CSRtrack: Faster Calculation of 3d CSR Effects

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- Projected Method / Sub-Bunch Approach
- Field Calculation: Convolution Method

Pseudo Green's Function Approach

Meshed Fields

- Iterative Tracking
- CSRtrack
- Example



Projected Method

(1d approach)

$$\dot{\mathbf{p}}_{\nu} = q \left(\mathbf{e}_{\nu \parallel} E^{(\lambda)}(s_{\nu}, t) + \mathbf{v}_{\nu} \times \mathbf{B}^{(\text{ext})} \right)$$



very low numerical effort

no transverse self-forces

rigid 1d charge distribution:

$$\lambda^{(\delta)}(s-t_0c) = \sum q_v \delta((s-t_0c) - (s_v - s))$$

$$\lambda(s-t_0c) = \lambda^{(\delta)}(s-t_0c) \otimes (g(s/\sigma)/\sigma)$$

1d E-field without γ^{-2} singularity: $E^{(\lambda)}(s,t_0) = \int \lambda'(u+s-ct_0)K(s,u)du$

no transverse dependency of longitudinal forces

see: Saldin, Schneidmiller, Yurkov: NIM A398 (1997) 373-394 Dohlus: TESLA-FEL-2003-05

Sub-Bunch Approach



Iterative Tracking



Iterative Tracking



Convolution Method



see: M.Dohlus, A.Kabel, T.Limberg: Efficient field calculation of 3D bunches on general trajectories. NIM A445 (2000) 338-342

Pseudo Green's Function Approach



$$\mathbf{E}^{(\nu)}(\mathbf{r}, t_0) \approx \frac{q_{\nu}}{q_0} \mathbf{R} \cdot \mathbf{E}^{(0)} \left(\mathbf{r}_0(t_0) + \mathbf{R}^{-1} (\mathbf{r} - \mathbf{r}_{\nu}(t_0)), t_0 \right)$$
$$\mathbf{B}^{(\nu)}(\mathbf{r}, t_0) \approx \frac{q_{\nu}}{q_0} \mathbf{R} \cdot \mathbf{B}^{(0)} \left(\mathbf{r}_0(t_0) + \mathbf{R}^{-1} (\mathbf{r} - \mathbf{r}_{\nu}(t_0)), t_0 \right)$$

the "Green's functions" are calculated numerically on a 2d-mesh with $M_{\rm g}$ points

$$\mathbf{E}^{(0)} = E_x^{(0,t_0)}(x, y)\mathbf{u}_x + E_y^{(0,t_0)}(x, y)\mathbf{u}_y$$
$$\mathbf{B}^{(0)} = B_z^{(0,t_0)}(x, y)\mathbf{u}_z$$

effort per field calculation:

$$E_{f.c.} = M_g E_{p \text{ to } p} + NME_{i,g}$$

| $E_{\rm p to}$ | $p_p = effort per point to point interaction$ |
|----------------|---|
| $E_{i,g}$ | = effort for interpolation on grid $\leq E_{p \text{ to } p}$ |
| N | = number of source distributions |
| M | = number of test particles (> N) |



Meshed EM Fields

density of particles large compared to fine structure of field: calculate field on mesh (M_{em} points) and interpolate to M test-particles effort: $E_{f.c.} = M_{em}NE_{p \text{ to } p} + ME_{i,em}$ (~ linear with particles)

EM-field macro-distribution

Meshed EM Fields + Pseudo Green's ...

effort:
$$E_{\text{f.c.}} = M_{\text{g}}E_{\text{p to p}} + M_{\text{em}}NE_{\text{i,g}} + ME_{\text{i,em}}$$





Scaling of Effort

(simplified)





Example: BC2-TTF1

overcompression initial distribution from ASTRA (200000 particles) $\gamma_0 = 266.6 \quad q_{tot} = 2.61 \, \text{nC}$

0.004 top view x_n slice 5.10-4 0.002 0 0 -0.002-5.10-4 -0.004-0.002-0.001Ο 0.001 0.002 0.002 -0.006-0.004-0.0020 0.004 0.006 0.008 0.01 xı s_n

 \rightarrow 41000 sub-bunches (CSRtrack)

Example: BC2-TTF1



Example: double BC



Example: double BC

