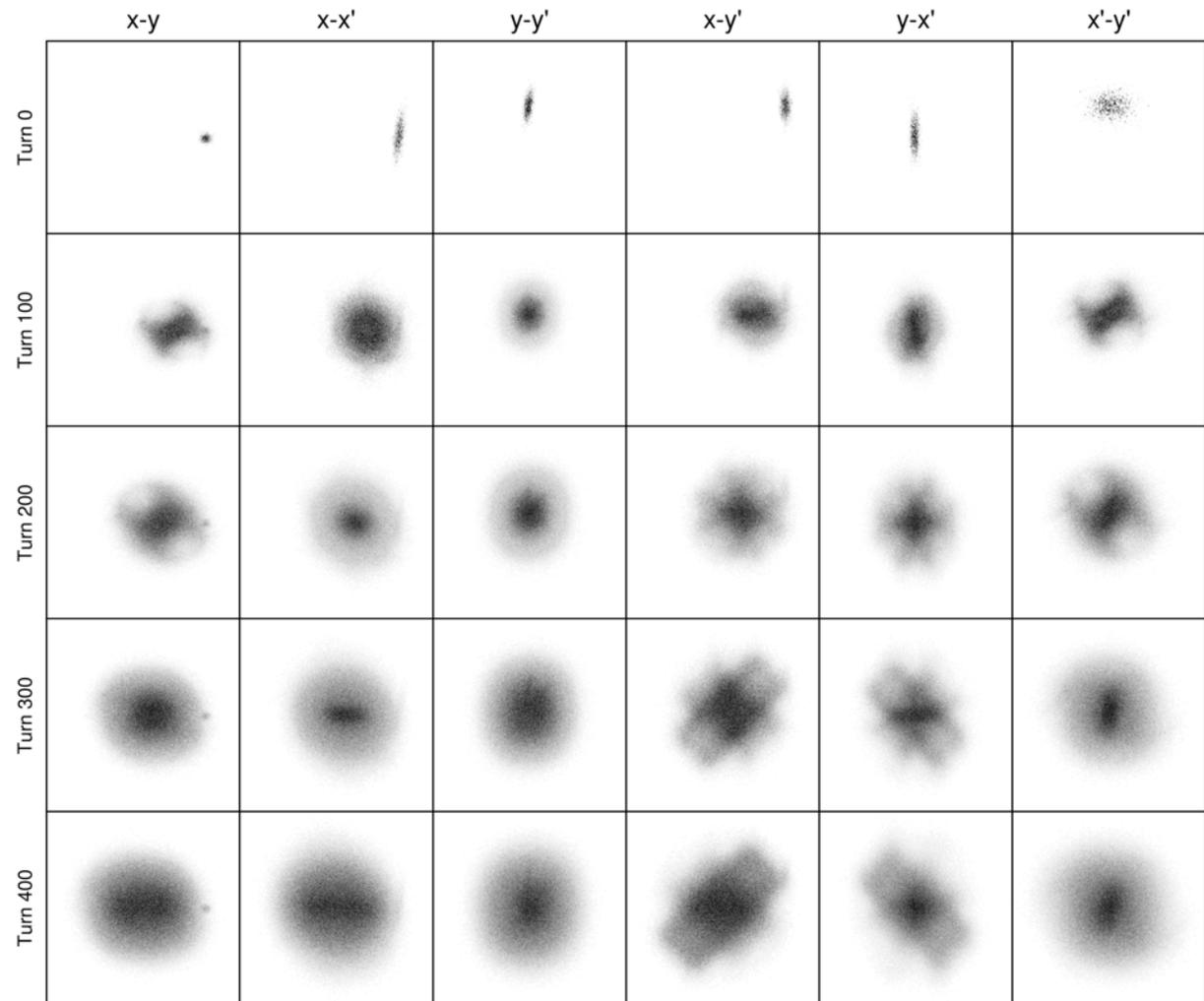
Figure 5.20: Measured wire-scanner profiles for the final distribution in Experiment 3.

Nice emittance ratio, but profile not very elliptical.

# Simulation vs. Measurement – No Solenoids Experiment



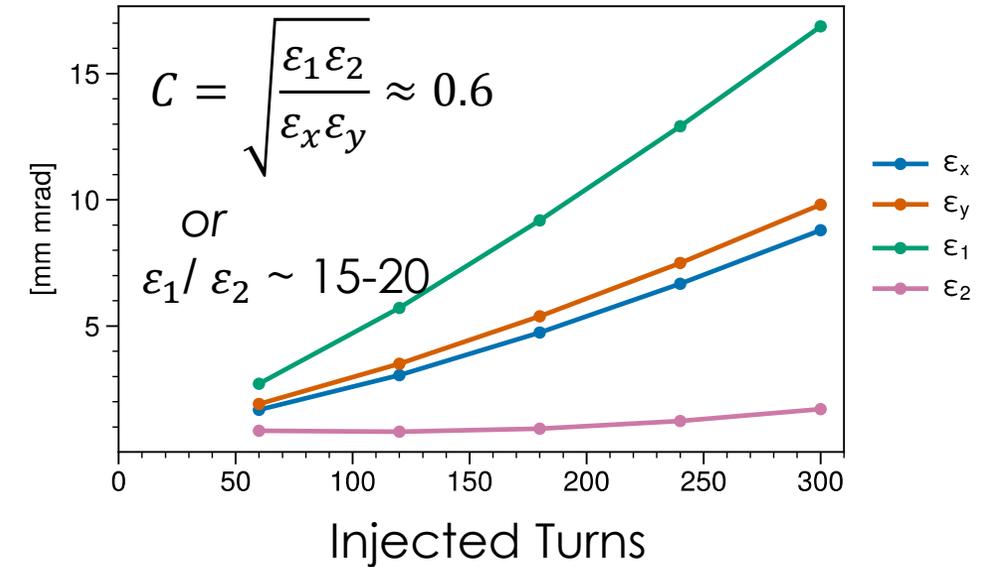
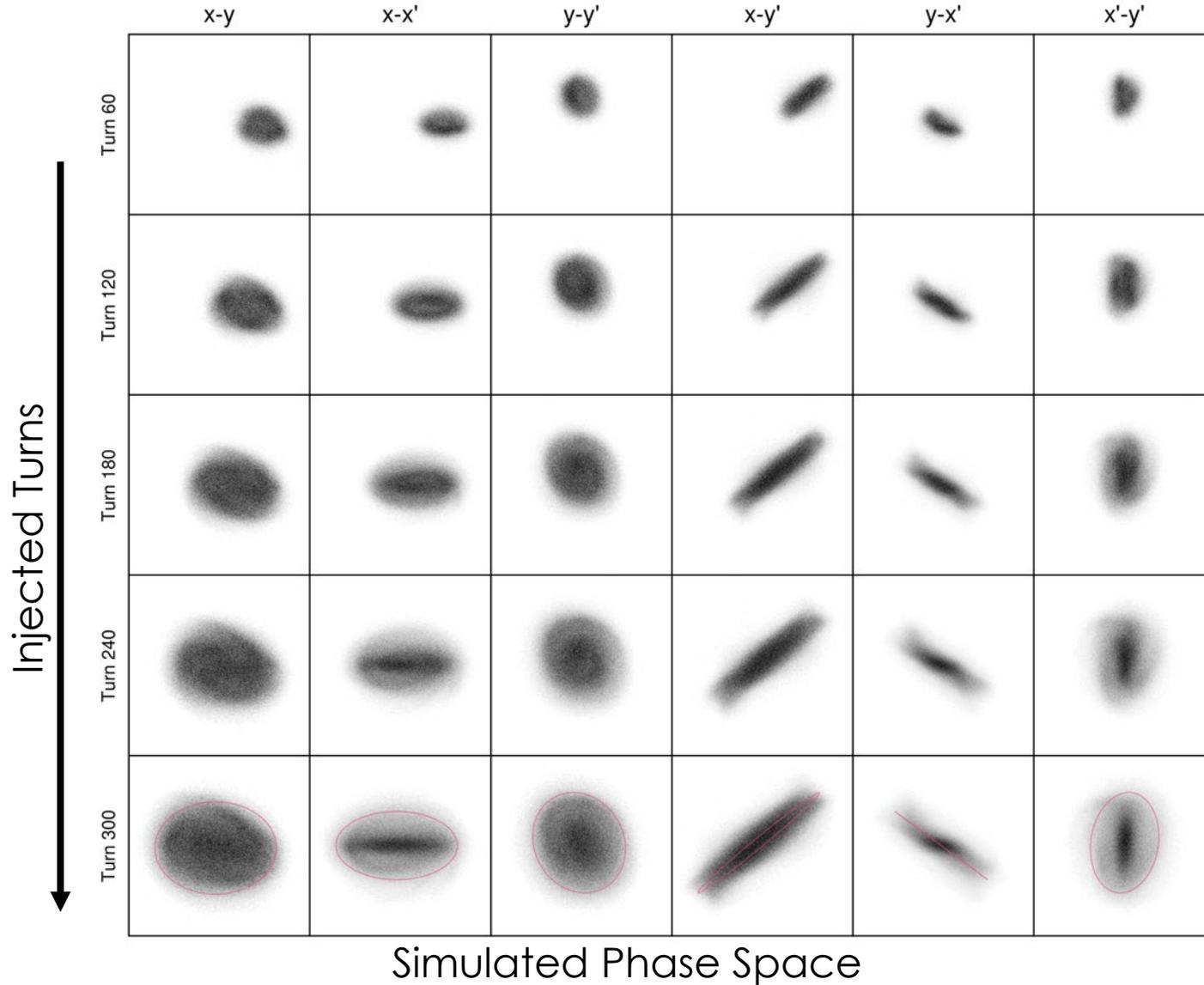
Injected Turns



Simulated Phase Space

Extract beam after N turns are accumulated and measure evolution of emittance.

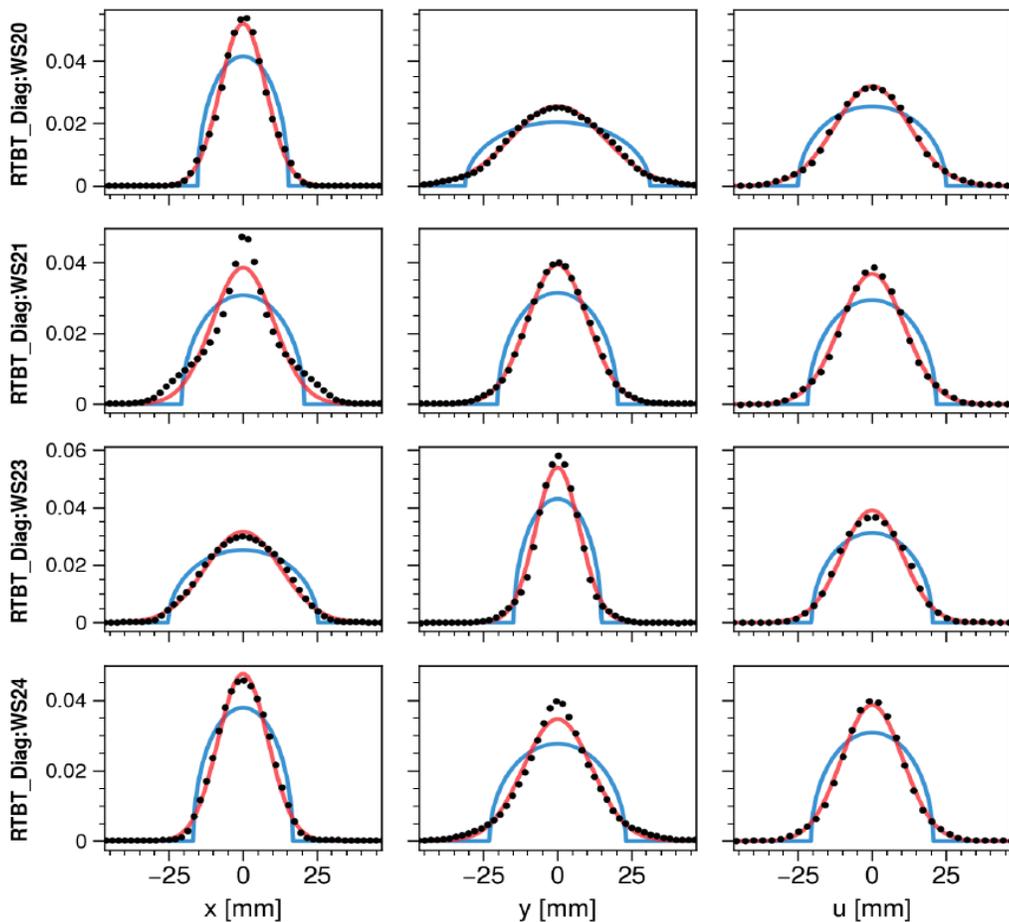
# Simulation with Solenoids



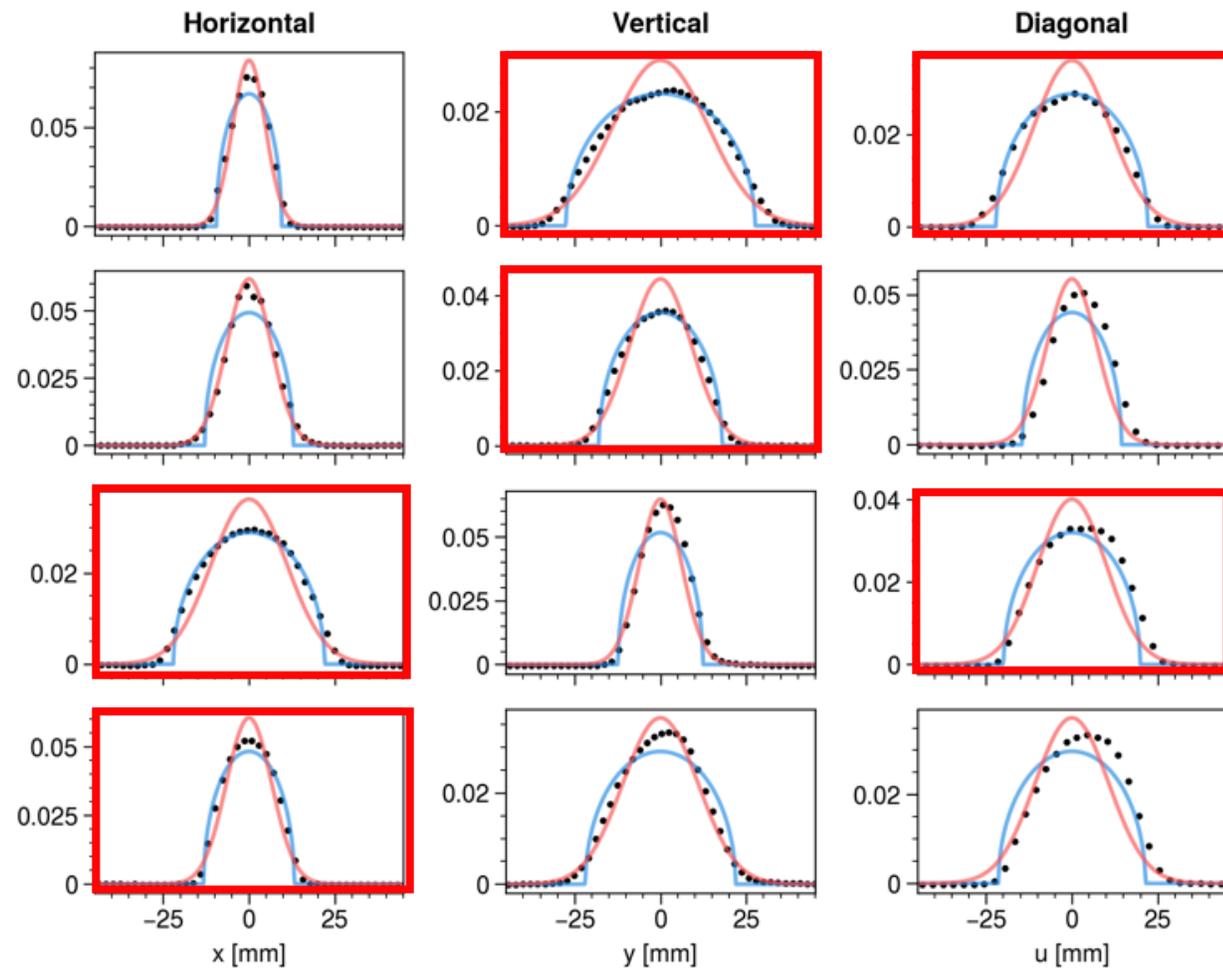
This is a representative “best case” – have not finished with simulation of recent results.

# Wirescans with Solenoids

Without Solenoids



With Solenoids



Red profiles are most elliptical.

# Summary Outlook

- We can 'eigenpaint' in the SNS ring
- Clear difference between case with/without solenoids
- We are interested in exploring behavior of eigenpainted Danilov (or other) distributions over longer storage times, ideas for space charge mitigation both in simulation and experiment

# Acknowledgements

- Thanks to Jeff Holmes, Tim Gorlov, Charles Peters, Dave Brown, Vasiliy Morozov and Austin Hoover for providing simulations, slides, tools, time, and discussion in no particular order