



# Application of infrared FEL oscillators for producing isolated attosecond X-ray pulses via high-harmonic generation in rare gases

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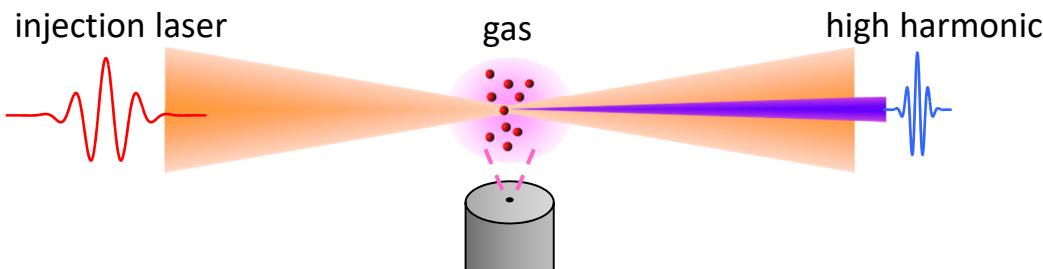
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This work was supported by MEXT Quantum Leap Flagship Program (MEXT Q-LEAP)  
Grant Number JPMXS0118070271.

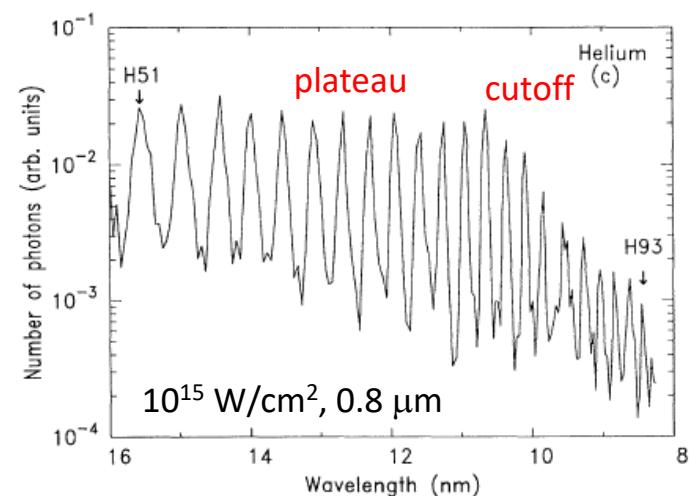
# Contents

- Introduction of HHG and possible combination with FELs
- Few-cycle pulse generation in FEL oscillators
- Stabilization of carrier-envelope phase (CEP)
- Research Program for FEL-HHG

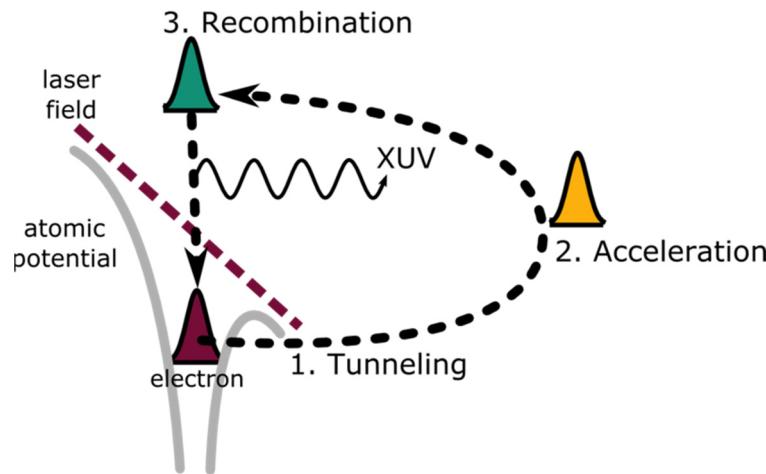
# High Harmonic Generation; HHG



odd-harmonics with time and spatial coherence



Wahlström et al., Phys. Rev. A 48, 4709 (1993)



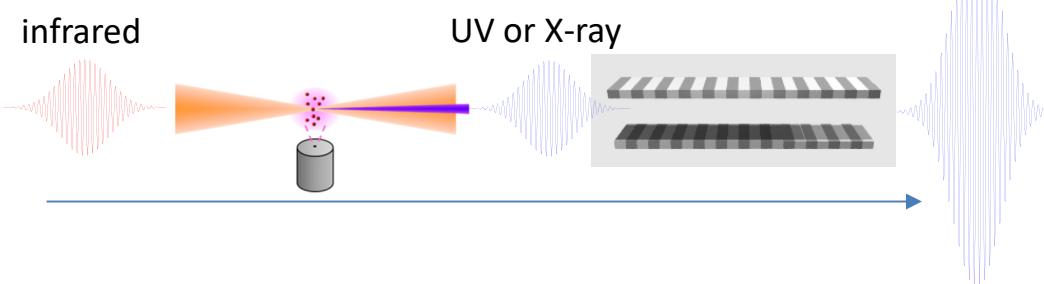
Wikipedia

## 3-step model

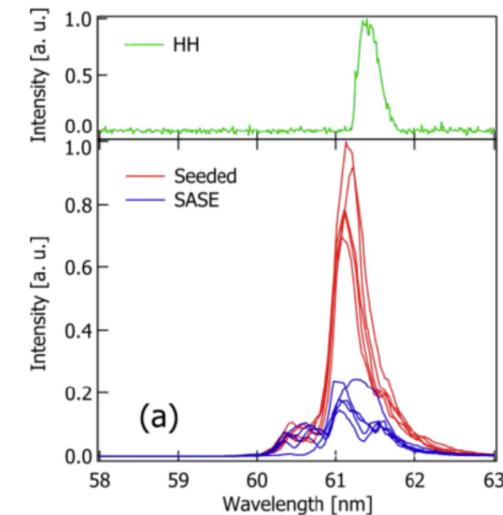
1. tunneling ionization by  $E_{\text{laser}}$
2. acceleration of the electron by  $E_{\text{laser}}$
3. recombination with the parent atom

# Combination of HHG and FEL

## HHG → FEL

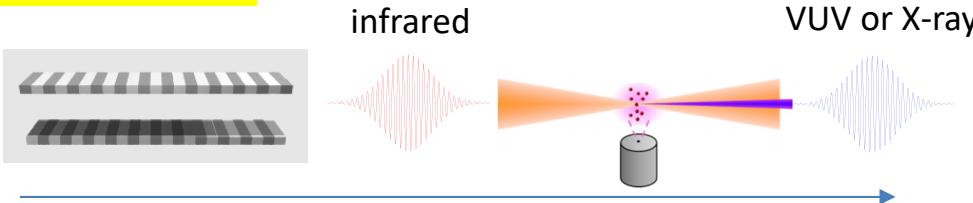


- ✓ By injecting HHG as a seed laser, we can control FEL spectral and temporal shapes to suppress SASE-induced fluctuation.



T. Togashi et al., Opt. Exp. 19, 317 (2011).

## FEL → HHG



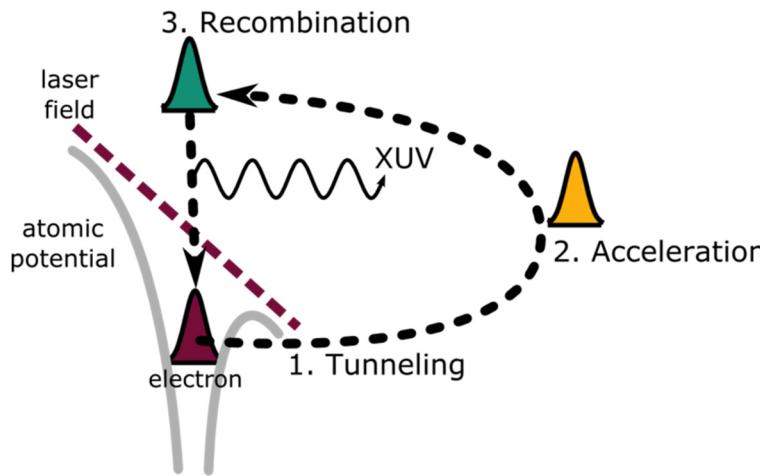
M. Tecimer, PRST-AB 15, 020703 (2012).

- ✓ generating VUV and X-ray with a small-size FEL
- ✓ attosecond pulses available

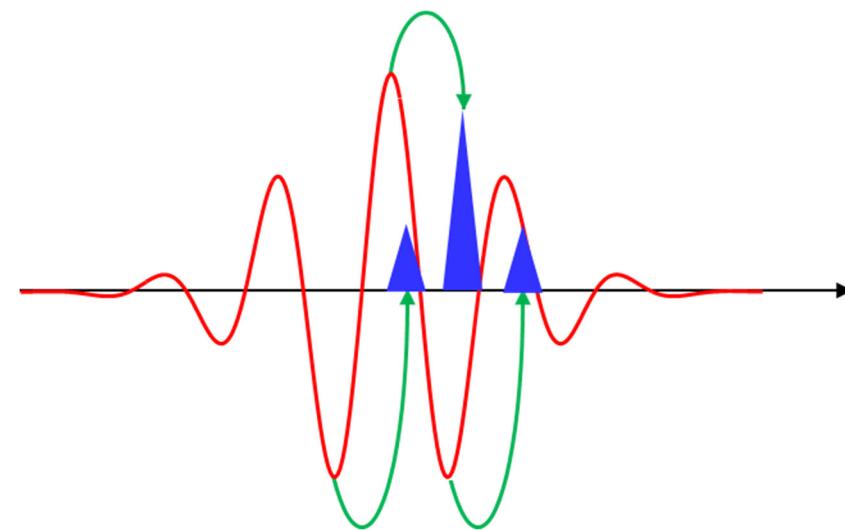
Not demonstrated yet !

# Keys to the attosecond pulse generation in HHG

High Intensity



Few-cycle pulse



Typical laser intensity for HHG

$$\sim 10^{14} \text{ W/cm}^2$$



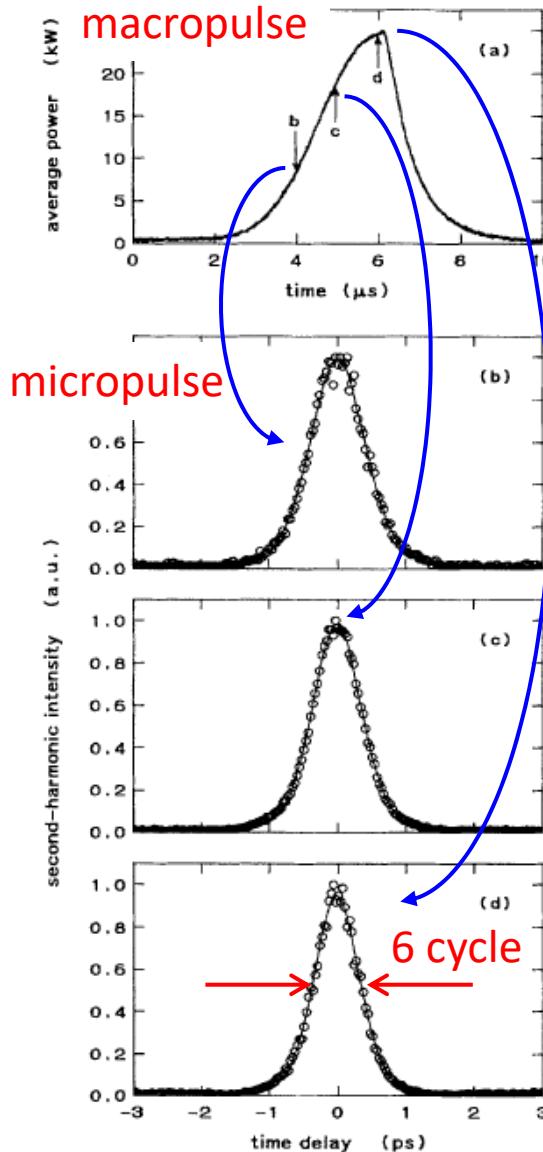
0.3-1 mJ, 3-cycle,  
 $\lambda = 2\text{-}6 \mu\text{m}$ ,  $w = 100 \mu\text{m}$

Can a FEL generate such pulses?

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# Few-cycle FEL pulses (transient regime)



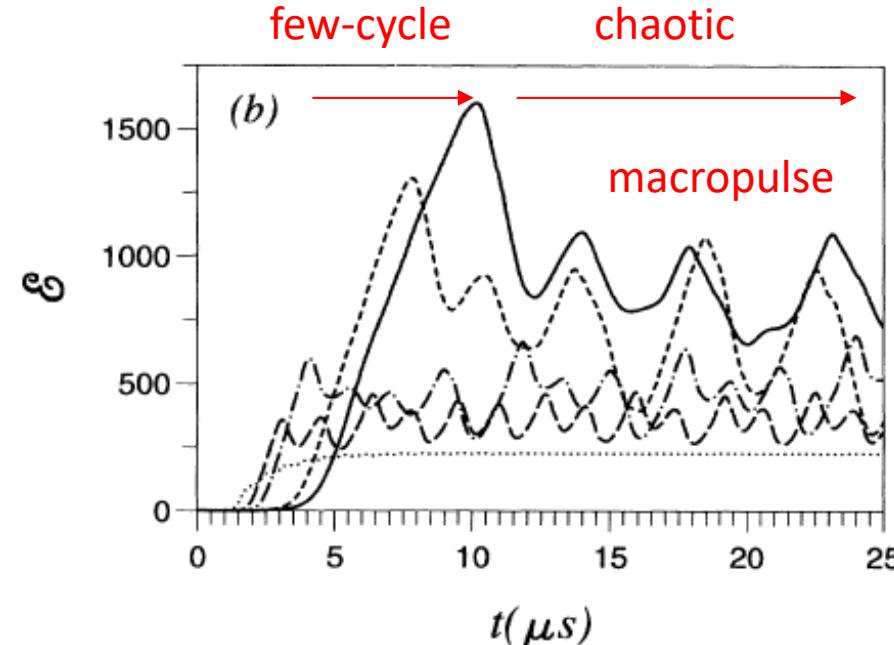
6-cycle pulses were demonstrated at a FEL oscillator, FELIX.

10  $\mu$ J, 6 cycle, 10.4 and 24.5  $\mu$ m

G.M.H. Knippels et al., Phys. Rev. Lett. 75, 1755 (1995)

Few-cycle pulses are only available at the transient regime.  
Chaotic lasing appears after the saturation.

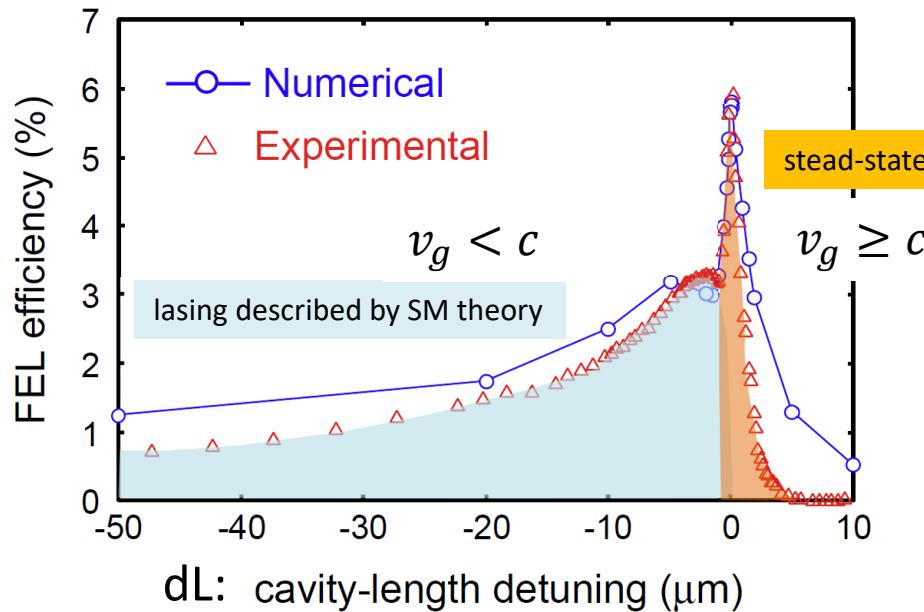
N. Piovella et al., Phys. Rev. E 52, 5470 (1995)



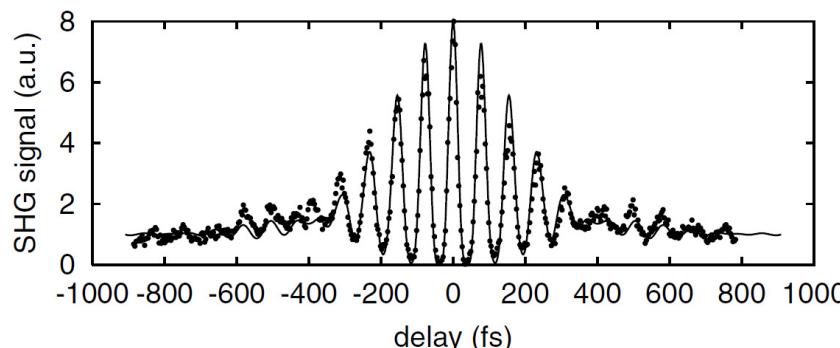
# Few-cycle FEL pulses (steady state)

High-efficiency lasing at  $dL=0$  was found at JAERI FEL.

A few-cycle FEL pulse was confirmed by autocorrelation measurement.



N. Nishimori et al., PRL 86, 5707 (2001)  
R. Hajima et al., NIM-A 475, 270 (2001)



1.55 cycle after chirp compensation  
pulse energy  $\sim 0.2$  mJ

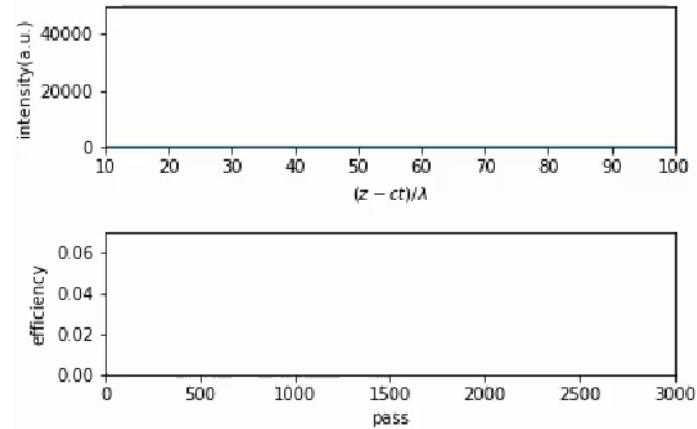
R. Hajima and R. Nagai, PRL 91, 024801 (2003)  
R. Nagai et al., NIM-A 483, 129 (2002)

# Few-cycle pulse evolution in FEL Oscillators

$dL < 0$

Transient regime  
Chaotic lasing

$dL = 0$

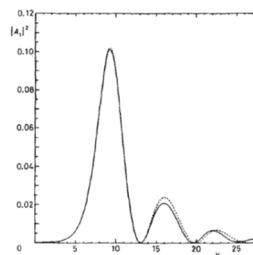


Steady state regime  
Solitary pulse

# Principle of few-cycle pulse generation at dL=0

## Single-pass FEL

weak\* superradiance  
in short-pulse limit



(\*) Peak is lower than the steady-state lasing

R. Bonifacio et al., Riv. Nuovo Cimento (1990)

## Short pulse FEL Oscillator at dL=0

Evolution of a solitary pulse

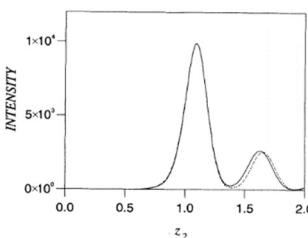
N. Piovella, Opt. Comm. (1991)

R. Bonifacio, N. Piovella, B.W.J. McNeil, PRA (1991)

Superradiant pulse evolution  
at a loss-less cavity

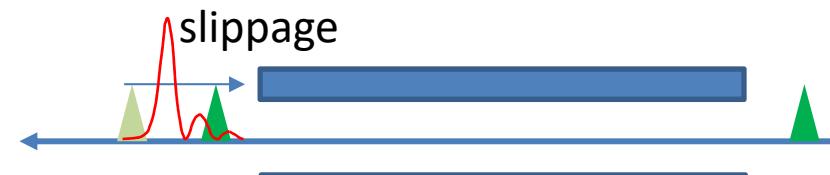
N. Piovella,  
Phys. Rev. E 51, 5147 (1995)

Peak exceeds the steady-state lasing

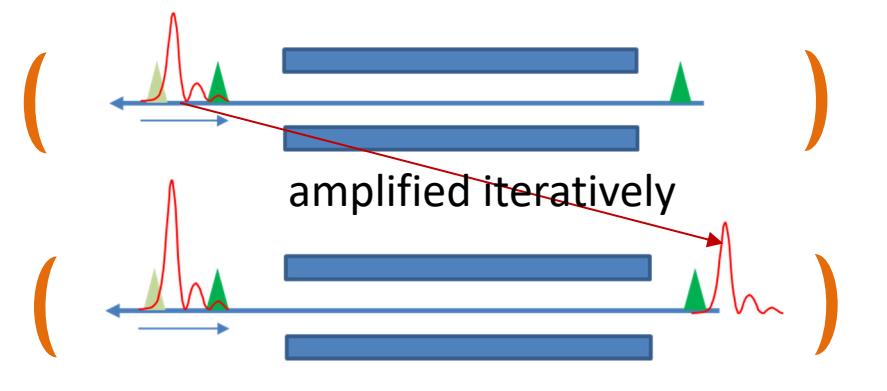


Superradiant pulse evolution  
at a lossy cavity (with shot noise)

R. Hajima et al., NIM-A 475, 270 (2001).



Radiation emitted in the slippage region.



$N$  bunches  $\sim Q = 1/\alpha_0$



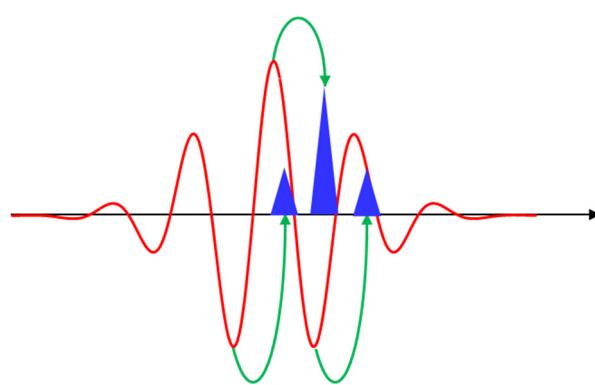
$$\text{peak} \propto N_e^2 \propto (qQ)^2$$

$$\text{width} \propto N_e^{-1/2}$$

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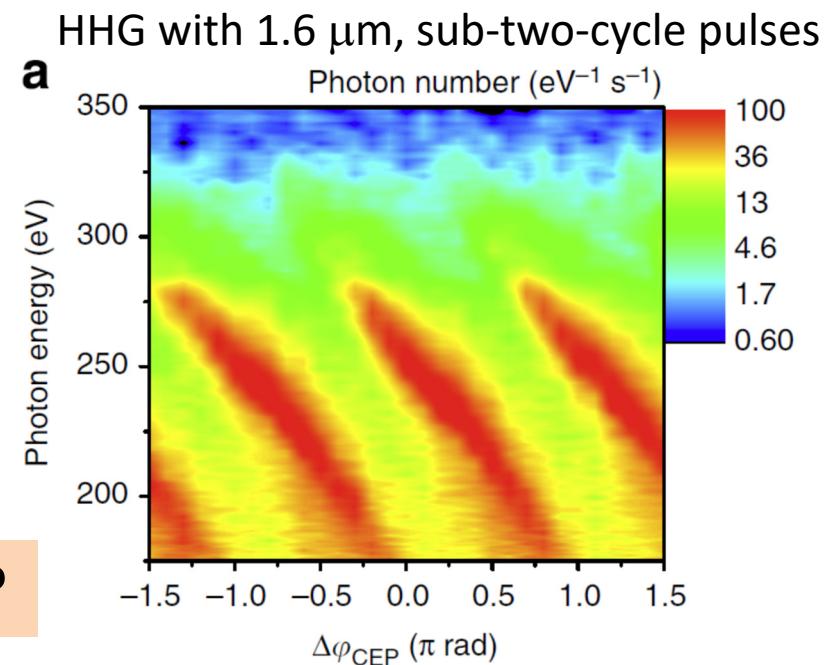
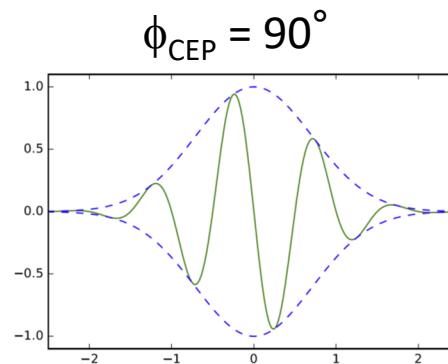
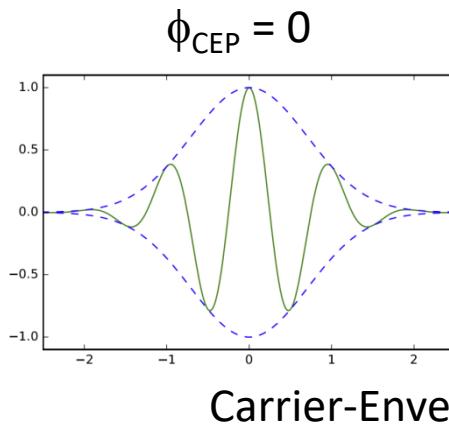
# Carrier-Envelope Phase (CEP)



HHG is governed by laser oscillating electric field.

Carrier-envelope phase (CEP) affects  
the properties of HHG, cut-off energy, spectrum and yield.

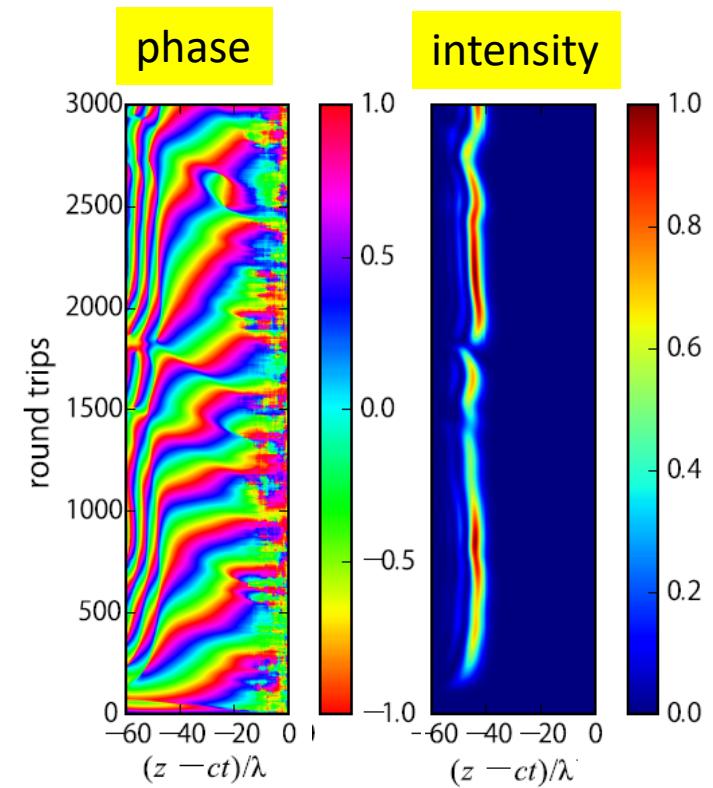
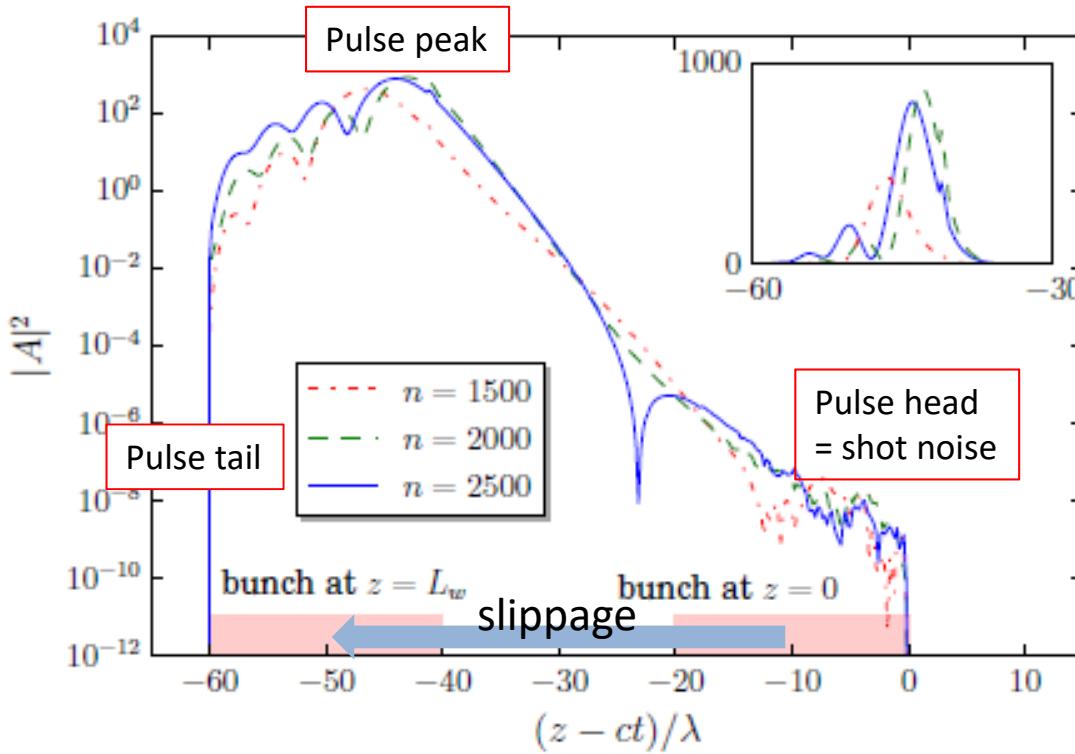
CEP must be stabilized for a practical use of HHG.



Can a FEL generate CEP-stable pulses?

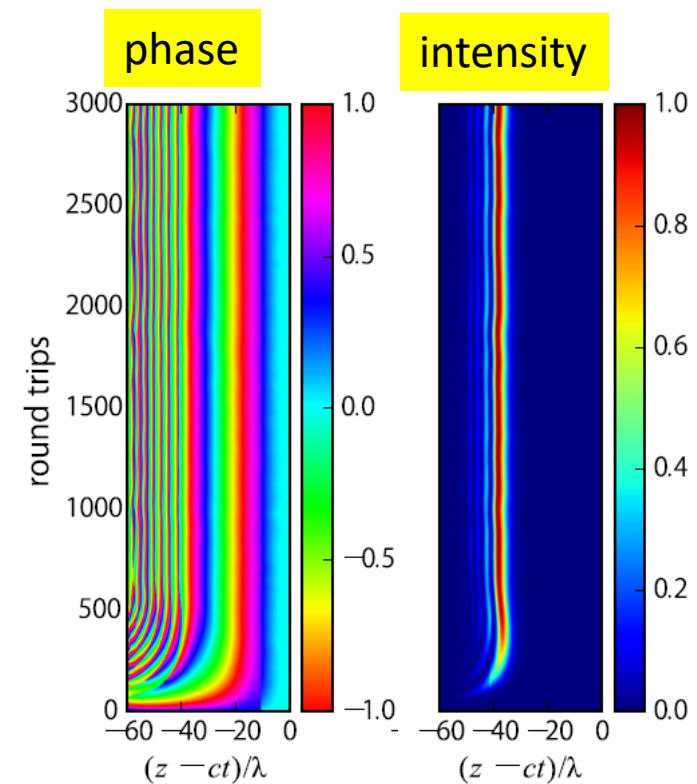
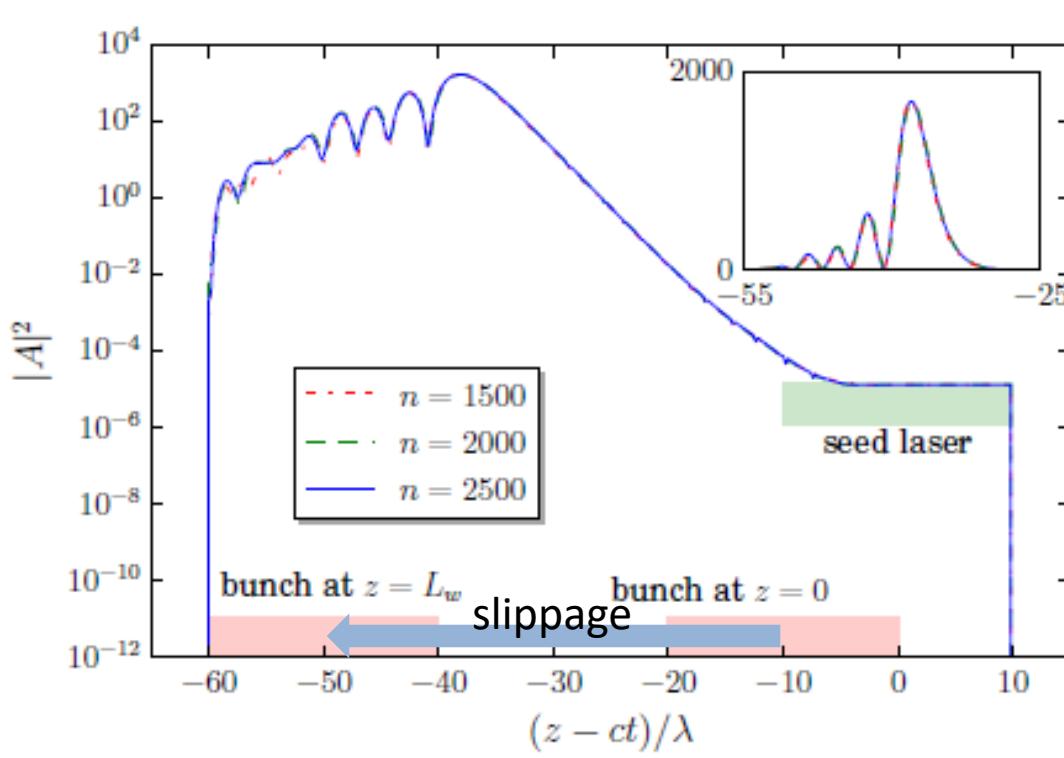
N. Ishii et al., Nature Comm. 5, 3311 (2014).

# FEL simulation for $dL=0$ lasing



- The electron bunch slips back in the optical pulse during the FEL interaction.
- Intensity of the optical pulse spans over 11 orders from shot noise in the head to the pulse peak.
- No intra-pulse feedback from the tail to the head because  $dL=0$ .
- The optical pulse has fluctuation both in its phase and intensity.

# CEP stabilization by an external seed laser

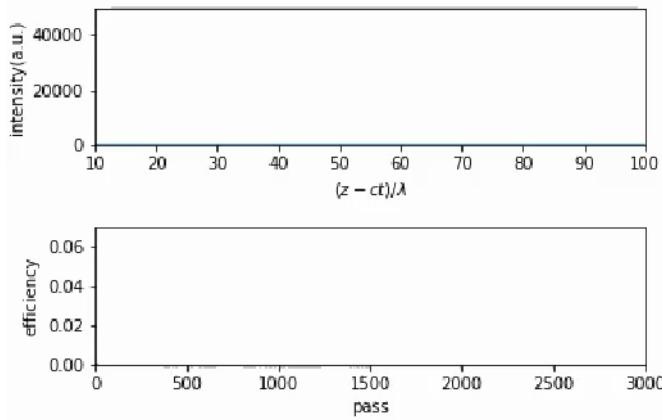


- Introducing a CEP-stabilized seed pulse to overlap the shot-noise part
- The leading edge of FEL pulse has a fixed amplitude and phase.
- The FEL interaction starts with a well-defined optical field.
- Over-all lasing dynamics is stabilized.
- CEP-stabilized few-cycle FEL pulses

R. Hajima and R. Nagai, PRL 119, 204802 (2017)

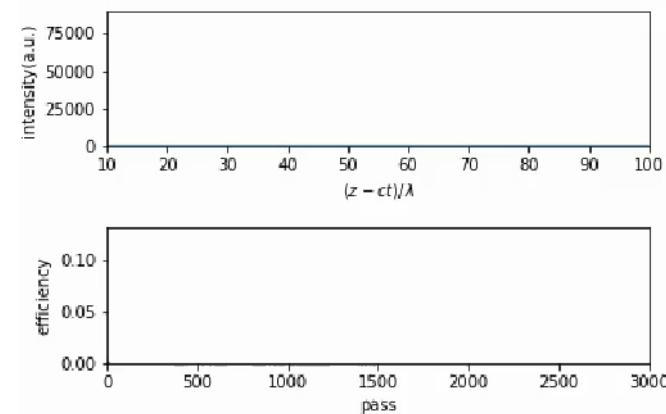
# Stabilization by an external seed laser

Lasing at  $dL=0$



Without a seed laser

Fluctuation due to the shot noise



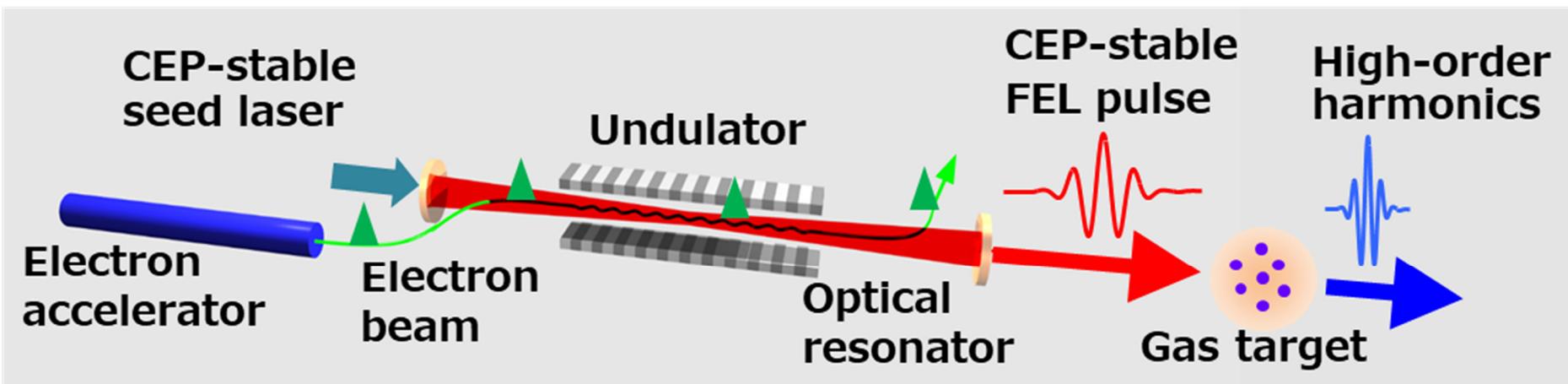
With a seed laser

Stabilization by the seed laser

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# Proposal of FEL-HHG



Infrared FEL Oscillator

+

Lasing at zero-detuning length → Few-cycle pulse

+

Seed laser → CEP stabilization

+

High-harmonic generation → Attosecond VUV/X-ray pulses

# Design Parameters

To obtain 0.5-mJ, few-cycle pulses

$$\lambda = 2 \text{ } \mu\text{m} \quad 85 \text{ MeV} \times 60 \text{ pC} \times 10\% = 0.5 \text{ mJ}$$

$$\lambda = 6 \text{ } \mu\text{m} \quad 50 \text{ MeV} \times 100 \text{ pC} \times 10\% = 0.5 \text{ mJ}$$

	(A)	(B)
Electron beam		
energy (MeV)	85	50
bunch charge (pC)	60	100
norm. emittance ( $x/y$ ) (mm-mrad)	12/12	12/12
bunch length (ps)	0.27	0.4
peak current (A)	220	250
bunch repetition (MHz)	10	10
undulator		
undulator parameter (rms)	1.34	1.25
pitch (cm)	4.0	4.5
number of periods	80	40
FEL		
wavelength ( $\mu\text{m}$ )	2	6
Rayleigh length (m)	0.92	0.52
FEL parameter, $\rho$	0.0030	0.0052
cavity loss	6%	4%

These parameters are within the existing technologies of SCA linacs.



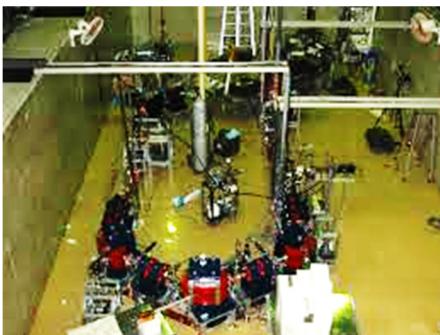
Photocathode gun



L-band SCA

# A research program has been launched for the FEL-HHG

Kyoto University



KU-FEL (3.4-26 μm)

Nihon University

LEBRA-FEL (0.827-6.1 μm)

Normal conducting linacs are utilized for R&D and a PoC experiment.



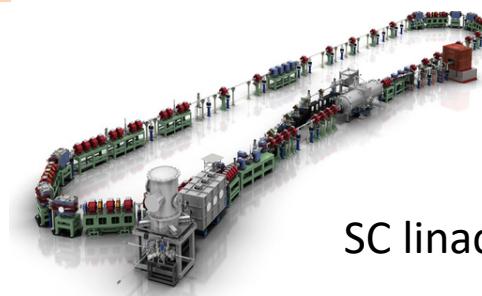
QST

Laser laboratory



KEK

Compact ERL



MEXT Q-LEAP

2018-2023

Development of basic technologies

2024-2027

Proof-of-Concept experiment of FEL-HHG

SC linac technologies

User facility of attosecond VUV/X-ray

# Challenge the efficiency, pulse duration limit

Analytical studies suggest

In short-pulse FELs,  
efficiency and optical cycles scale as

$$4\pi N_w \eta \approx 1.43/\sqrt{\alpha}$$

$$N_s \approx 0.56 N_w \sqrt{\alpha} \quad \text{for small } dL$$

$\alpha$ : cavity loss normalized by gain parameter

N. Piovella, P. Chaix, G. Shvets, D.A. Jaroszynski, PRE (1995)  
P. Chaix, N. Piovella, G. Grégoire, PRE (1999)

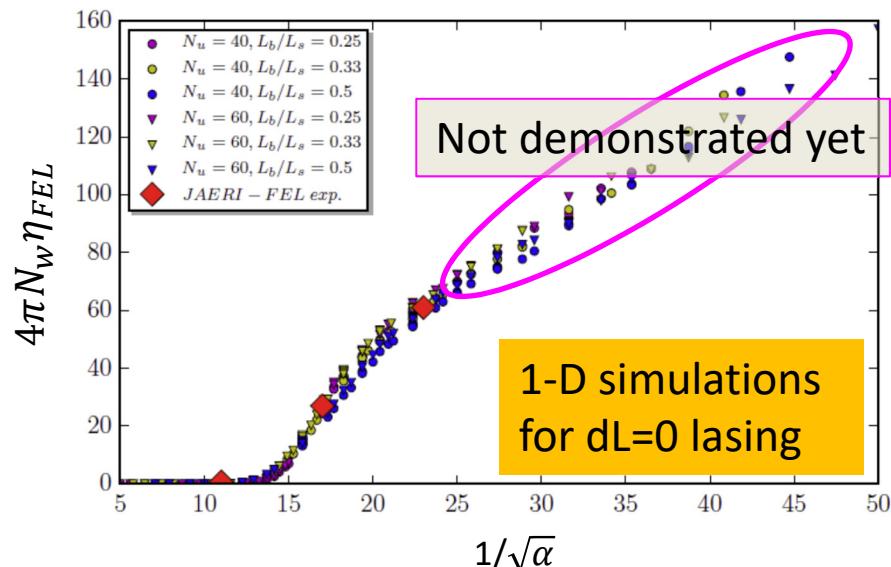
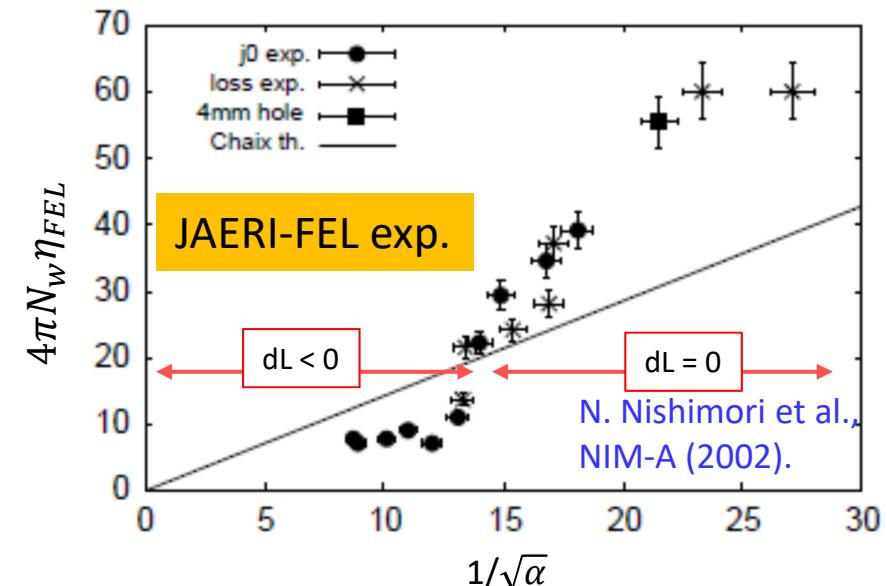
“solitary FEL pulse” in FEL oscillator of  $dL=0$

N. Piovella, Opt. Comm. (1991)  
R. Bonifacio, N. Piovella, B.W.J. McNeil, PRA (1991)

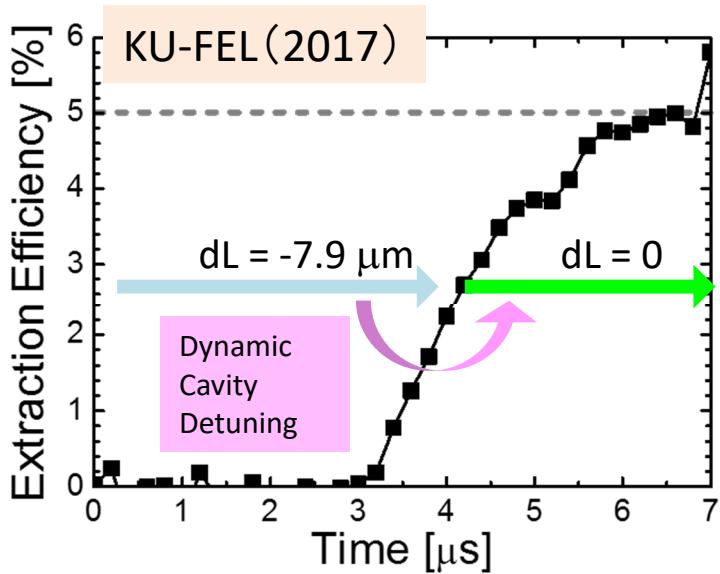
threshold exists for “solitary FEL pulse”

$$S \geq 1 + 2K^{3/2} \left[ 1 - \left( 2\sqrt{3/9} \right) \log|b_0| \right]^{3/2}$$

N. Piovella, Opt. Comm. (1991)



# High-efficiency lasing at KU-FEL

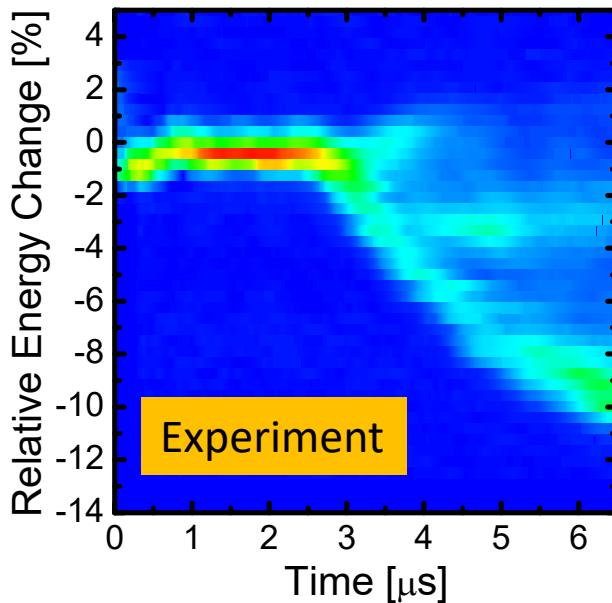


We follow the technique of dynamic cavity desynchronization (DCD).

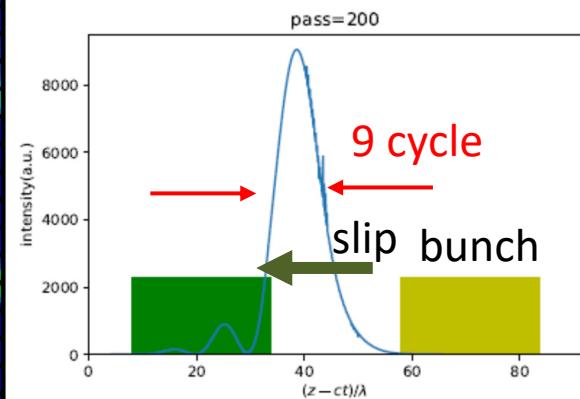
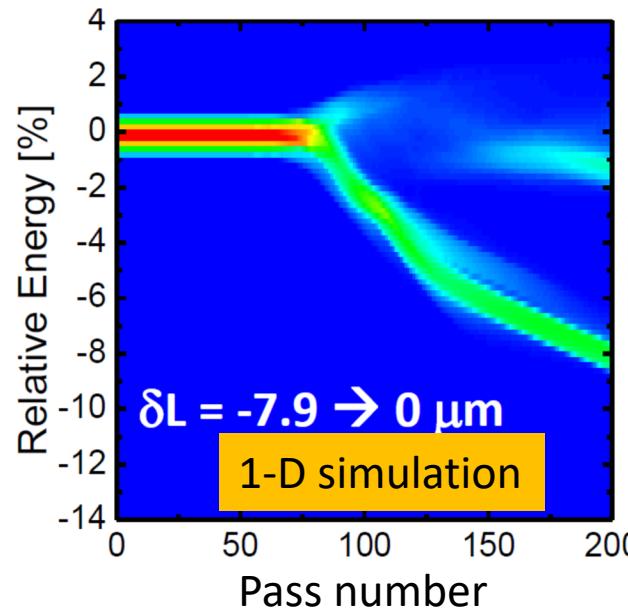
D.A. Jaroszynski et al., NIMA (1990),  
R.J. Bakker et al., PRE (1993).

Bunch repetition is modulated to introduce effective cavity-length variation in a macro pulse.

"dL=0 lasing" is obtained at a normal conducting FEL.



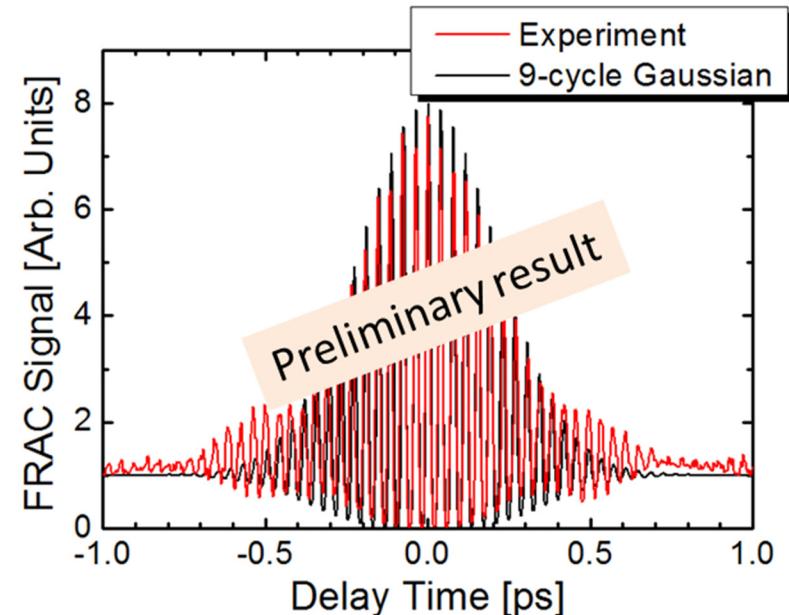
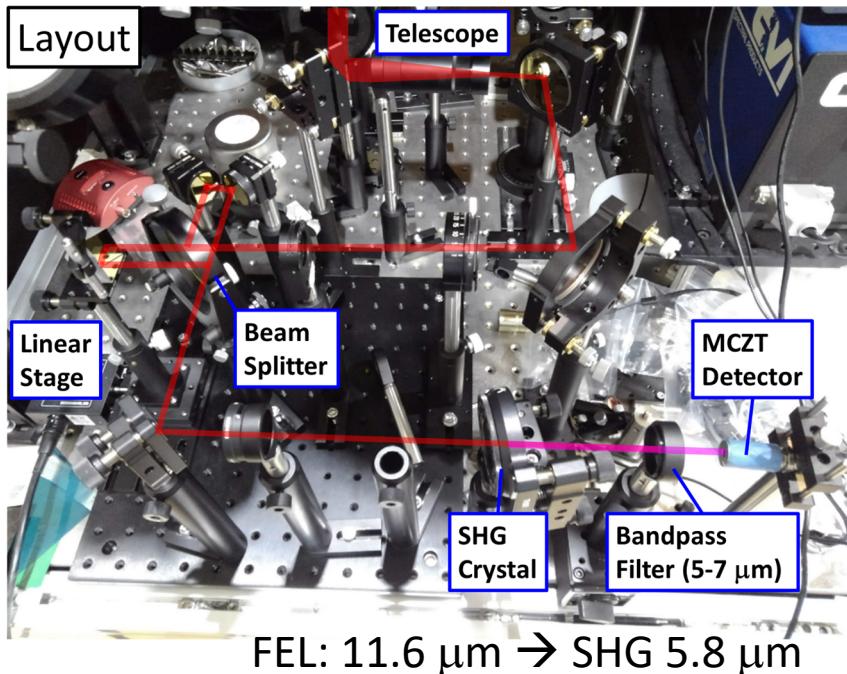
H. Zen et al., Poster TUP013



Simulation suggests  
a 9-cycle pulse

# FEL pulse measurement at KU-FEL

## Fringe-resolved auto correlation (FRAC)

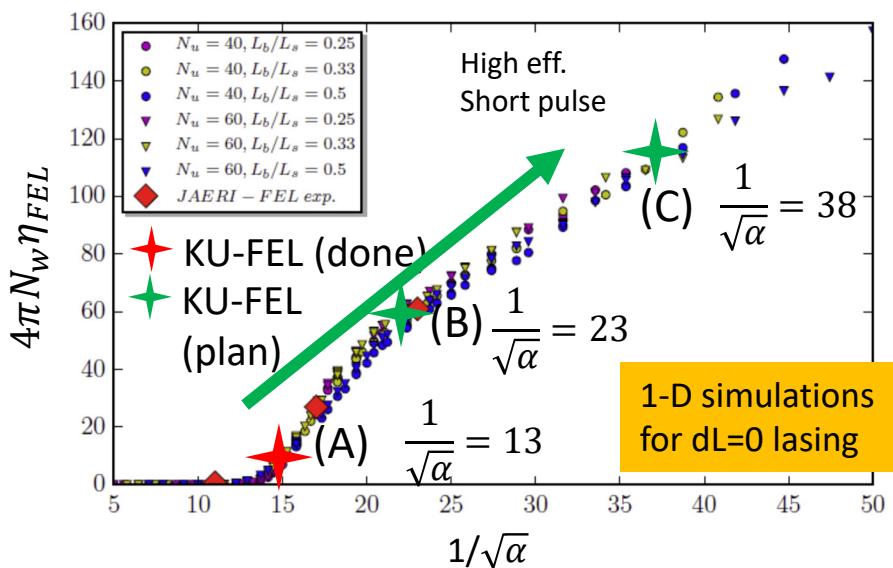


Pulse duration is evaluated by FRAC.

Measured FRAC signal is examined with Gaussian pulses and numerical results.

Further measurements and analysis are in progress.

# Challenge the efficiency, pulse duration limit at KU-FEL



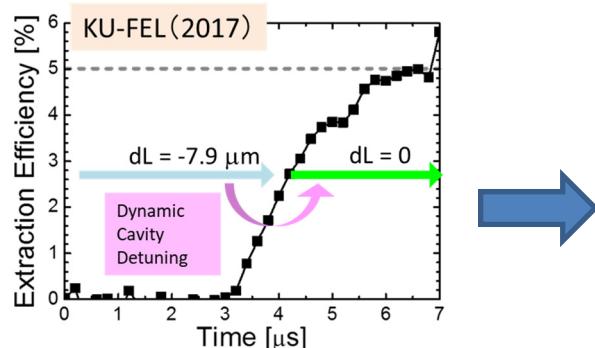
$$\alpha = \alpha_0 / \Gamma$$

$\alpha_0$  cavity round-trip loss

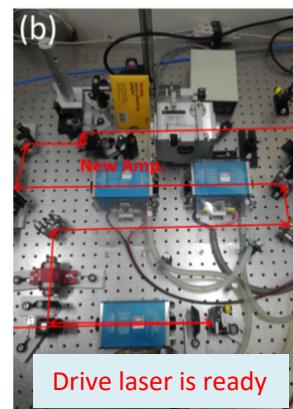
$\Gamma = (L_b / L_s)(j_0 / 2)$  gain integrated over the slippage length

$N_s \propto 1/\eta$  optical cycle

N. Piovella et al., PRE (1995); P. Chaix et al., PRE (1999)



(A) 4.5-cell RF gun with thermionic-cathode mode (40 pC,  $\lambda=11\text{ }\mu\text{m}$ )



(B) 4.5-cell RF gun with photo-cathode mode (120 pC)

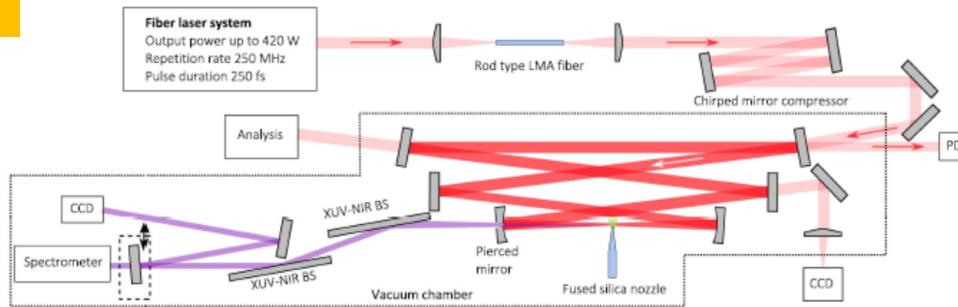
(C) Replace a hole-coupled mirror by a low-loss dielectric mirror (loss = 3% → 1%)



(D) Install a new 1.6-cell RF gun (1-nC bunch train)

# Pulse stacking in an external enhancement cavity

HHG



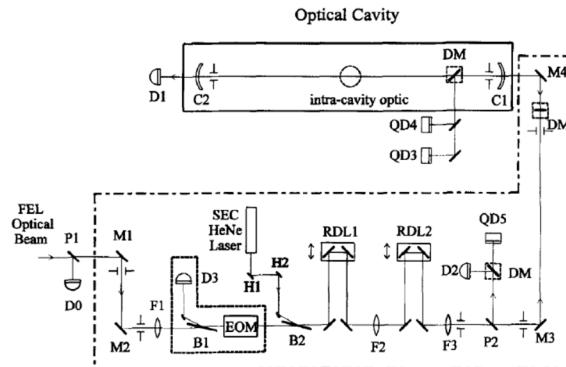
MPQ

Enhancement is 170 W → 10 kW

H. Carstens et al., Optica (2016).

External enhancement cavities in FELs

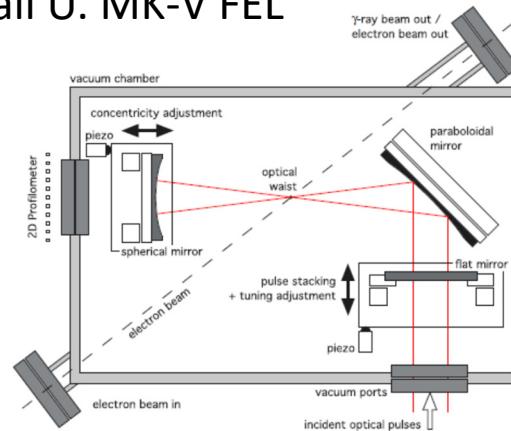
Stanford SCA FEL



75-times enhancement  
in the steady-state regime (quasi-CW)

T.I. Smith et al., NIMA (1997).

Hawaii U. MK-V FEL



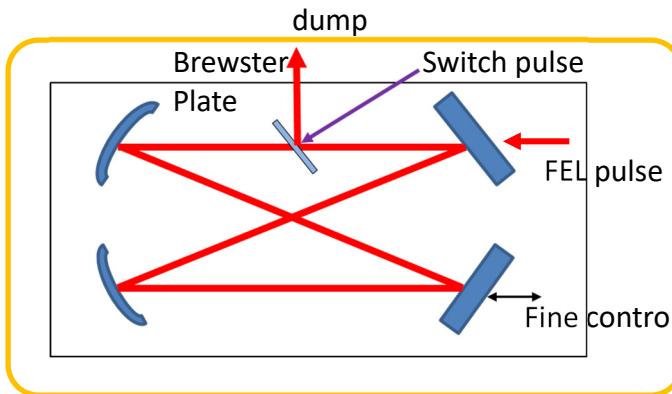
GHz repetition with phase-locked FEL  
in the transient regime (4.5 μs)

P. Niknejadi et al., PR-AB (2019).

# Pulse stacking cavity at LEBRA FEL

LEBRA FEL has a relatively long macro pulse (20  $\mu$ s)

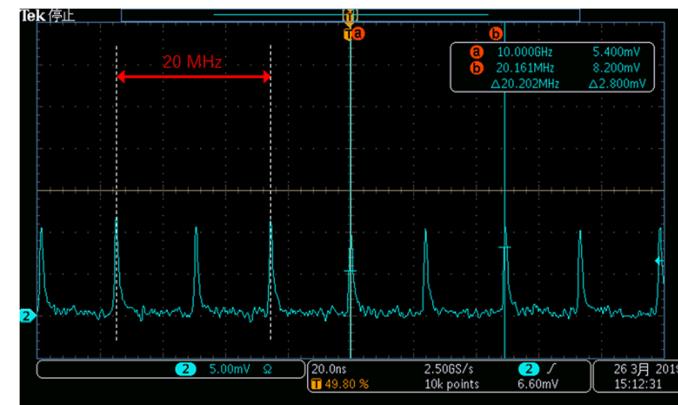
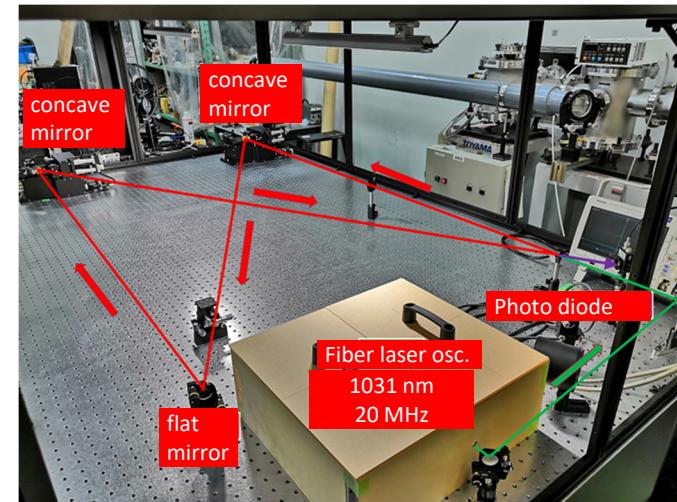
→ Suitable for pulse stacking experiment.



External cavity is under development.  
Recirculation was confirmed with a fiber laser.

We continue the experiment to demonstrate pulse enhancement, first with the mode-locked fiber laser, and then real FEL pulses.

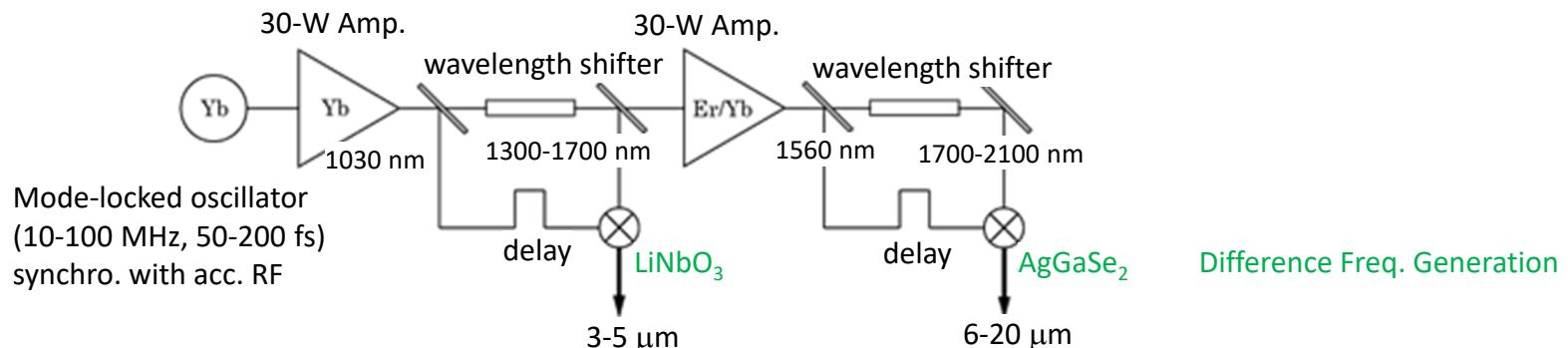
Intracavity exp. and cavity dumping are planned for HHG.



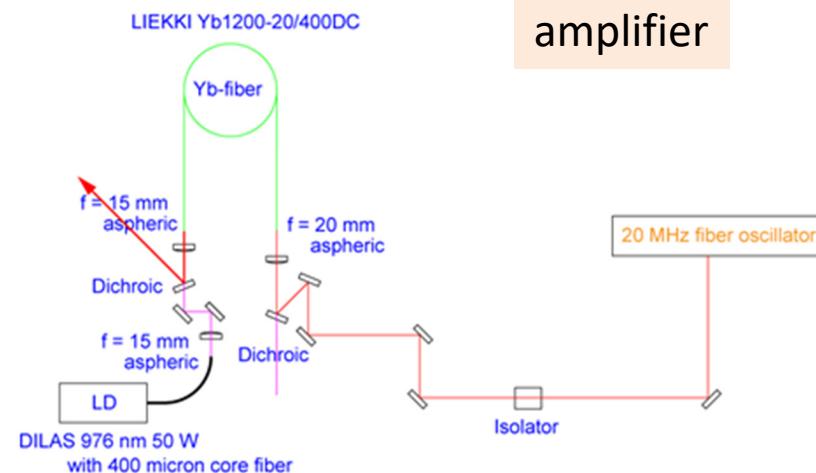
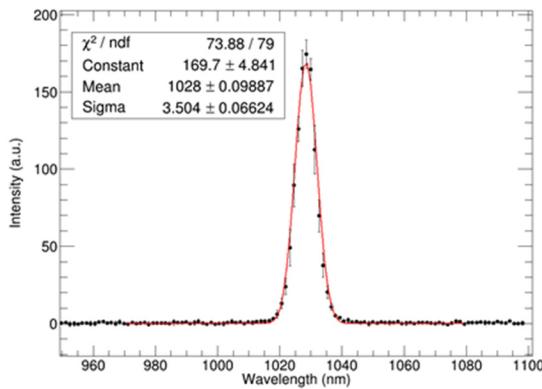
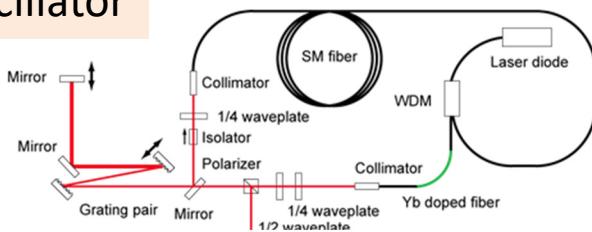
# Mid-IR laser for seeding FEL

## Laser system

CEP-stable Mid-IR pulses synchronized to the acc. RF.

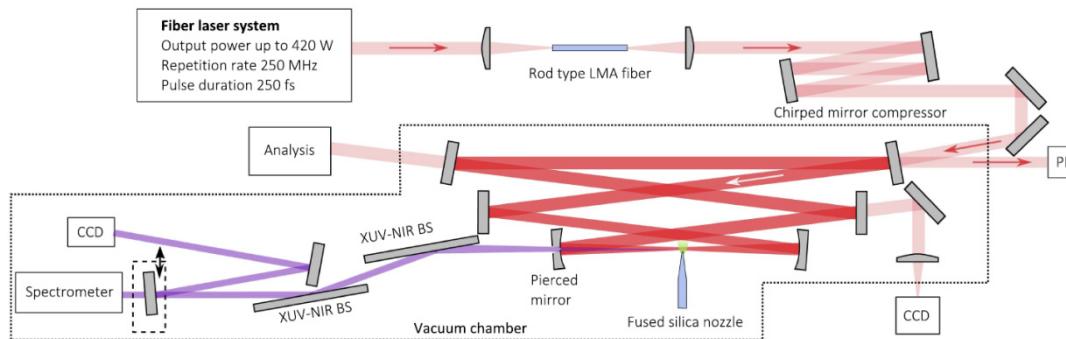


## oscillator



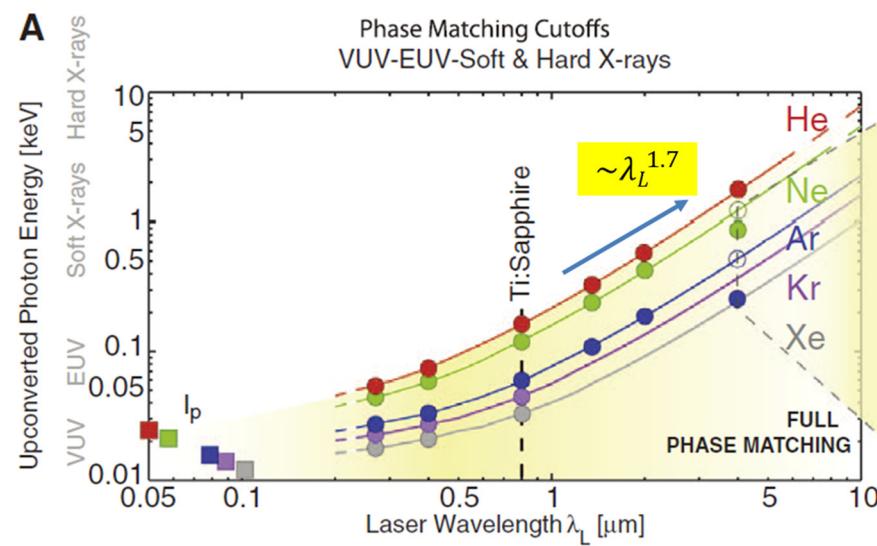
## amplifier

# What are Impacts of FEL-HHG ?



HHG in a laser enhancement cavity for UV/X-ray frequency combs, and pump-probe photoelectron microscopy and spectroscopy  
-- 250 MHz, 10 kW, 30 fs

H. Carstens et al., Optica 3, 366 (2016).



## 1. Higher flux

Average power of FEL can exceed 100 kW with an external cavity of a modest Q ~25.

## 2. Higher photon energy

Mid-infrared FEL (4-10 μm) is suitable for generating 1-10 keV in HHG.

T. Popmintchev et al., Science 336, 1287-1291 (2012).

# Summary

- Few-cycle pulses are available in a FEL oscillator at  $dL=0$ .
- CEP-stabilization is possible with injection seeding.
- Operated at mid-infrared wavelengths, the FEL is an efficient driver of HHG to produce high-flux and high-energy photon pulses with attosecond duration.
- A research program has been launched for technology development and a proof-of-concept experiment of FEL-HHG.
  - Challenge the limit of efficiency and pulse duration (KU-FEL)
  - FEL pulse stacking at an external cavity (LEBRA-FEL)
  - Seed laser (QST)
  - PoC experiment (KU-FEL and/or LEBRA-FEL)
- After the PoC, a full-scale FEL-HHG can be constructed with a SC linac FEL.