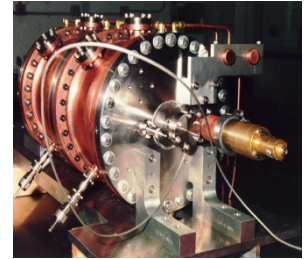
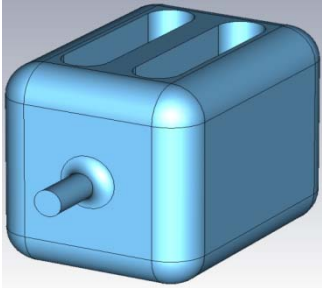


# Beam Dynamics Studies of Parallel-bar Deflecting Cavities



**S. Ahmed<sup>1</sup>, G. Krafft<sup>1,2</sup>, K. Deitrick<sup>3</sup>, S. De Silva<sup>1,2</sup>, J. Delayen<sup>1,2</sup>,  
M. Spata<sup>1</sup>, M. Tiefenback<sup>1</sup>, A. Hofler<sup>1</sup>, K. Beard<sup>4</sup>**

**<sup>1</sup>Thomas Jefferson National Accelerator Facility, Newport News, VA, USA**

**<sup>2</sup>Center for Accelerator Science, Old Dominion University, Norfolk, USA**

**<sup>3</sup>Rensselaer Polytechnic Institute, Troy, NY, USA**

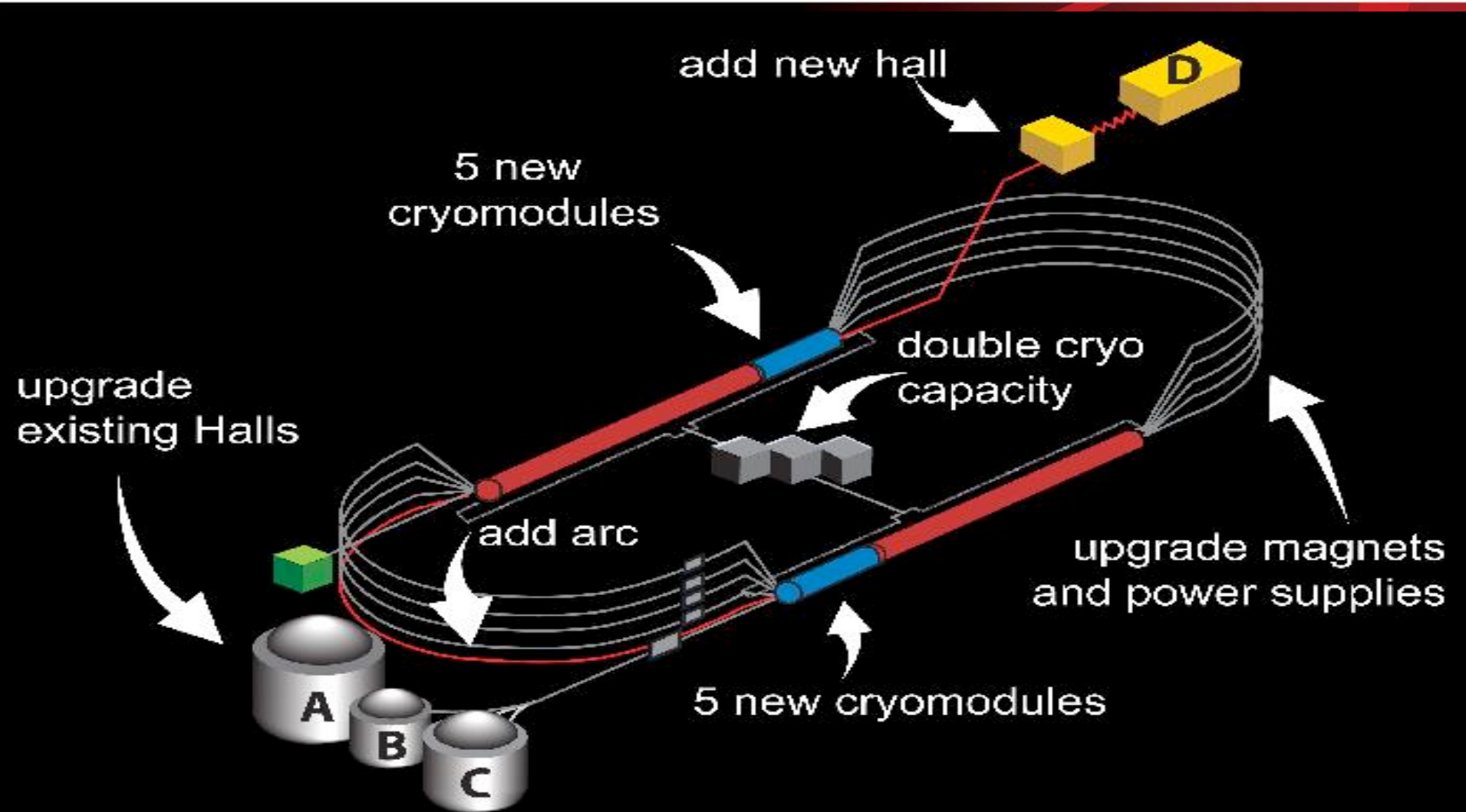
**<sup>4</sup>Muons, Inc., Batavia, IL, USA**

**Particle Accelerator Conference, NY, USA, Mar. 28 – Apr. 01, 2011**

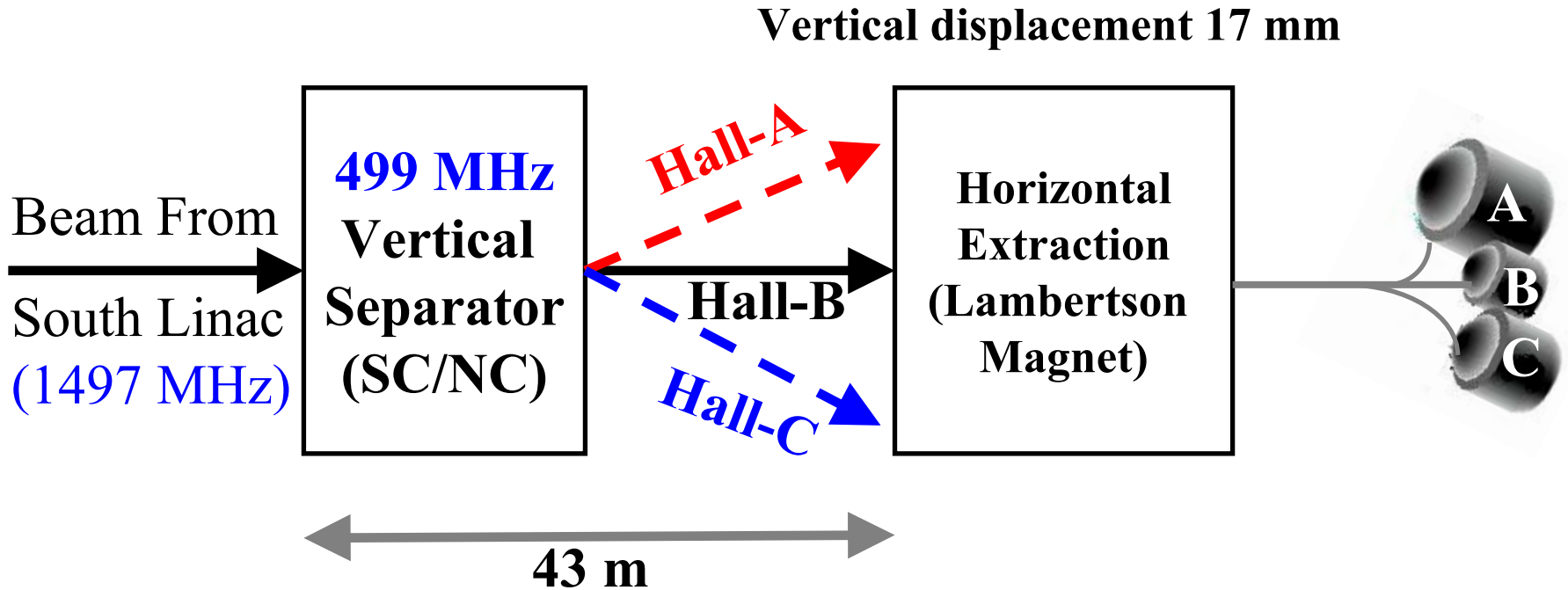
# Layout of Presentation

- ❖ Brief Overview of 12 GeV Upgrade related to 11 GeV RF separation
- ❖ Motivation
- ❖ Superconducting Structure
- ❖ NC Cavity Arrangements
- ❖ Comparison Between NC and SC Structures
- ❖ Summary

# Accelerator Schematic with 12 GeV Upgrade Options



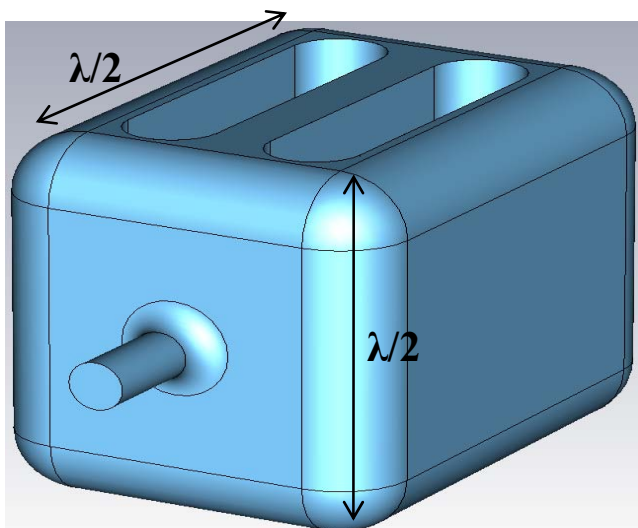
# Schematic of Separation Plus Extraction System



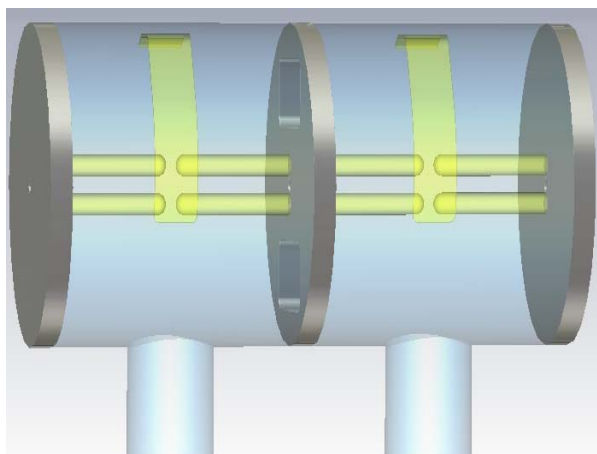
## Noteworthy Points:

- ❖ Utilize existing horizontal extraction magnet (Lambertson)
- ❖ Vertical separation followed by horizontal extraction
- ❖ 17 mm vertical displacement at entrance of extraction magnet

# Deflecting Cavities – NC & SC



Superconducting (SC)



Normal Conducting (NC)

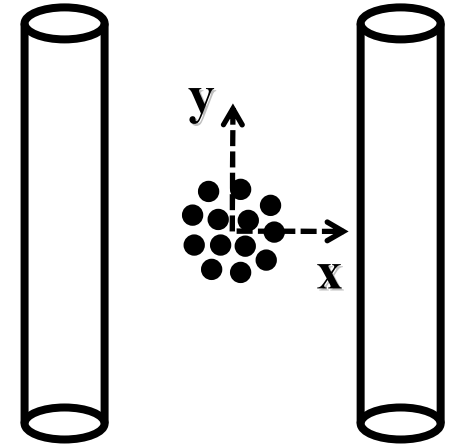
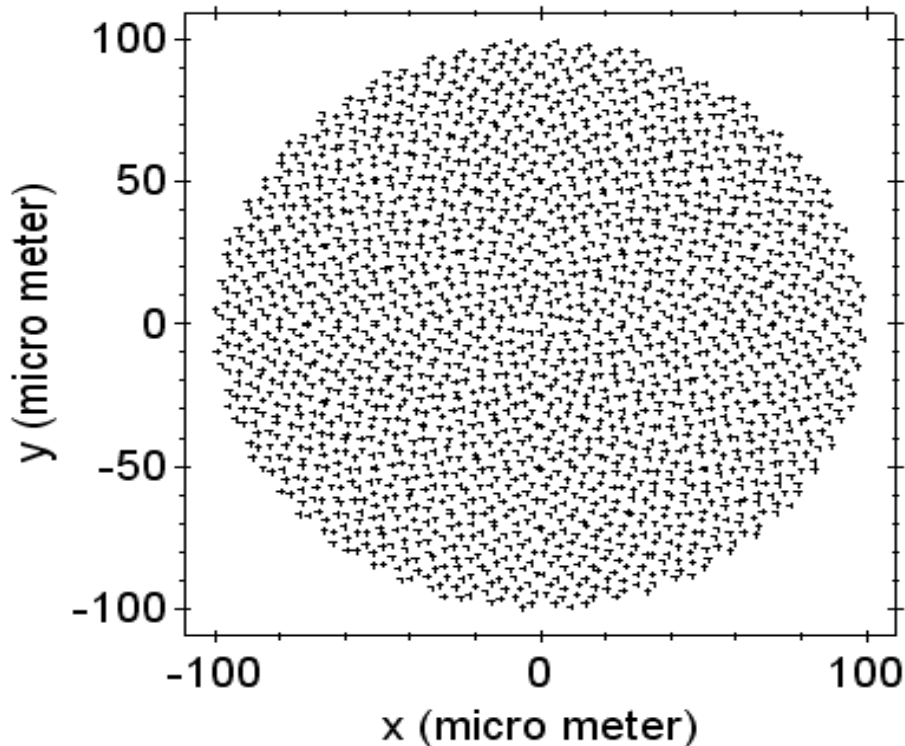
| Parameter                   | SC     | NC    | Unit     |
|-----------------------------|--------|-------|----------|
| Frequency of $\pi$ mode     | 499.2  | 499   | MHz      |
| $\lambda/2$ of $\pi$ mode   | 300.4  | 300.4 | mm       |
| Cavity length               | 394.4  | 300   | mm       |
| Bars width                  | 67     | 20    | mm       |
| Bars length                 | 284    | 135   | mm       |
| Aperture diameter           | 40.0   | 15    | mm       |
| $V_{\text{def}}^*$          | 0.3    | 0.3   | MV       |
| $E_p^*$                     | 1.85   | 3.39  | MV/m     |
| $B_p^*$                     | 6.69   | 8.87  | mT       |
| $G = QR_s$                  | 67.96  | 34.9  | $\Omega$ |
| $[R/Q]_T$                   | 933.98 | 24921 | $\Omega$ |
| At $E_T^* = 1 \text{ MV/m}$ |        |       |          |

# Why Need Simulations ?

- ❖ Two different deflecting cavities : normal conducting (exists for 6 GeV CEBAF operation) and superconducting (design available)
- ❖ No beam dynamics predictions available for 11 GeV separation
- ❖ Require one/two SC but six/eight NC structures
  - ☞ Aperture diameter : 40 mm for SC and ~ 15 mm for NC
  - ☞ Beam stay clear condition requires 6.5 mm from either wall (SC is OK but NC may not enough)
  - ☞ Alignment tolerance for NC arrangement
  - ☞ Emittance dilution needs to know

# Beam Dynamics : Simulation Schematic

- Particle : 1000 electron ( $m_e = 5.11 \times 10^{-4}$  GeV),  $Q = 1$  pC
- $E : 11$  GeV ,  $p = \sqrt{E^2 - m_e^2} \sim 11$  GeV/c
- $\beta = E / p \sim 1$  ,  $\gamma = E / m \sim 2.15264 \times 10^4$

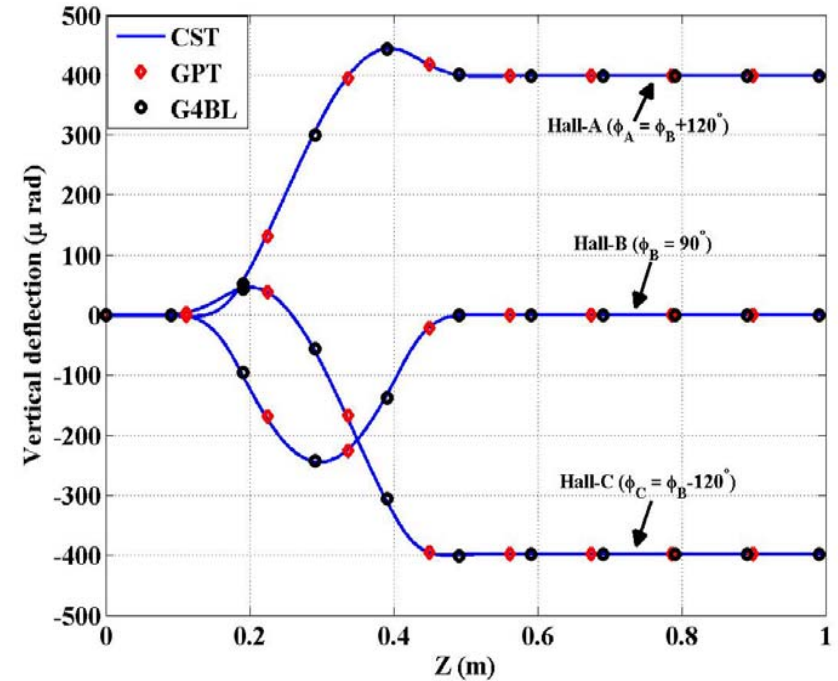
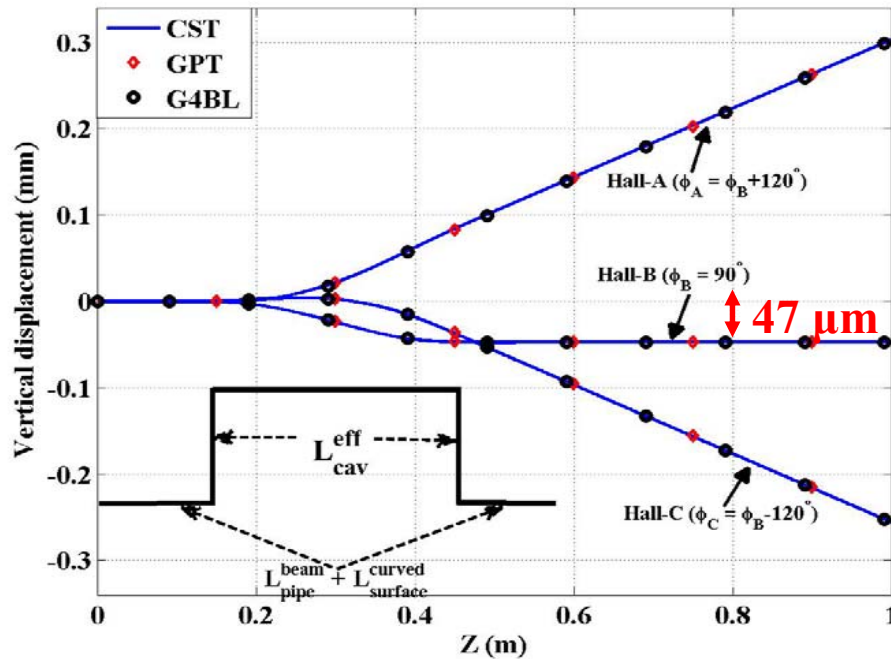


Distribution : uniform  
Initial Emittance : zero

First discussion for SC structure  
followed by comparison with NC



# Transverse Displacement & Deflection



$$x'_f = x'_0 + \frac{q_e V_{\text{def}}}{E_b} \cos \phi$$

$$x_f = x_0 + \frac{L}{2} (x'_0 + x'_f) + \frac{q_e V_{\text{def}}}{k E_b} \sin \phi$$

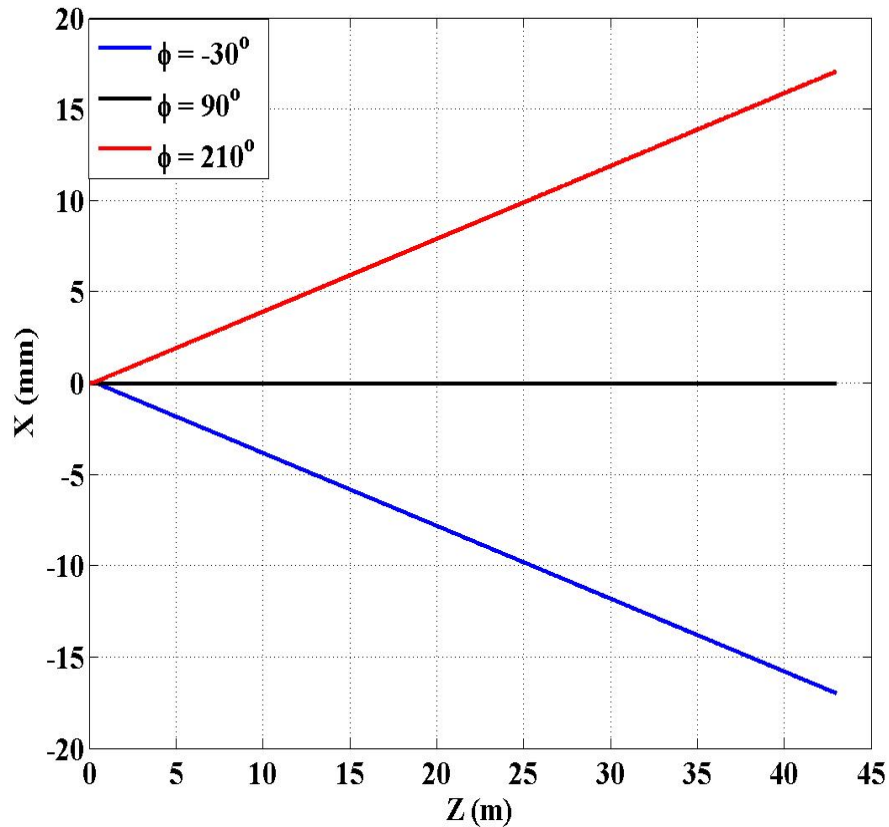
Angle has cosine function

Displacement has sine function

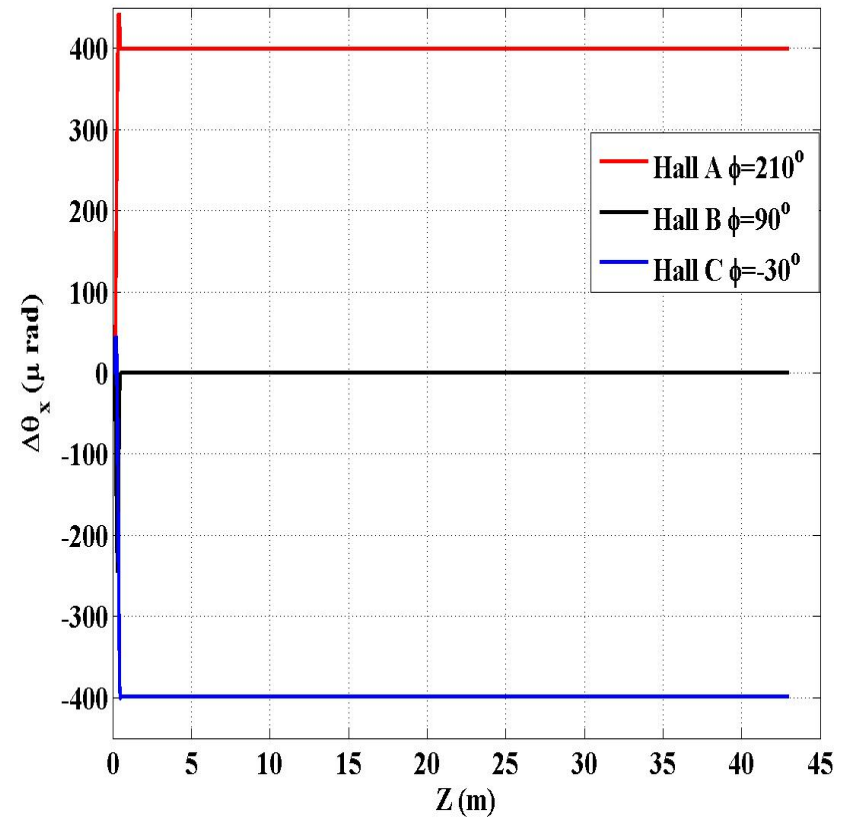


# Displacement & Deflection @ Lambertson Magnet

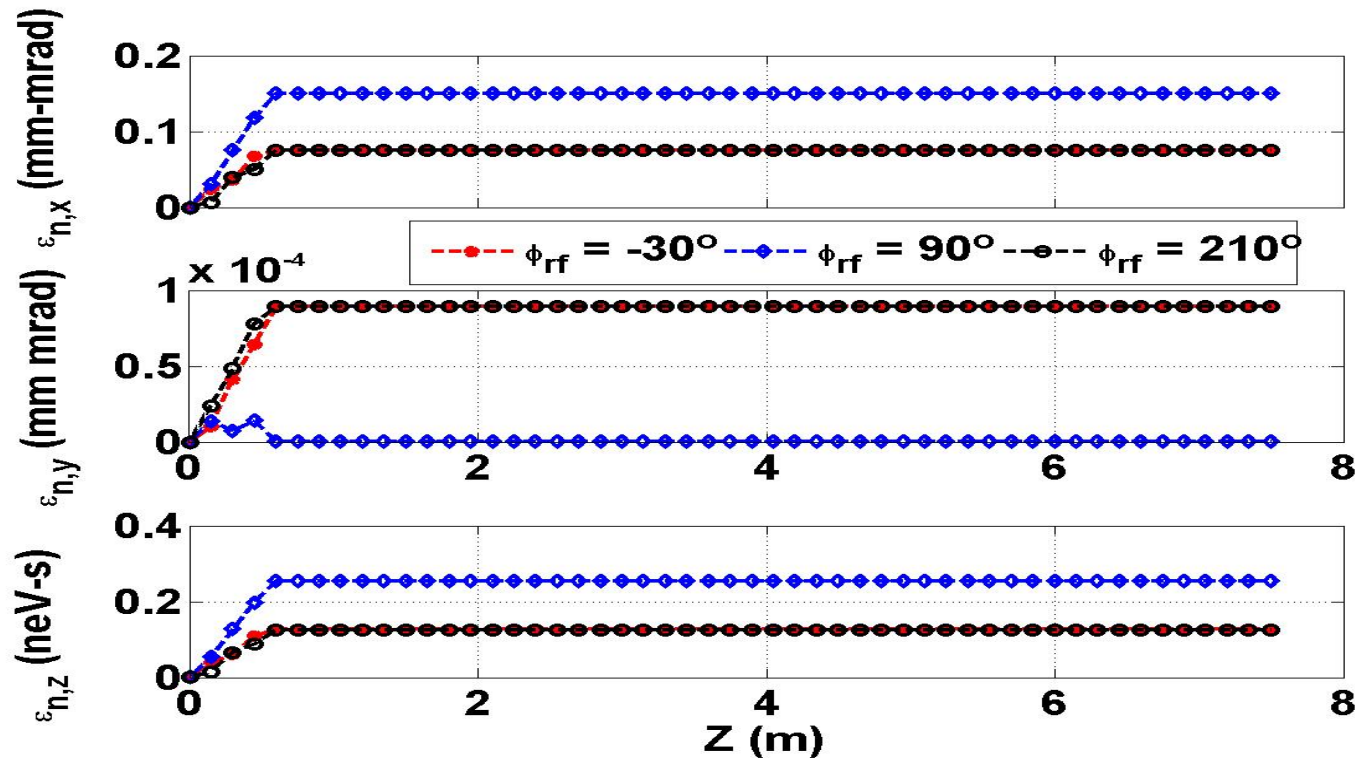
## Displacement



## Deflection



# Normalized RMS Emittance

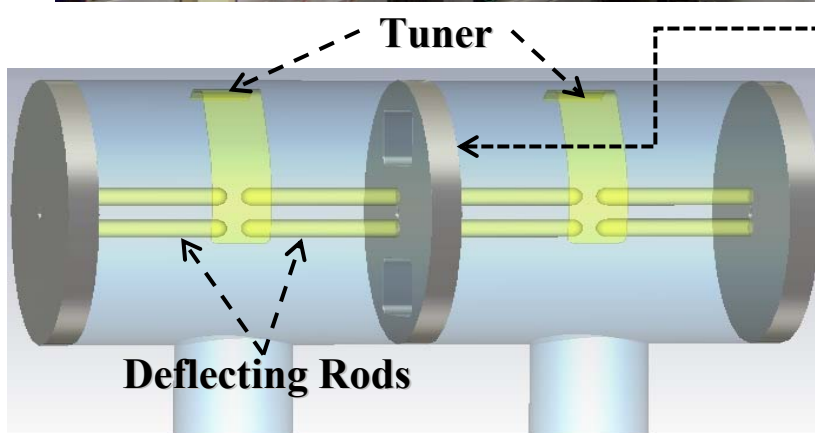
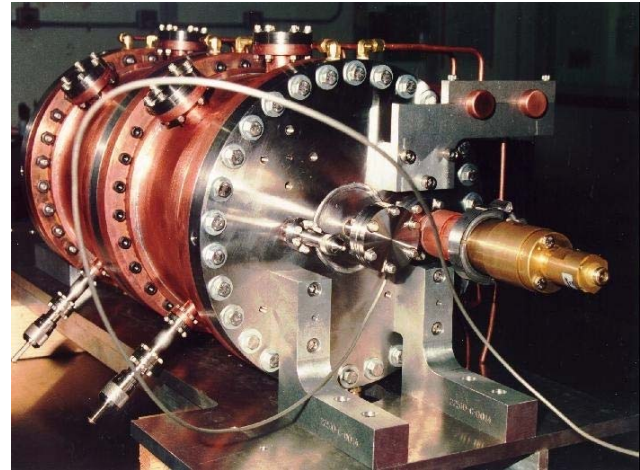
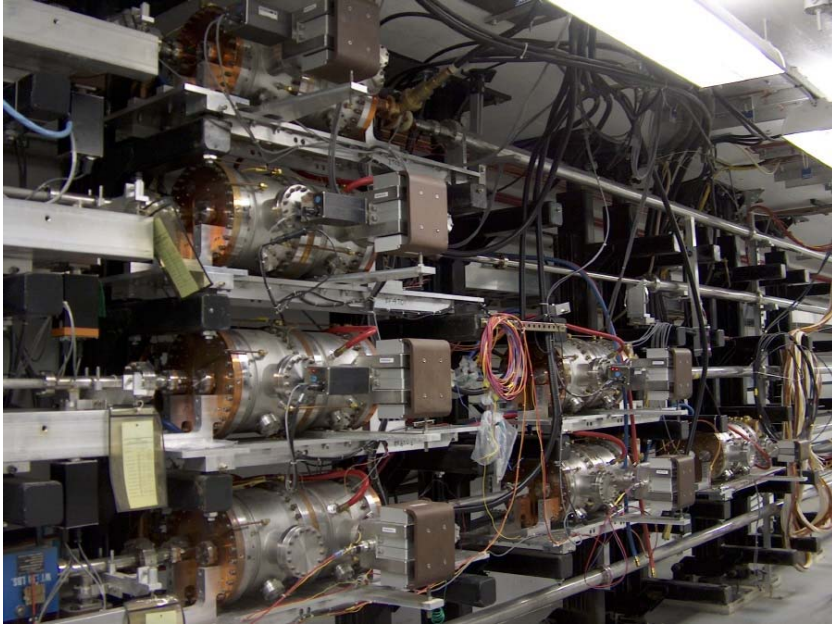


For uniform distribution corresponding to  $\varphi = \varphi_{ref}$ :

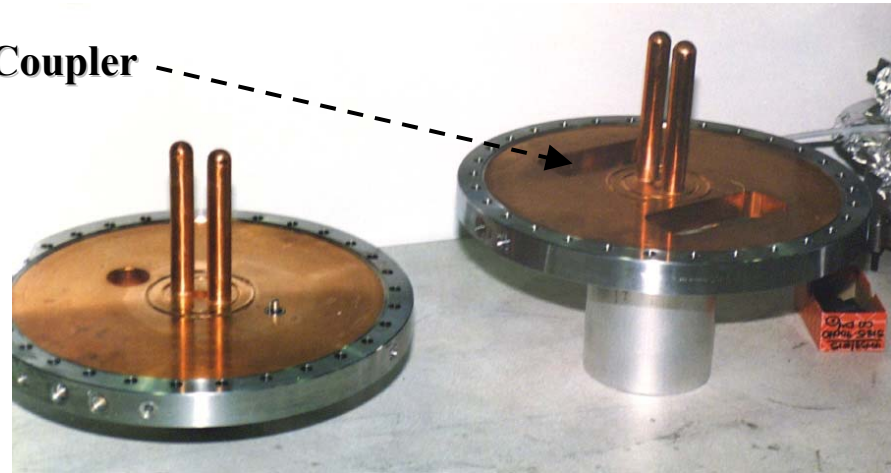
$$\epsilon_{n,rms} = \frac{q_e V_{def}}{4\sqrt{3}m_e c^2} k r_b l_b = 0.15 \text{ mm-mrad} \text{ agrees with simulation}$$

$$\epsilon_{n,rms}^{def} = 0.5 \times \epsilon_{n,rms}^{ref} ; \text{ as deflecting gradient is half.}$$

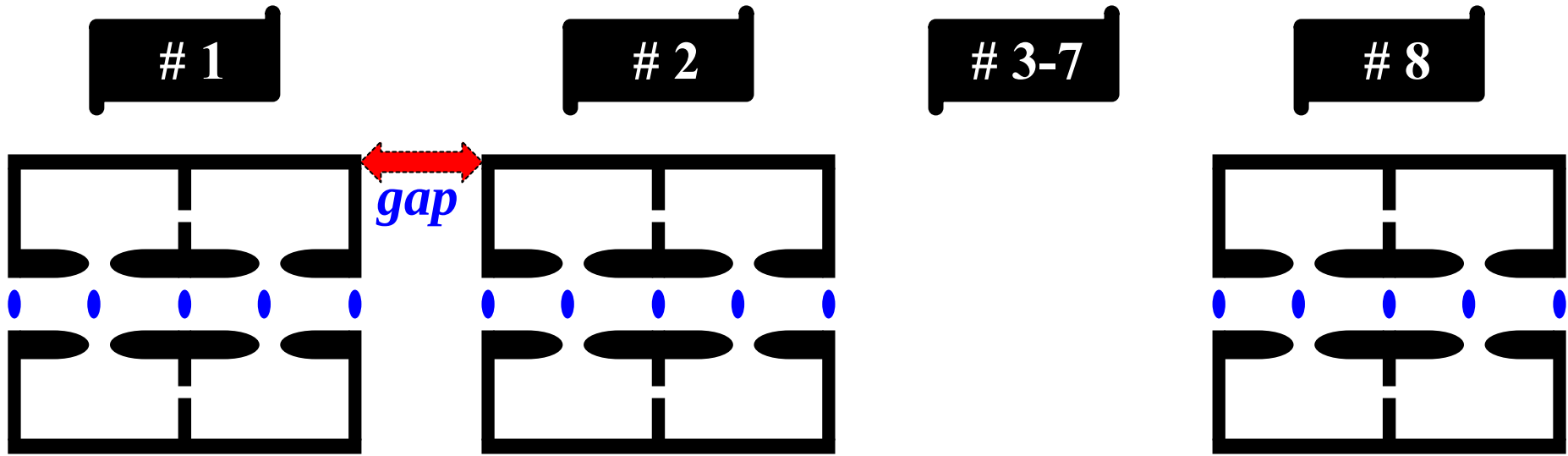
# Normal Conducting Cavity



EM Coupler



# 8-Cavity Arrangement



Cavity Length = **601.2 mm** @  $f = 499 \text{ MHz}$  ,  $c = 3 \times 10^8 \text{ m/s}$

Gap = **130.06 mm**

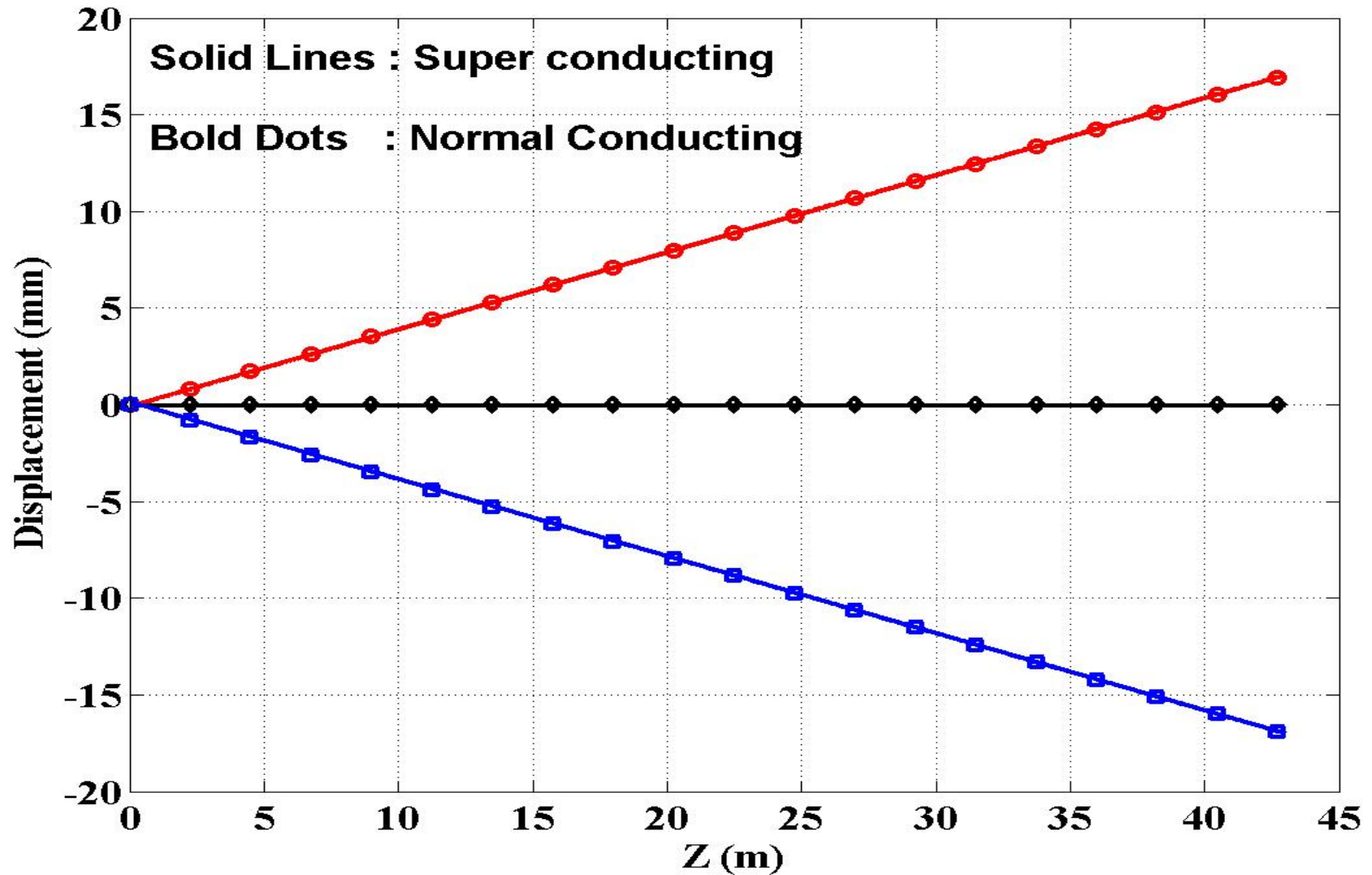
Center-to-center distance = **731.26 mm**

Time-Delay =  $(731.26 \times 10^{-3}) / (3 \times 10^8) =$  **2.44 ns**

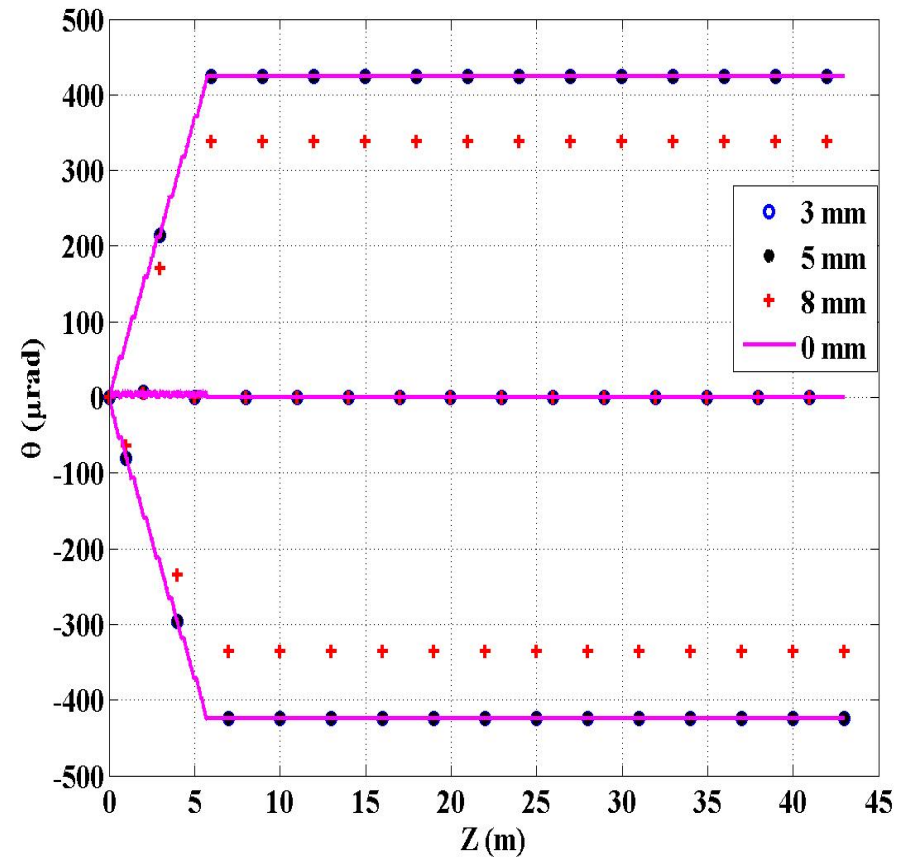
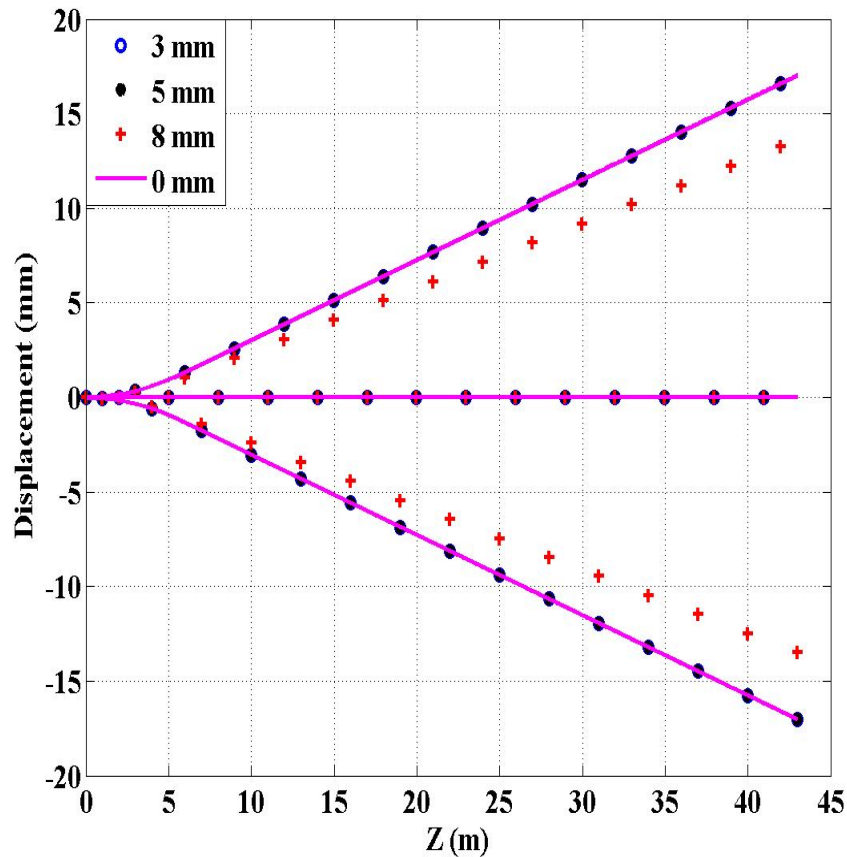
Phase Delay =  $2\pi f \times \text{Time-Delay} =$  **437.88 deg**



# NC Versus SC



# Mechanical Vibration : Displacement & Deflection



# Conclusion

- One/two SC or an array of NC structures can be used to provide required vertical displacement
- Emittance dilution is small
- Array of NC cavities demonstrated stability against mechanical vibration
- Both SC and NC structures are suitable for 11 GeV separation in 12 GeV upgrade of CEBAF