

# Short Rayleigh Length Free Electron Lasers

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- **Motivation:** consider compact FEL oscillators
  - Scientific laboratories want compact FELs
  - Industrial & military applications need compact FELs
  - Assume “compact” means mirror separation  $S < 12$  m
  - Mirror damage at intensities  $I > 1 \rightarrow 10 \text{ kW/cm}^2$
  - Typical FEL design:  $\perp$  size  $\approx 1 \text{ mm}$ ,  $\parallel$  length  $\approx 10 \text{ m}$   
 **$\Rightarrow$  mirror damage limits optical power !!**



# FEL Design Examples

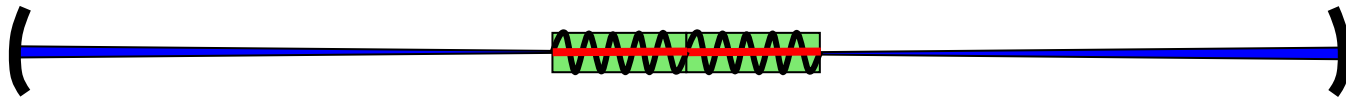


- o **Assume:** Compact FEL mirror separation:  $S \approx 12 \text{ m}$ 
  - o Mirror damage at intensities like  $I > 1 \rightarrow 10 \text{ kW/cm}^2$
  - o Diffraction of mode radius  $w(z) = w_0(1+z^2/Z_0^2)^{1/2}$   
where optical Rayleigh length is  $Z_0 = \pi w_0^2 / \lambda$
  - o Typical FEL interaction gives  $w_0 \approx 2r_b \approx 1 \text{ mm}$
  - o Resonator output coupling (10%):  $Q_n \approx 10$
  
- o **Example 1:** desired wavelength  $\lambda \approx 1 \mu\text{m}$  (infrared)
  - o FEL interaction:  $w_0 \approx 2r_b \approx 1 \text{ mm} \Rightarrow Z_0 \approx 3 \text{ m}$
  - o Mode area at mirror ( $z \approx S/2 \approx 6 \text{ m}$ ) is  $A \approx 0.15 \text{ cm}^2$
  - Therefore: FEL power limited to  $P_{\text{out}} < 150 \text{ W}$**
  
- o **Example 2:** desired wavelength  $\lambda \approx 0.1 \mu\text{m}$  (UV)
  - o FEL interaction:  $w_0 \approx 2r_b \approx 1 \text{ mm} \Rightarrow Z_0 \approx 30 \text{ m}$
  - o Mode area at mirror ( $z \approx S/2 \approx 6 \text{ m}$ ) is  $A \approx 0.03 \text{ cm}^2$
  - Therefore: FEL power limited to  $P_{\text{out}} < 3 \text{ W}$**

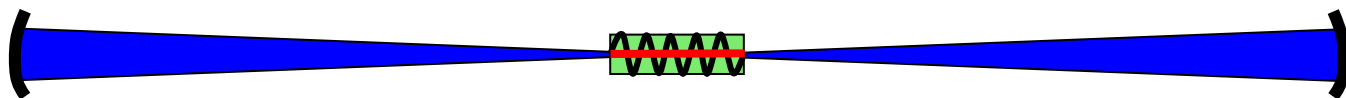


# Short Rayleigh Length FEL Concept

- o Alter a basic design rule:  $Z_0 \approx 0.5L$   
where  $L$  is undulator length, typically  $L \approx$  meters
- o Short Rayleigh Length (SRL) reduces mirror intensity
- o Determine SRL by adjust mirror radius of curvature
- o FEL interaction altered with SRL mode:
  - o rapidly changing optical amplitude and phase - bad !
  - o accelerated bunching in more intense optical fields - good !
- o Conventional FEL:



- o Short Rayleigh Length FEL\*:

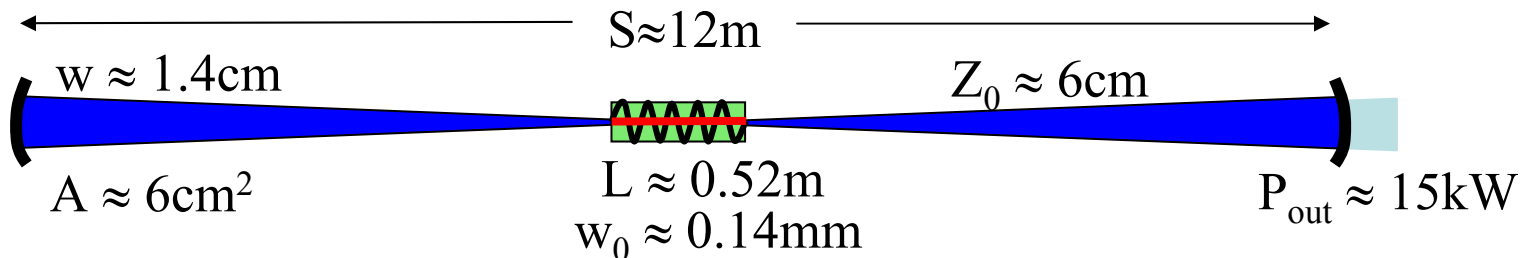


\* NIM A **393**, 262 (1997)



# A Short Rayleigh Length FEL Design

- SRL expands mode and protects mirrors
- Expanding mode requires shorter undulator length  $L$
- Shorter  $L$  requires adequate peak current in micropulse
- **Example SRL FEL:**
  - Undulator:  $N \approx 22$ ,  $L \approx 52\text{cm}$ ,  $\lambda_o \approx 2.36\text{cm}$ ,  $K \approx 1$
  - Electron Beam:  $E_b \approx 80\text{MeV}$ ,  $I_{\text{peak}} \approx 400\text{A}$ ,  $r_b \approx 0.06\text{mm}$
  - Optical:  $\lambda = \lambda_o(1+K^2)/2\gamma^2 \approx 1\mu\text{m}$
  - Resonator:  $S \approx 12\text{m}$ ,  $Z_0 \approx 6\text{cm}$ ,  $w_0 \approx 0.14\text{mm}$ ,  $Q_n \approx 4$
  - At mirror:  $w \approx 1.4\text{cm}$ ,  $A \approx S^2\lambda/4Z_0 \approx 6\text{cm}^2$ ,  **$P_{\text{out}} \approx 15\text{kW}$**

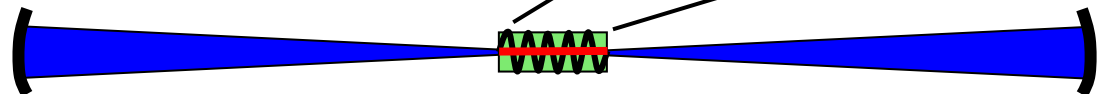
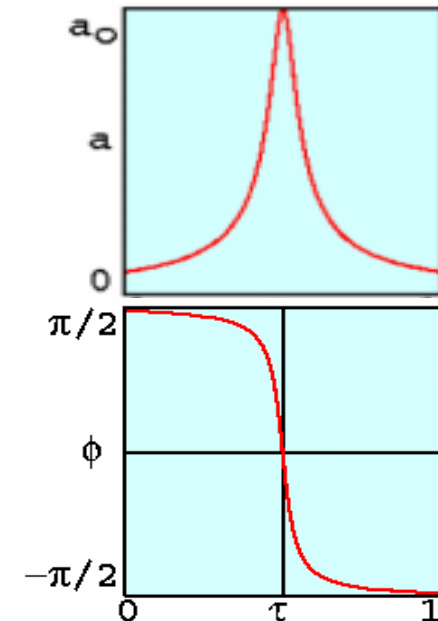


# FEL Interaction with a Short Rayleigh Length Mode

- Electrons interact with field along undulator from  $\tau = ct/L = 0 \rightarrow 1$
- Electrons “see” intense optical field  
 $a(\tau_w)$  and phase  $\phi(\tau_w)$  at mode focus  $\tau_w$
- Rapidly changing field reduces FEL interaction, but surprisingly OK
- Examine FEL interaction:  $r_b$ ,  $N$ ,  $Z_0$
- Examine FEL gain,  $G$ , in weak fields
- Examine FEL extraction,  $\eta$ , in strong fields

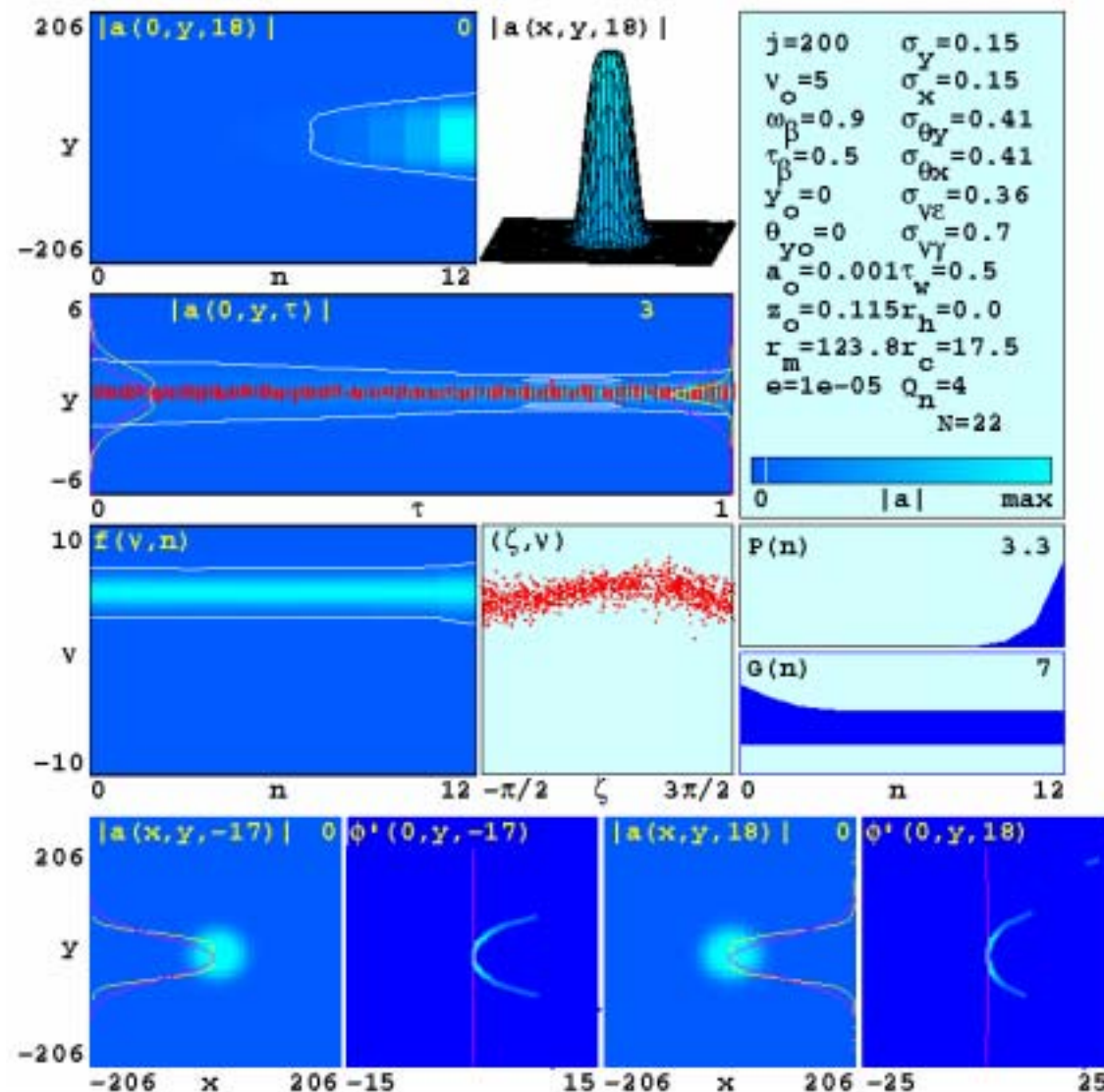
$$a(\tau) = \frac{a_0}{(1 + (\tau - \tau_w)^2 / Z_0^2)^{1/2}}$$

$$\phi(\tau) = -\tan^{-1}((\tau - \tau_w) / Z_0)$$



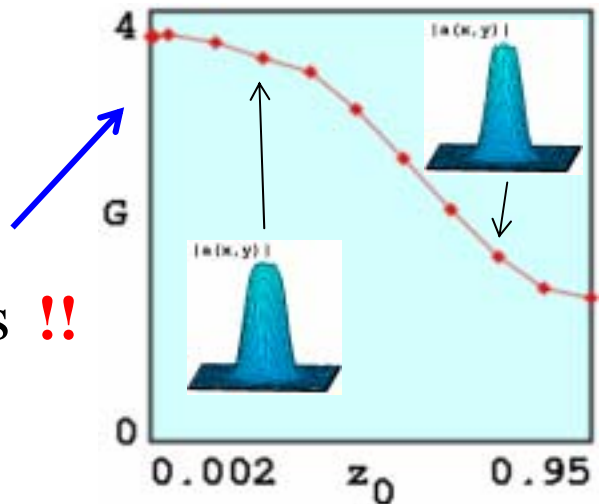
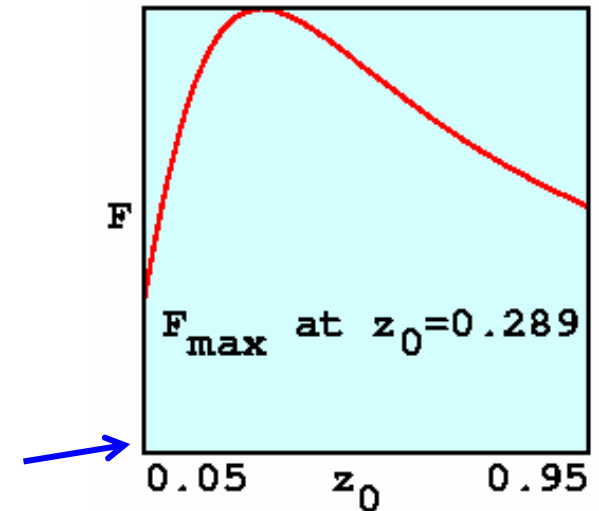
# Multimode FEL Simulations

- o Simulation follows:
  - o Many  $\perp$  modes
  - o Optical diffraction
  - o Betatron motion
  - o Energy spread
  - o Mirror vibration
  - o Beam alignment
  - o Self-consistent
  - o SVAP approx.
- o Note:
  - o mode shape
  - o mode in undulator
  - o mode at mirrors
  - o steady-state gain
- o See Poster: MOPOS65



# Vary Rayleigh Length

- Vary  $Z_0 = 2.6\text{cm}$  to  $Z_0 = 49\text{cm}$
- Normalized Rayleigh length  $z_0 = Z_0/L$
- Mode area at mirrors is  $A_{S/2} \propto 1/z_0$   
as desired to reduce mirror intensity
- Mode area at waist is  $A_0 \propto z_0$
- Mode area averaged over undulator is  
 $\langle A \rangle \propto [z_0 + 1/(12z_0)] \propto 1/F$  (above)
- Simple theory:  $G \propto F$  (filling factor)
- $G_{\text{max}}$  at  $z_0 = (12)^{-1/2}$  ;  $Z_0 = L/(12)^{1/2}$
- Simulation allows many optical modes:
  - Gain  $G$  increases for small  $z_0$  values !!
- **Small  $Z_0 \Rightarrow$  still good gain !!**
- **Can save mirrors with good gain !!**





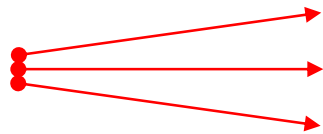
# Vary Electron Beam Focus

- Keep beam inside focused optical mode

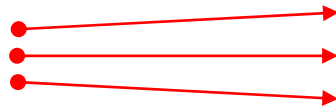
- Emittance  $\varepsilon_n = \gamma r_b \theta_b \approx 3 \text{ mm-mrad}$

- For large  $r_b$ , beam is outside mode

- For small beam focus  $r_b \Rightarrow \theta_b$  bigger



$r_b$  small,  $\theta_b$  big

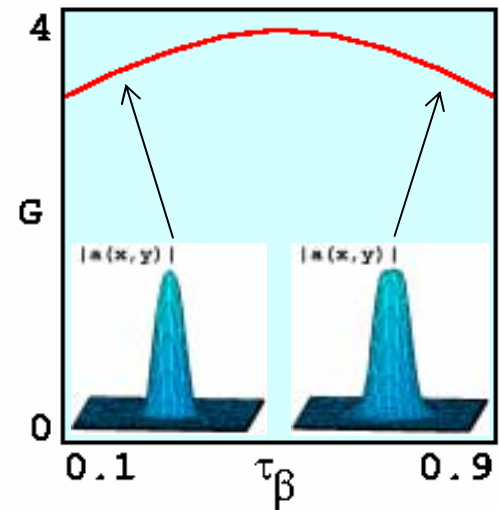
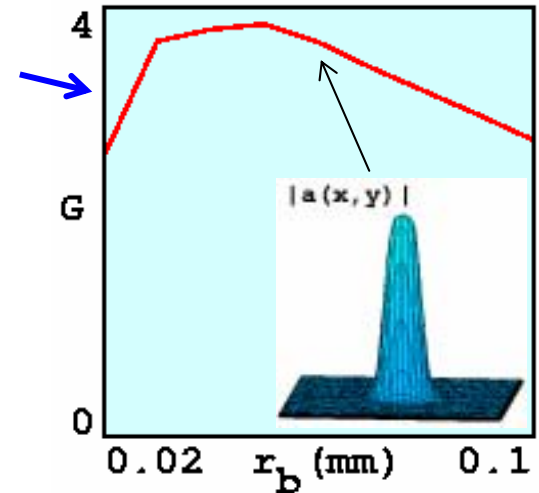


$r_b$  big,  $\theta_b$  small

- Electron beam focus optimum  
at middle of undulator  $\tau_\beta = 0.5$

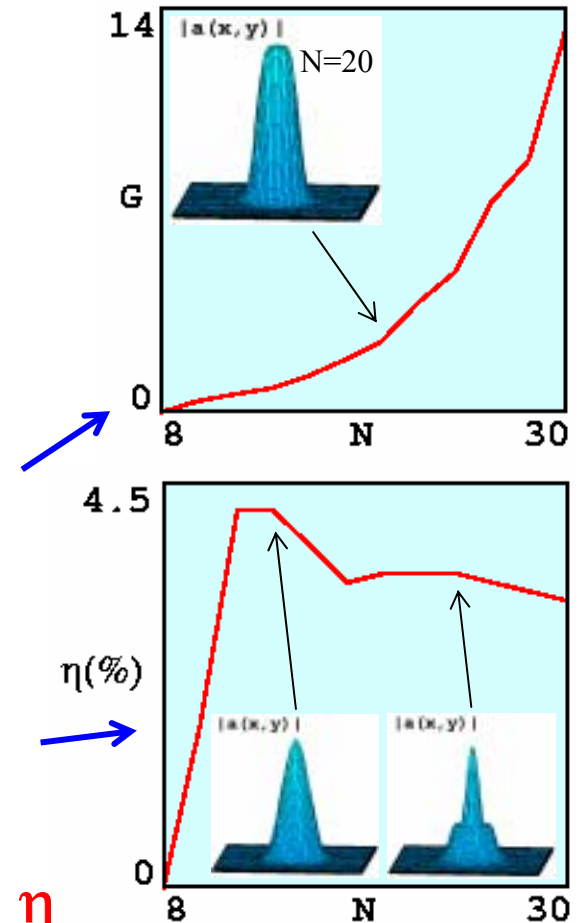
(with optical mode centered at  $\tau_w = 0.5$ )

- So, focus electron at optical mode waist !!



# Vary Undulator Length N

- Vary N from 8 to 30 periods
- Undulator period fixed at  $\lambda_o \approx 2.36\text{cm}$   
to give  $\lambda \approx 1\mu\text{m}$  optical wavelength
- Undulator gap is  $g \approx 1\text{cm}$
- Mode scraping not an issue for small N's
- $N > 8$  needed for  $G > 1/Q_n$ , “threshold”
- Gain increases rapidly with increasing N
- Extraction  $\eta \approx 4.3\%$  peaks at  $N \approx 12 - 14$
- Extraction decreases as  $\approx 1/2N$
- Use  $N = 22$  in design: **BIG Gain, good  $\eta$**
- See Poster: MOPOS66



# Short Rayleigh Length FELs

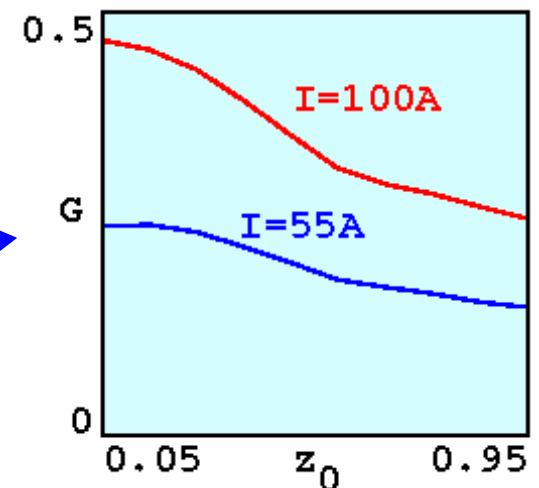
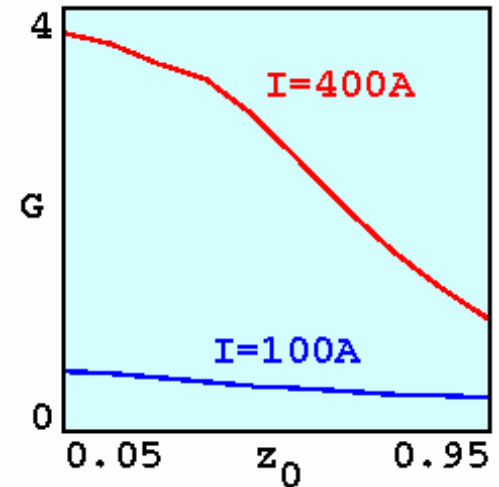


- Reduce peak current  $I = 400\text{A}$  to  $I = 100\text{A}$
- Still SRL is a better FEL design option !!

- **New example SRL FEL:**

- Same Undulator:  $N \approx 22$ ,  $L \approx 52\text{cm}$ ,  $K \approx 1$
- Resonator:  $S \approx 12\text{m}$ ,  $Z_0 \approx 6\text{cm}$ ,  $Q_n \approx 20$
- Same Optical wavelength:  $\lambda \approx 1\mu\text{m}$
- New Electron Beam:  $E_b \approx 80\text{MeV}$ ,  
 $\varepsilon_n \approx 10\text{mm-mrad}$  (typical emittance)  
 $r_b \approx 0.1\text{mm}$  (beam focal radius)  
 $I_{\text{peak}} \approx 100\text{A}$ , and  $I_{\text{peak}} \approx 55\text{A}$

- SRL gives better FEL gain in each case

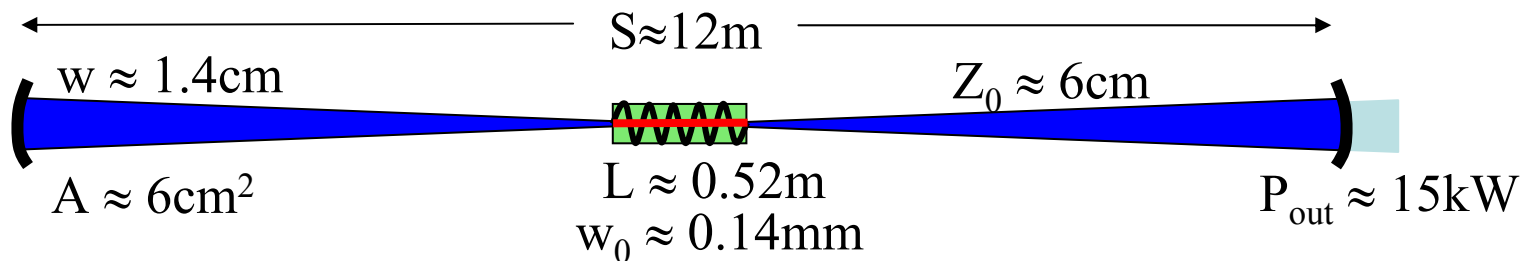


- **Appears that SRL FEL is just a better design !!**

# Conclusions: SRL Advantages & Issues



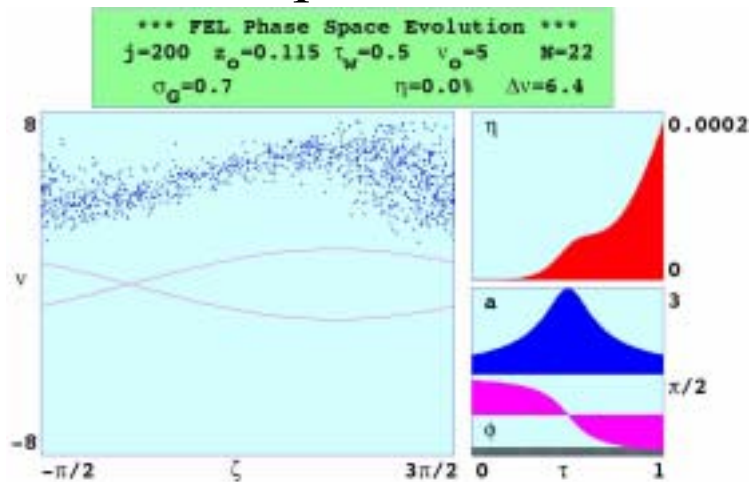
- Short Rayleigh Length (SRL) optical mode  $\Rightarrow$  2 advantages
  - reduces optical intensity on resonator mirrors at smaller S
  - single optical wavefront amplified  $\Rightarrow$  excellent beam quality
- Issues:** (See Poster: THPOS59)
- Electron Beam - Optical Mode Alignment is **delicate**:
  - Electron beam ( $r_b \approx 60\mu\text{m}$ )  $<$  optical mode ( $w_0 \approx 140\mu\text{m}$ )
  - But, FELs now hold beam to tolerance of  $0.1r_b \approx 6\mu\text{m}$  !!
- Optical Resonator Mirror Alignment is **delicate**:
  - Mirror must “aim” mode back to small waist  $\approx w_0$  over  $\approx S$
  - So, allowed mirror tilt  $\Delta\theta \approx w_0/S \approx$  a few  $\mu\text{radians}$
  - But, FELs now hold to  $\approx 0.1\mu\text{radians} \Rightarrow$  **Active Alignment !!**



# SRL FEL Phase Space

- Show phase space evolution for weak & strong fields
- Separatrix “balloons” to “pull down” bunched electrons
- Electron bunching mechanism is **NOT** conventional
- Note optical amplitude sharp focus and phase shift

weak optical fields



strong optical fields

