

Format of the session

on lattice optimisation for stochastic cooling

**5 short (5 min.) “warm up talks”,
40 min. of general discussion**

D. Möhl : Introduction

J. Wei: Lattices for collection and cooling

Y. Senichev: Lattices for COSY and HESR

A. Dolinskii: Collector and Accumulator for FAIR

V. Nagaslaev: Fermilab Antiproton Accumulator

ALL : Discussion

Introduction to the session on lattice optimisation for stochastic cooling

D. Möhl

A ‘split ring’... why?

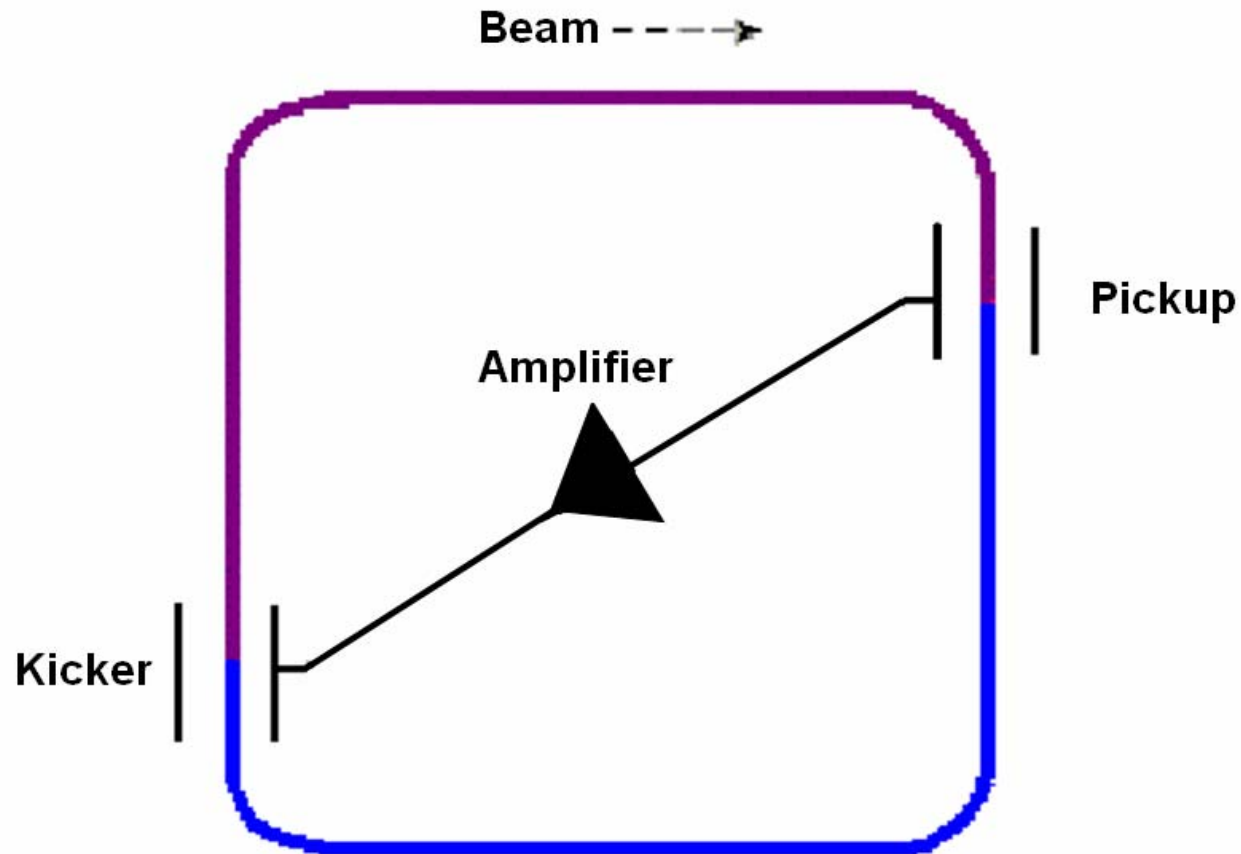
Gain to be expected.

A ‘split ring’...how?

Price to be paid.

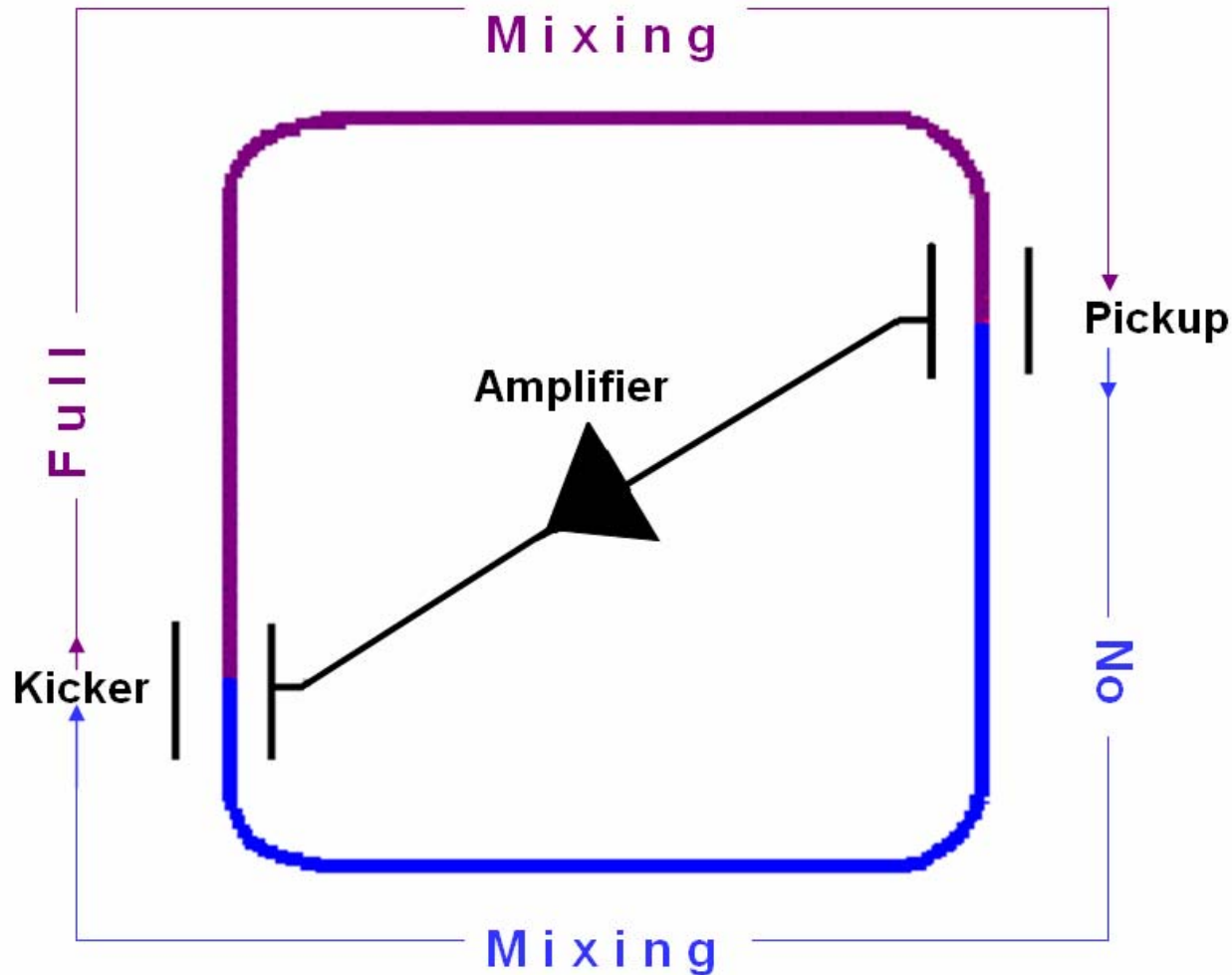


The mixing dilemma



No mixing desired PU to kicker, full mixing desired kicker to PU.

The mixing dilemma



This requires a 'split ring' with different properties in the **blue** and **red** part



Advantages

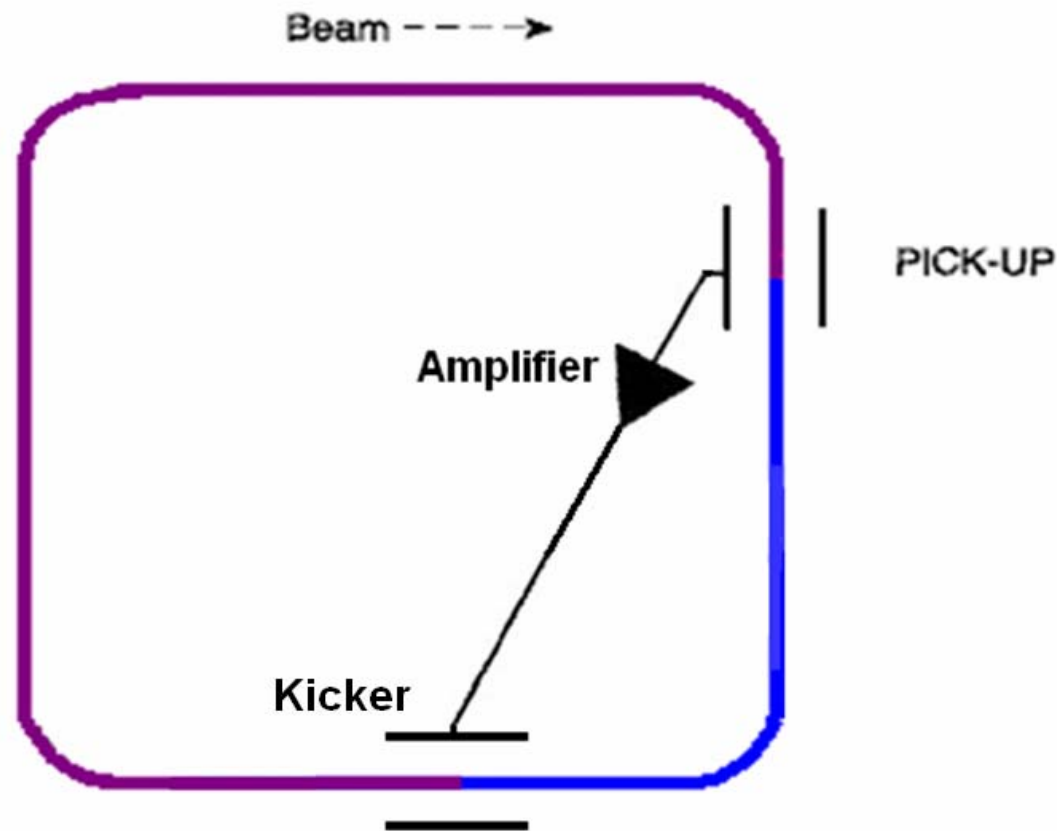
**The potential gain with an ‘optimum mixing lattice’ is:
-- a factor of three to six in cooling speed --**

This concerns transverse cooling and longitudinal cooling by the Palmer and local time of flight methods but not the filter method.

**It assumes a diagonal cooling path and negligible system noise
For a distance PU to K shorter than K to PU and also with poor
signal to noise ratio, the gain is less pronounced.**



Shorter path PU to kicker



For a distance PU to K shorter than K to PU and also with poor signal to noise ratio, the gain is less pronounced.



Lattice Design

The optimum mixing lattice can be built from Flexible Momentum Compaction ('FMC') modules.

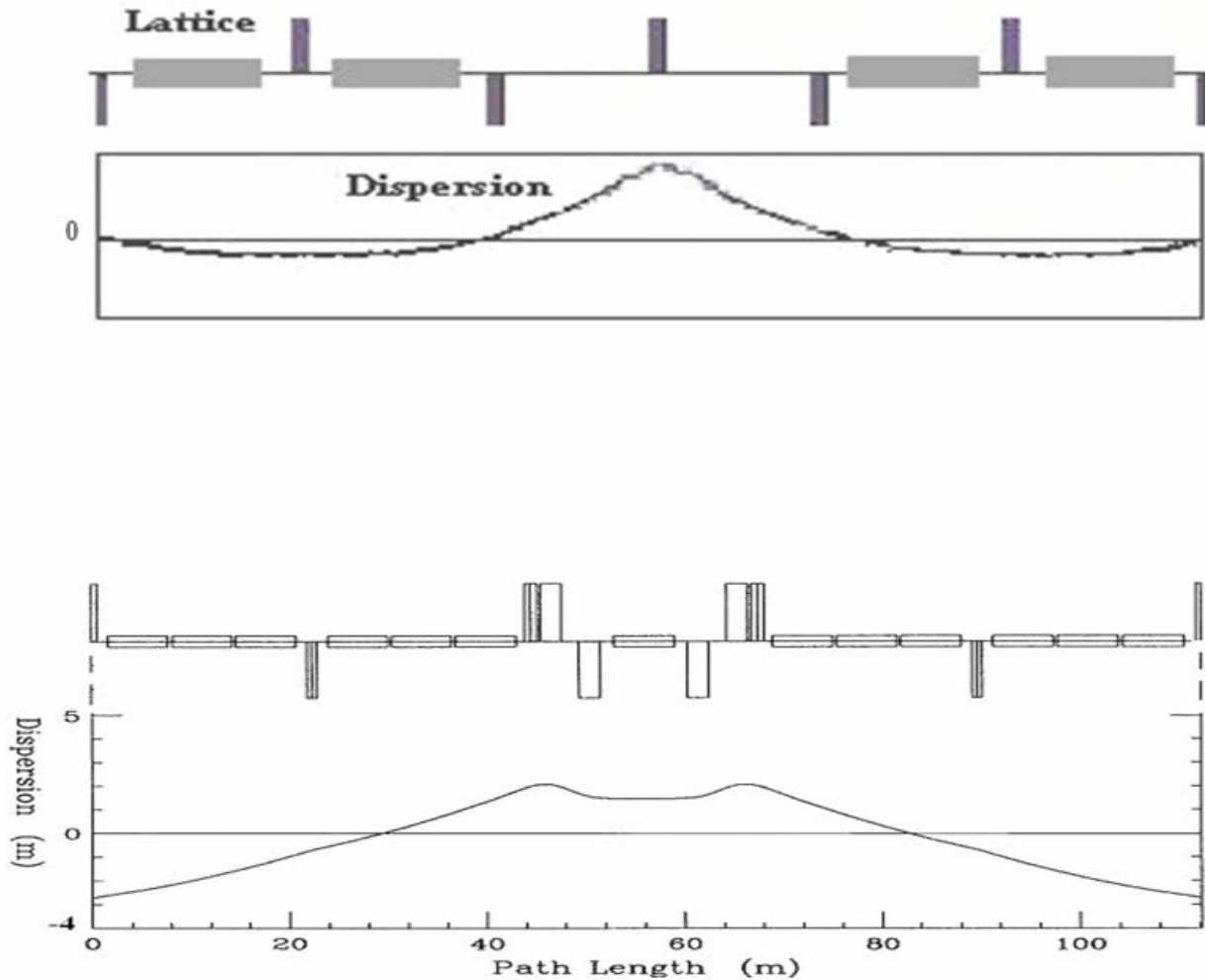
A long list of references exists concerning the design of ('FMC') modules suited for this purpose.

The low mixing section (PU to kicker) needs low momentum compaction modules ($\alpha_p = \gamma^{-2} \rightarrow \eta = 0$).

The strong mixing section (**kicker to PU**) needs large momentum compaction modules (preferably negative α_p)
 $\rightarrow \eta$ large.



Examples of FMC modules



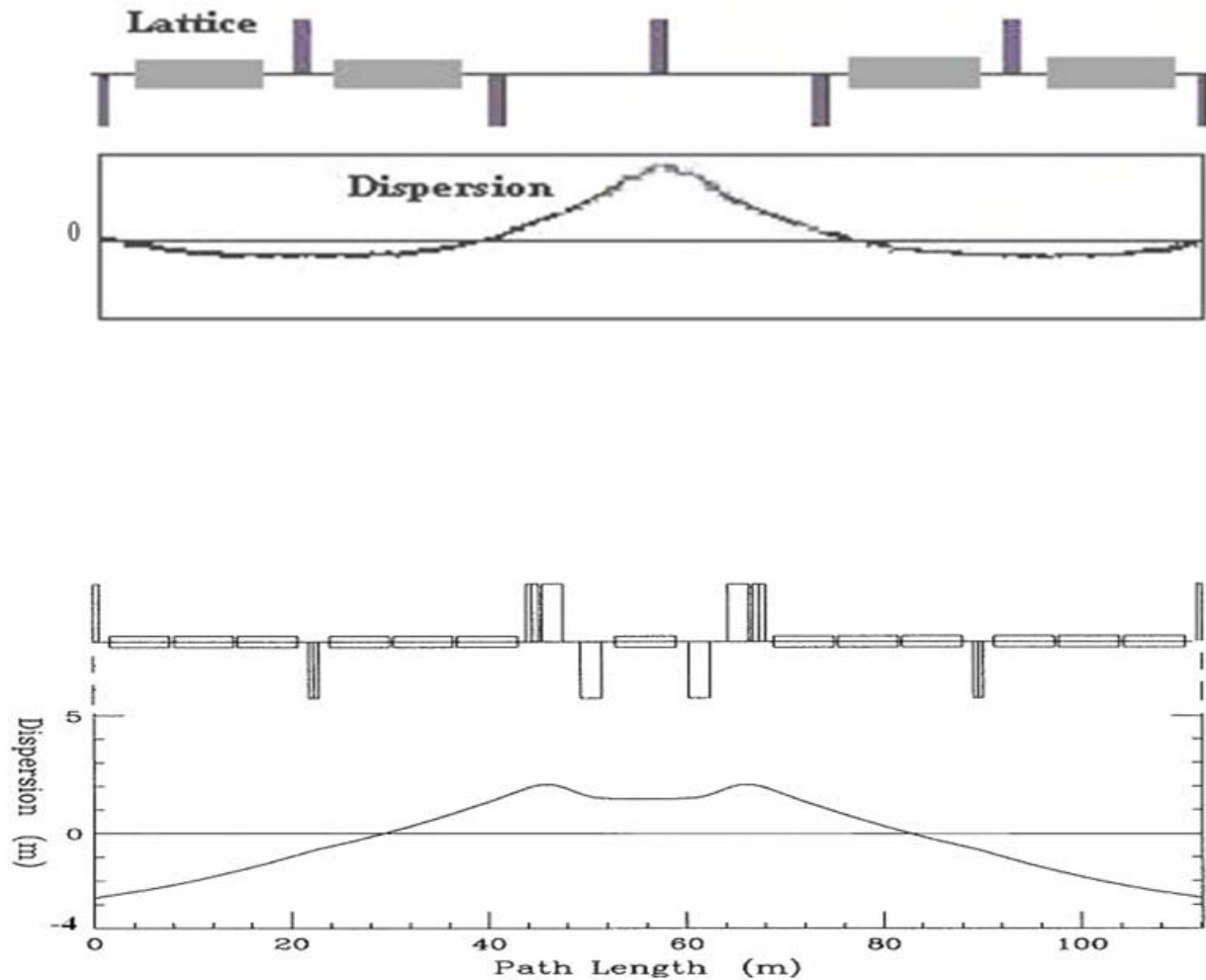
Disadvantages

The optimum mixing lattice is more complex and more expensive than a simple FODO structure

- Needs more quadrupoles and esp. more quad. families
- The simple structure has reduced acceptance (increased maxima of lattice functions)
- Periodicity 1 \rightarrow many systematic resonances
- Many pieces of straight section and low betas at places where one cannot always use them
- Influence of η_{ring} on RF quantities ($U \propto \eta \dots$)



More quadrupoles for the FMC modules



Features that turn out to be of no great disadvantage

Collective instabilities and dynamic aperture do not seem to be of special concern

The η entering into the ‘Keil-Schnell-Boussard’ criterion

is the ‘full turn’ $\eta_{ring} = \frac{L_{pk}}{C} \eta_{pk} + \frac{L_{kp}}{C} \eta_{kp}$. For large η_{kp} this, and hence the tolerable impedances, are large

S.Y. Lee et al. conclude, that the dynamical aperture in the advanced FMC-modules can be at least as large as that of regular FODO cells



Conclusion

- 1. The potential gain with an ‘optimum mixing lattice’ is a factor of three to six in cooling speed.**
- 2. The optimum mixing lattice can be built from Flexible Momentum Compaction (‘FMC’) modules.**
- 3. The optimum mixing lattice is more complex and more expensive than a simple FODO structure.**

Test in COSY???



Some simple relations

$$\frac{\Delta T_{1,2}}{T_{1,2}} = \eta_{1,2} \frac{\Delta p}{p}$$

Time of flight spread
point '1' to '2'

$$\eta_{1,2} = \alpha_{1,2} - 1/\gamma^2$$

Local 'off momentum
factor'

$$\alpha_{1,2} = \frac{1}{L_{1,2}} \int_{'1'}^{'2'} \frac{D}{\rho} ds$$

Local momentum
compaction factor

$$\eta_{ring} = \frac{L_{pk}}{C} \eta_{pk} + \frac{L_{kp}}{C} \eta_{kp}$$

Addition theorem

