

Lattice design for the future ERL-based electron hadron colliders eRHIC and LHeC

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eRHIC and LHeC lattice design

Basic characteristics electron-hadron colliders LHeC and eRHIC

Lattice concept for $M_{5,6} = 0$

LHeC

eRHIC

LAYOUT

Achromatic &
basic cells

Splitters/
Combiners

Bypass/IR

LAYOUT

Achromatic &
basic cells

Splitters/
Combiners

Bypass/IR

LHeC

Electron Energy [GeV]	60
Luminosity [$\text{cm}^{-2} \text{s}^{-1}$]	1×10^{33}
Electron bunch length [μm]	300
Bunch interval [nm]	50
Transverse emittance $\gamma\epsilon_{x,y}$ [μmrad]	50
<i>rms</i> beam size [μm]	7
Repetition rate	CW
Total wall power [MW]	100

eRHIC - $\beta^* = 5$ cm

	Protons	Electrons
Maximum energy [GeV]	325	30
# of bunches/bunch freq [MHz]	166	14.08
Bunch intensity	2×10^{11}	0.2×10^{11}
Bunch charge [nC]	32	3.5
Beam current [mA]	415	50
Transverse norm. emittan. [μmrad]	0.18	20
<i>rms</i> beam size [nm]	0.52	0.52
Polarization	70	80
Luminosity @ 25 GeV [$\text{cm}^{-2} \text{s}^{-1}$]	1.5×10^{34}	

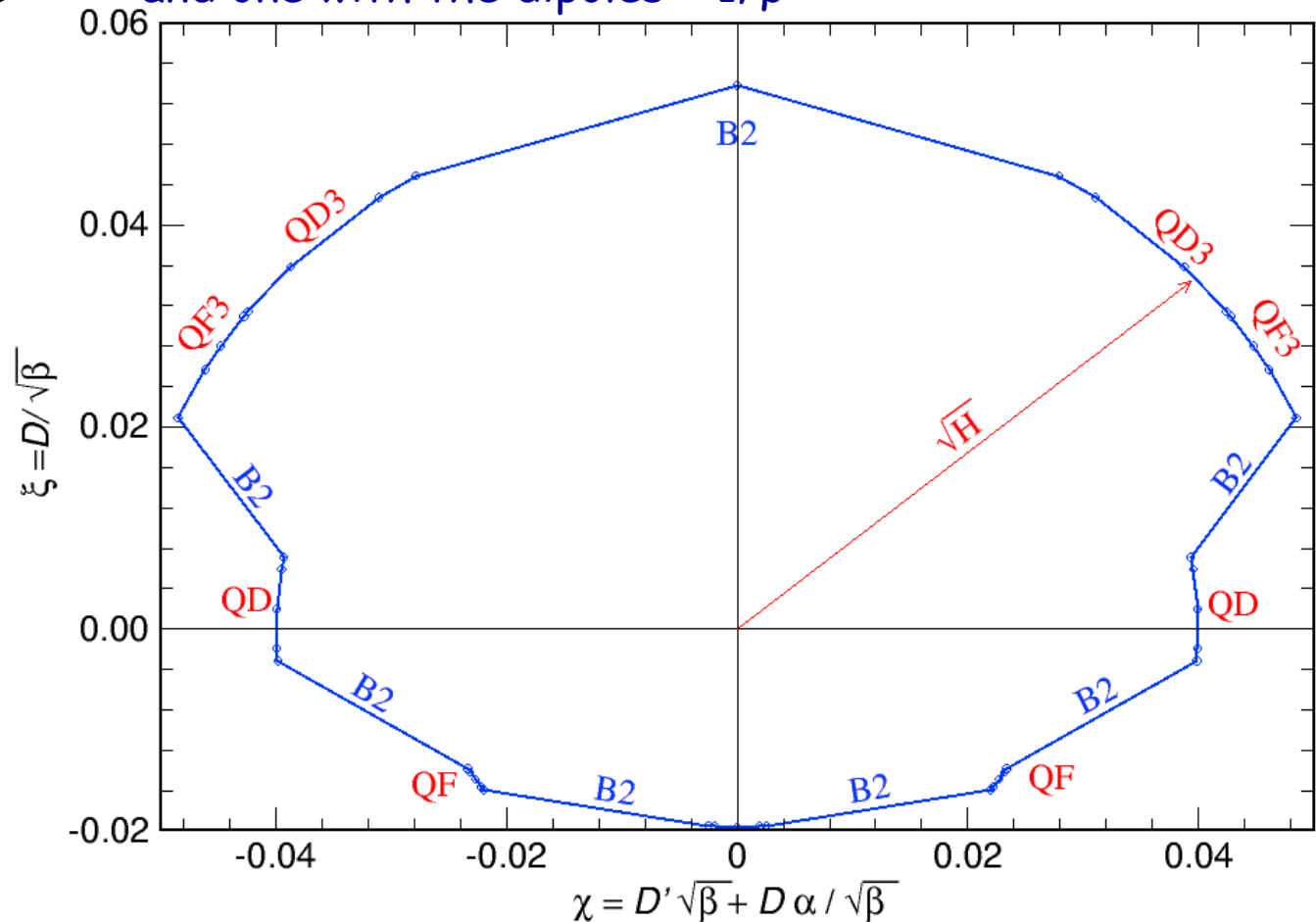
Basic concept of the adjustable momentum compaction lattice $M_{5,6} = 0$

$$D'' + kD = \begin{cases} = 0 \\ \neq 0 = 1/\rho \end{cases}$$

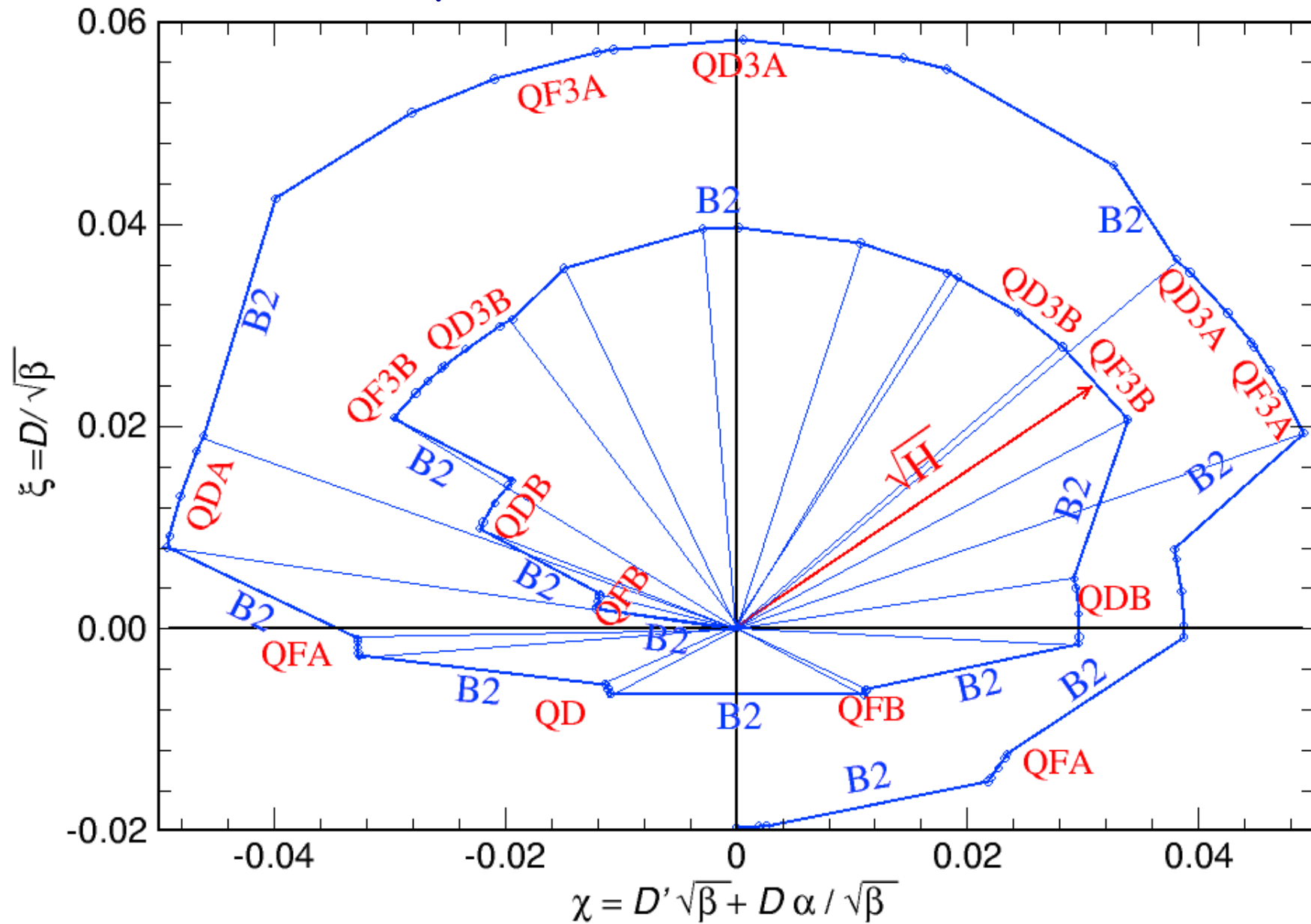
$$\chi = D'\sqrt{\beta} + D\frac{\alpha}{\sqrt{\beta}}$$

$$\xi = \frac{D}{\sqrt{\beta}}$$

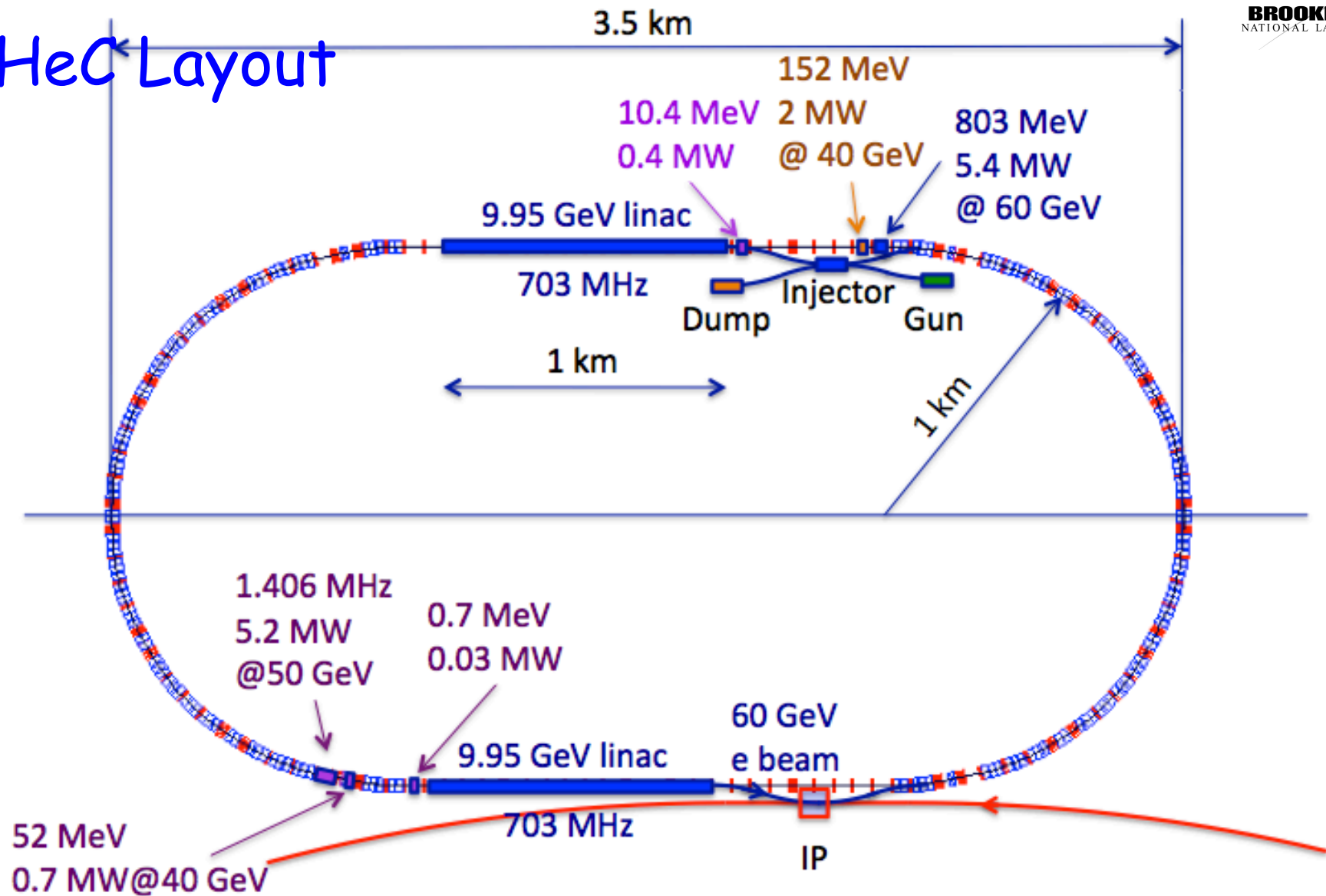
The homogeneous equation of the dispersion function D has two solutions: one without dipoles present ($=0$) and one with the dipoles $= 1/\rho$

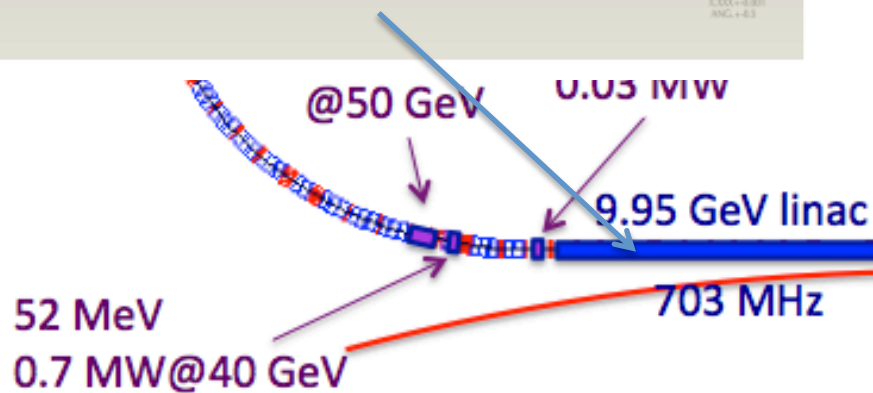
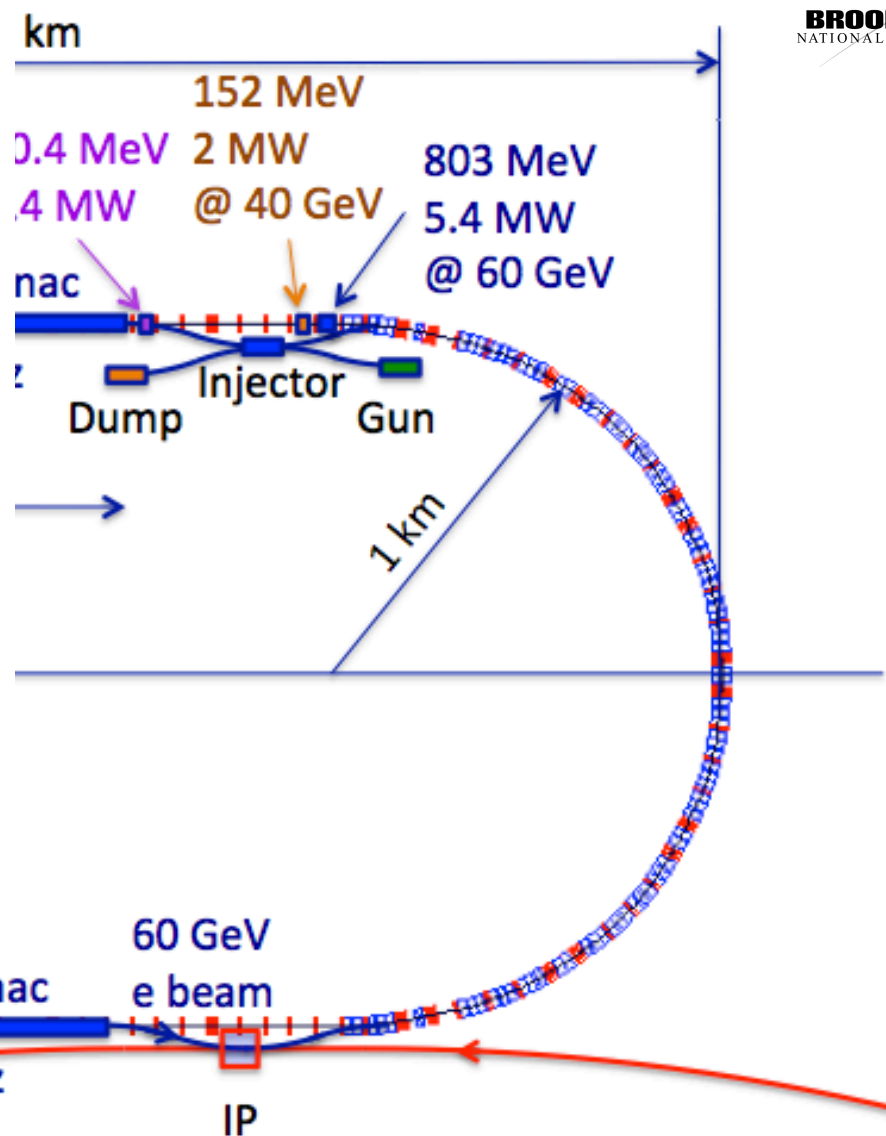
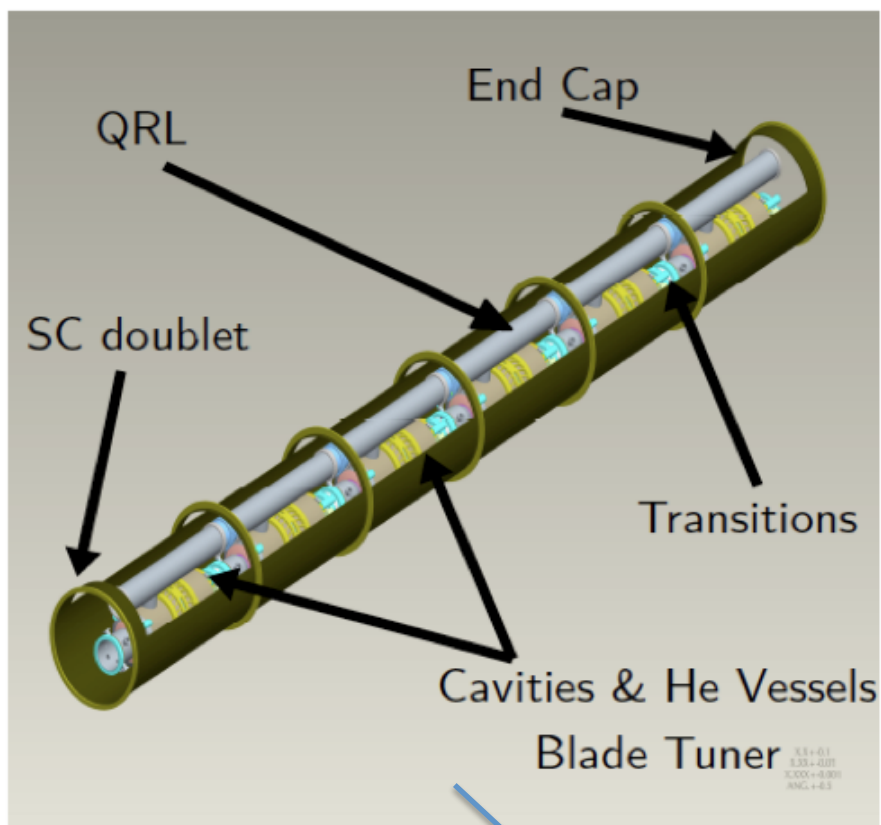


Normalized dispersion in the achromatic cells

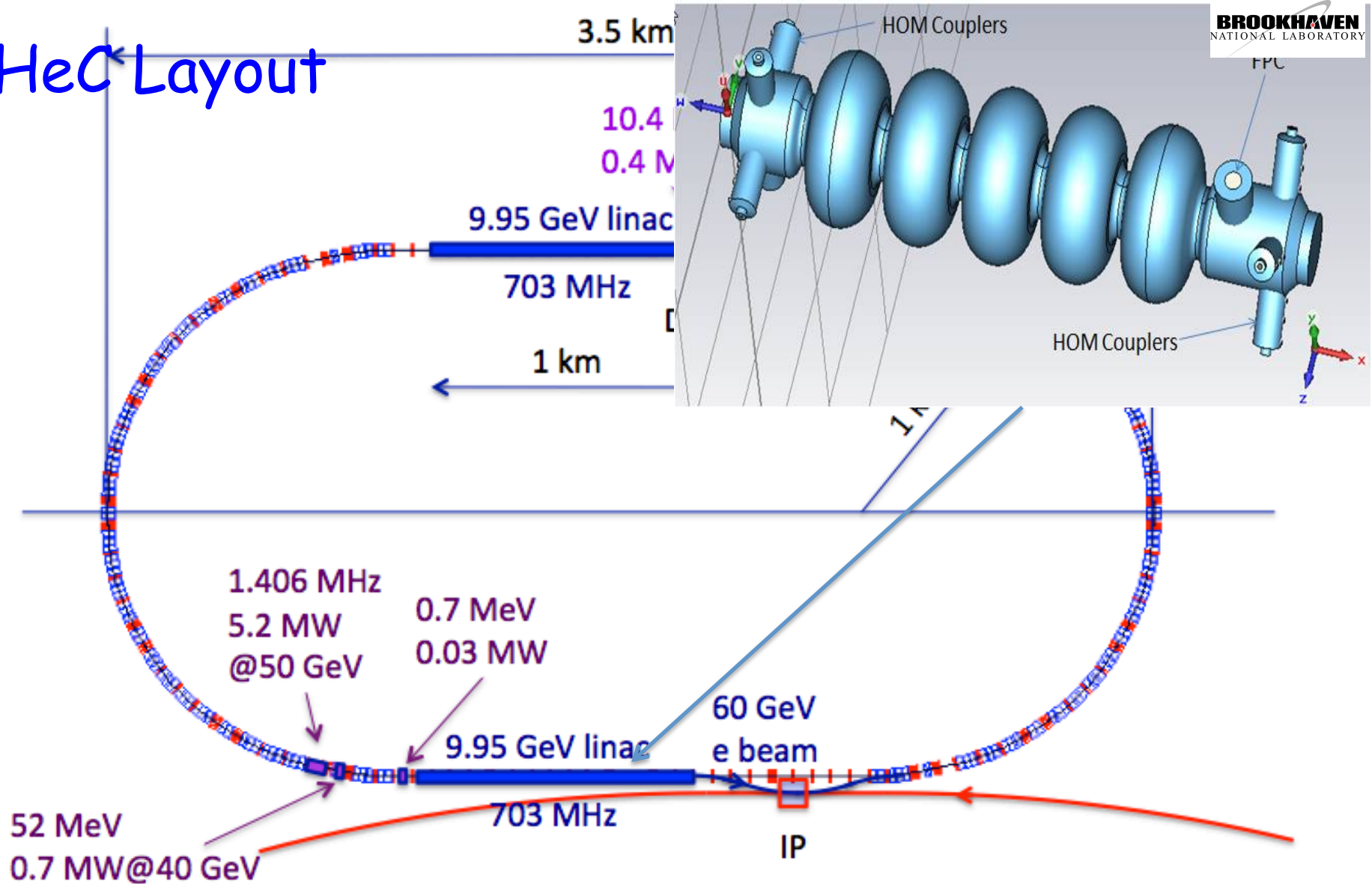


LHeC Layout

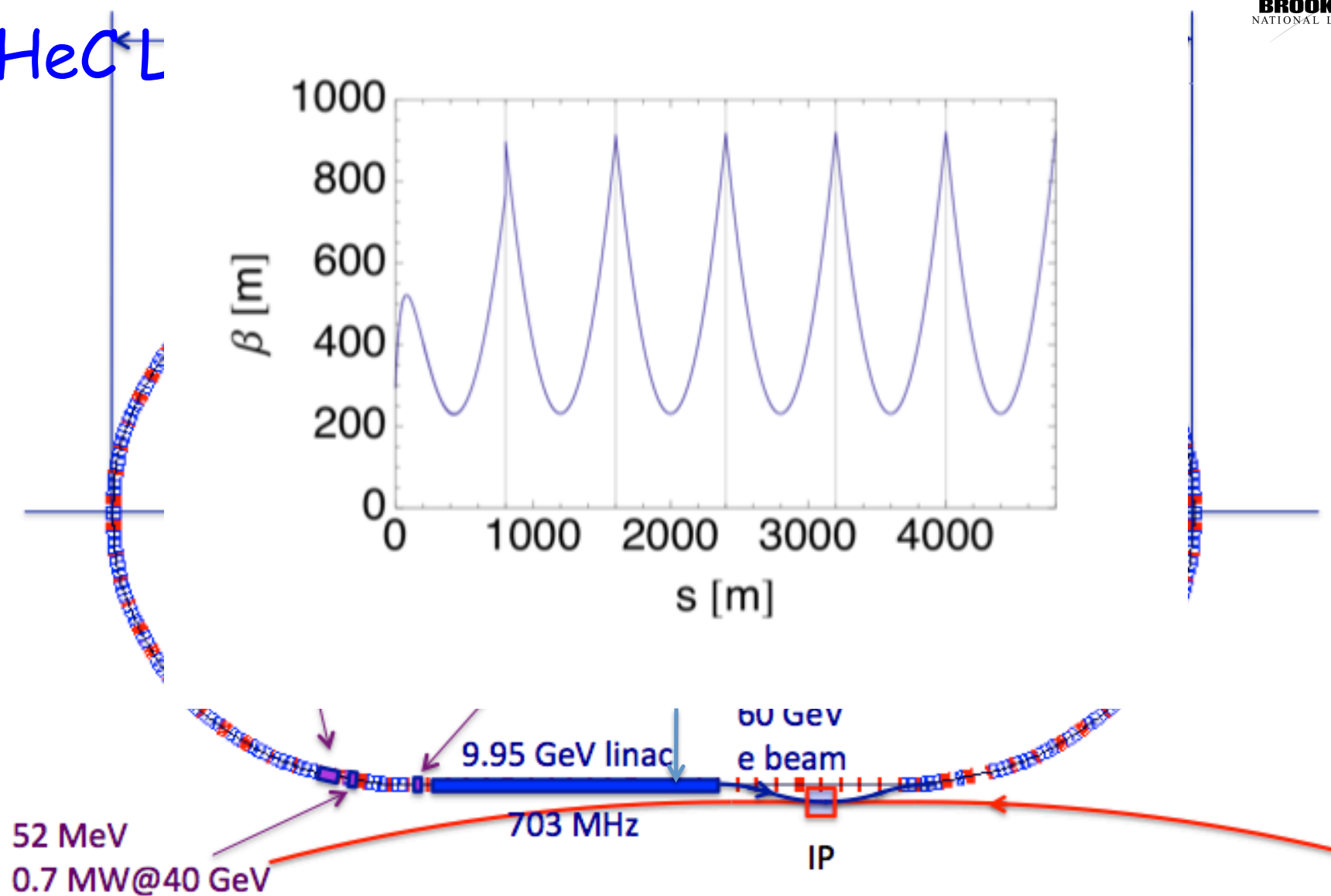




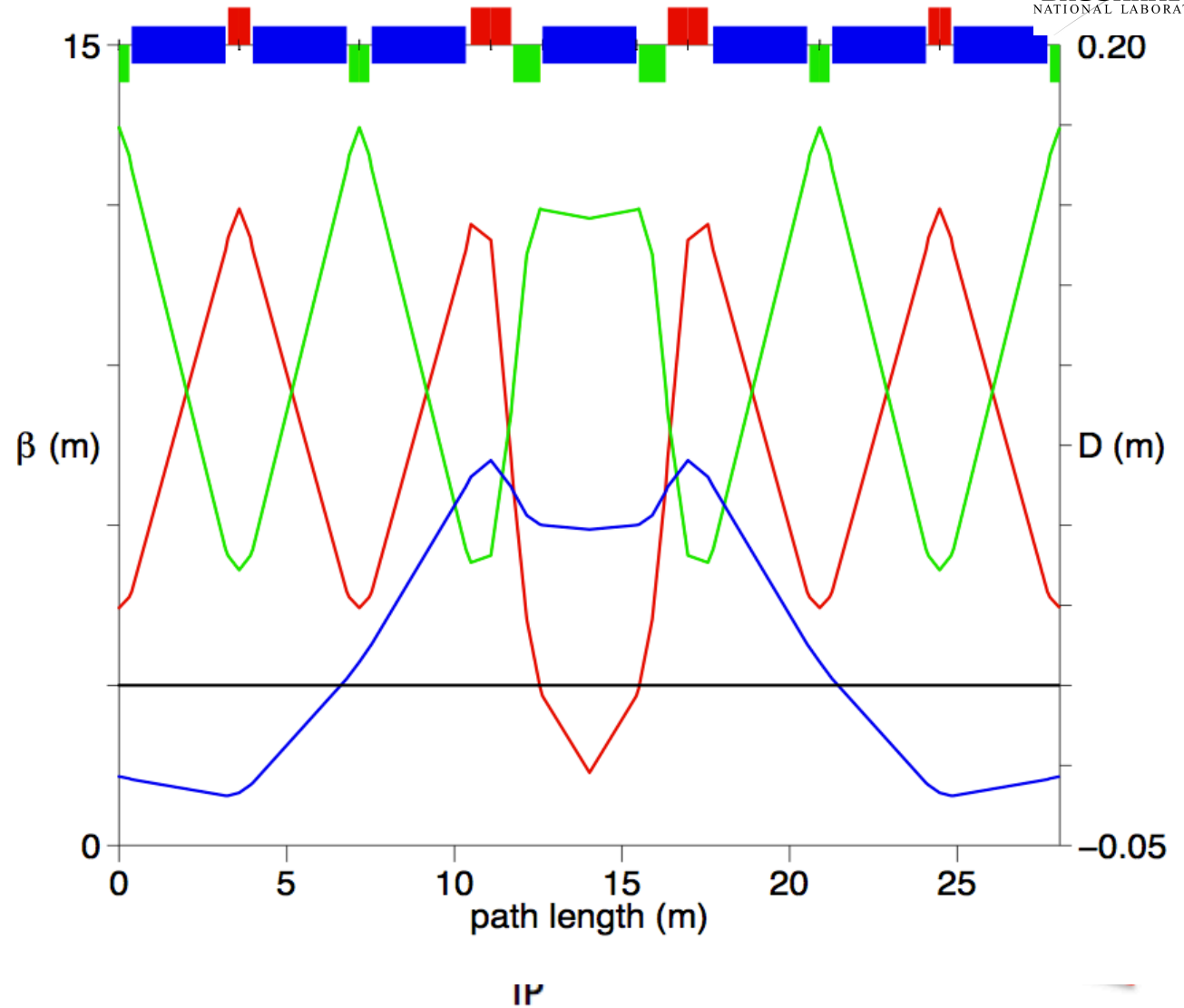
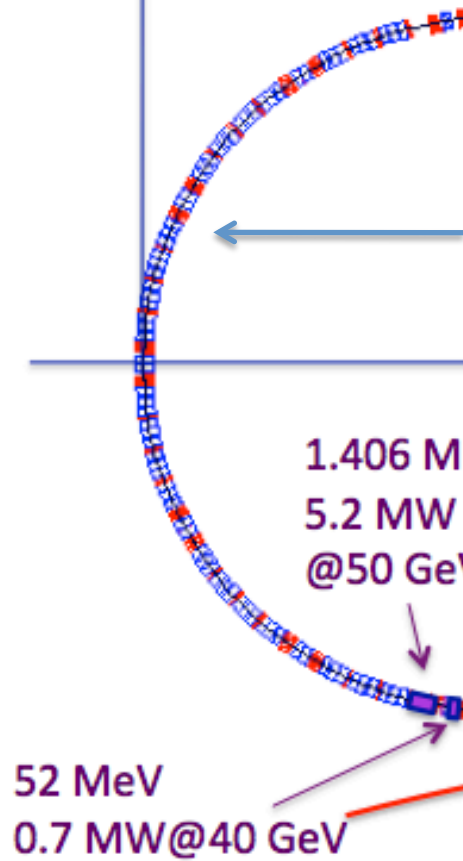
LHeC Layout



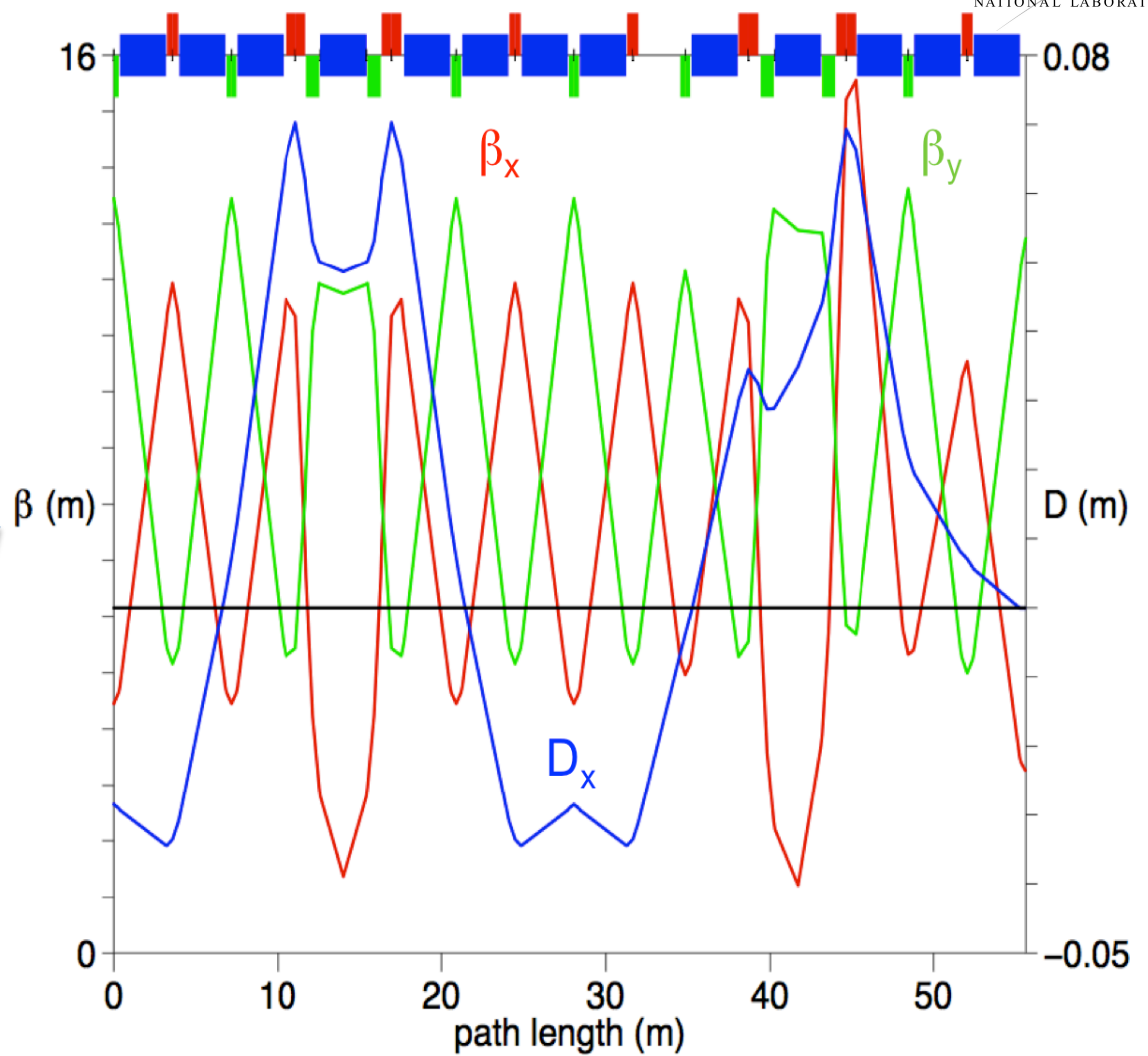
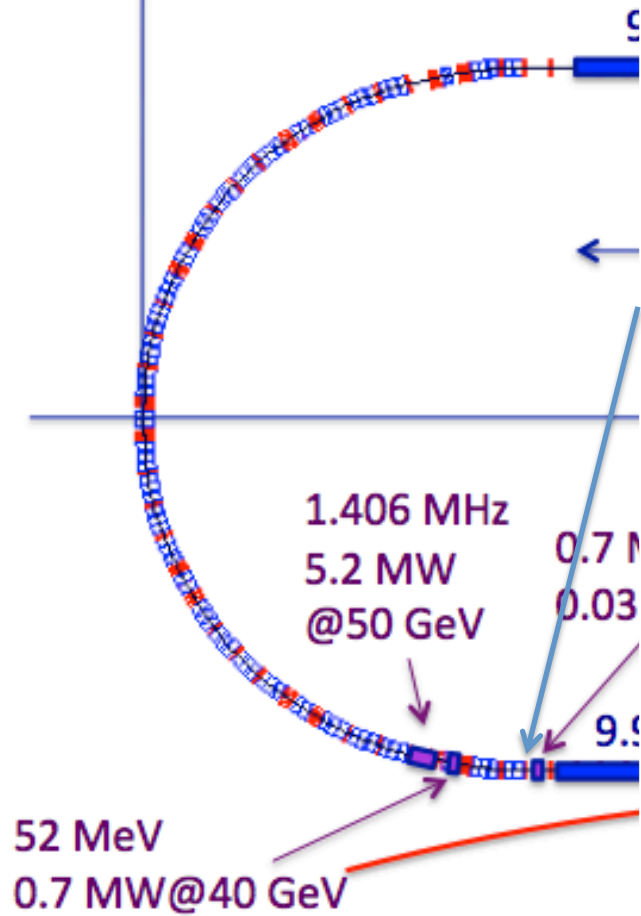
LHeCL



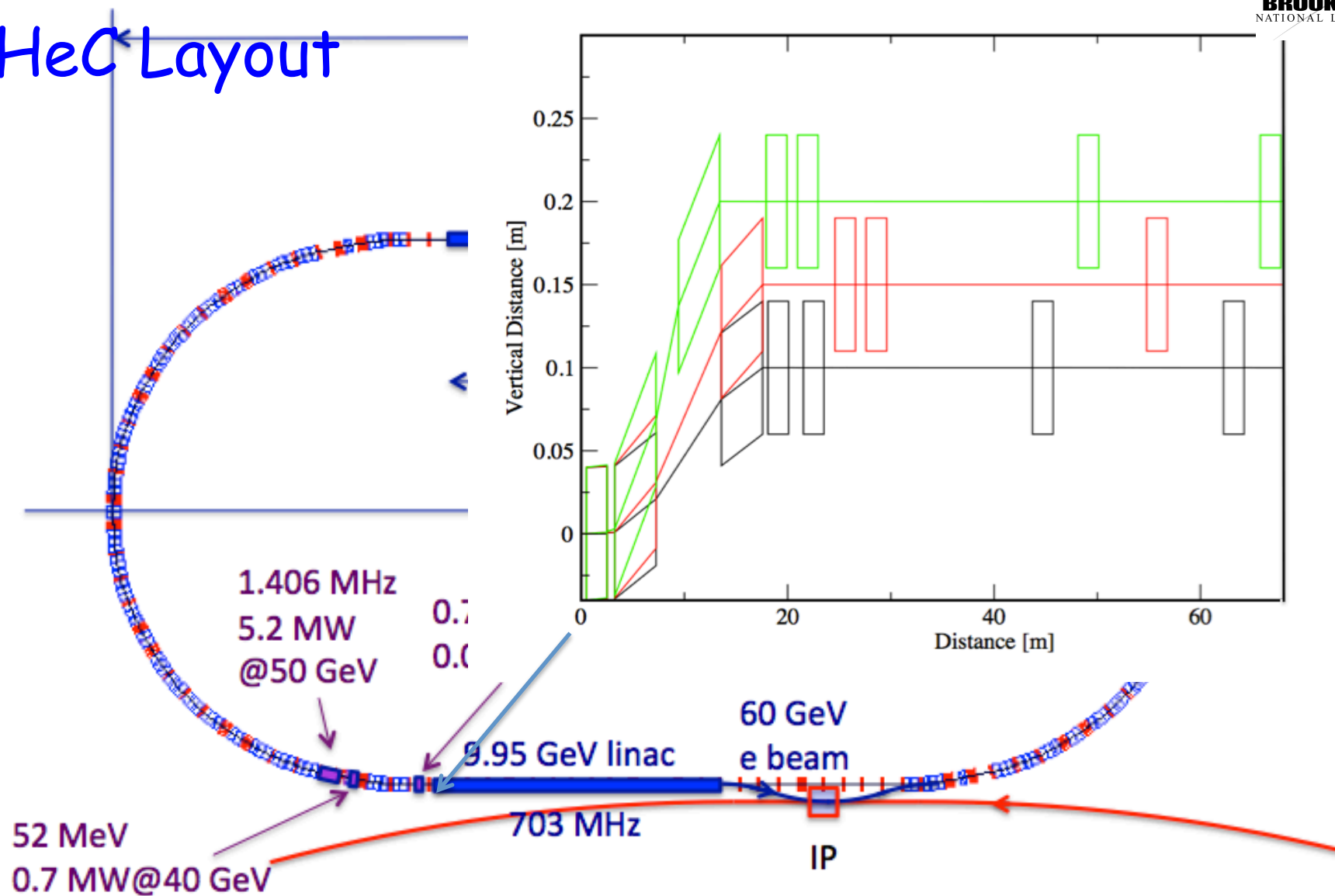
LHeC Layout



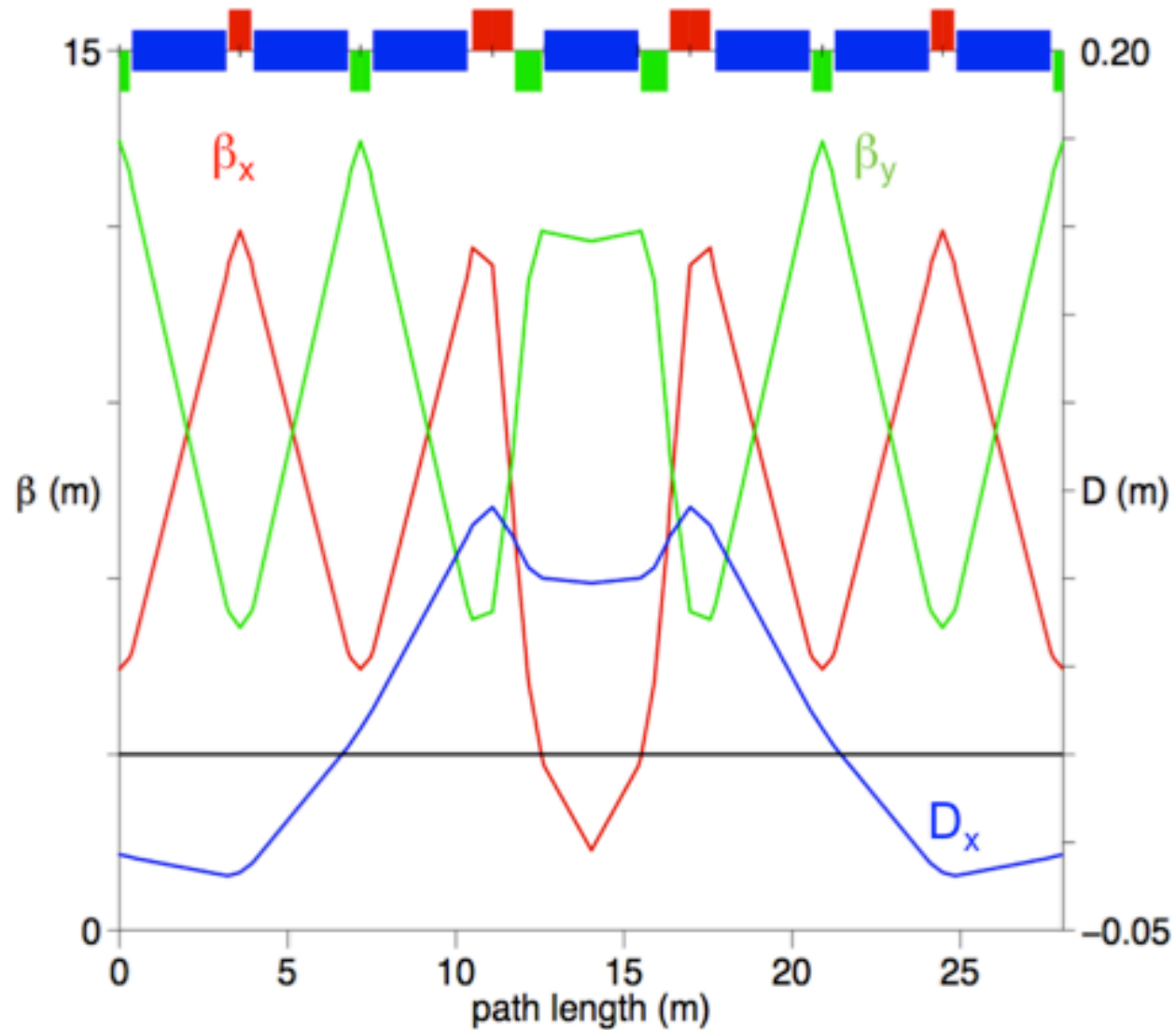
LHeC Layout



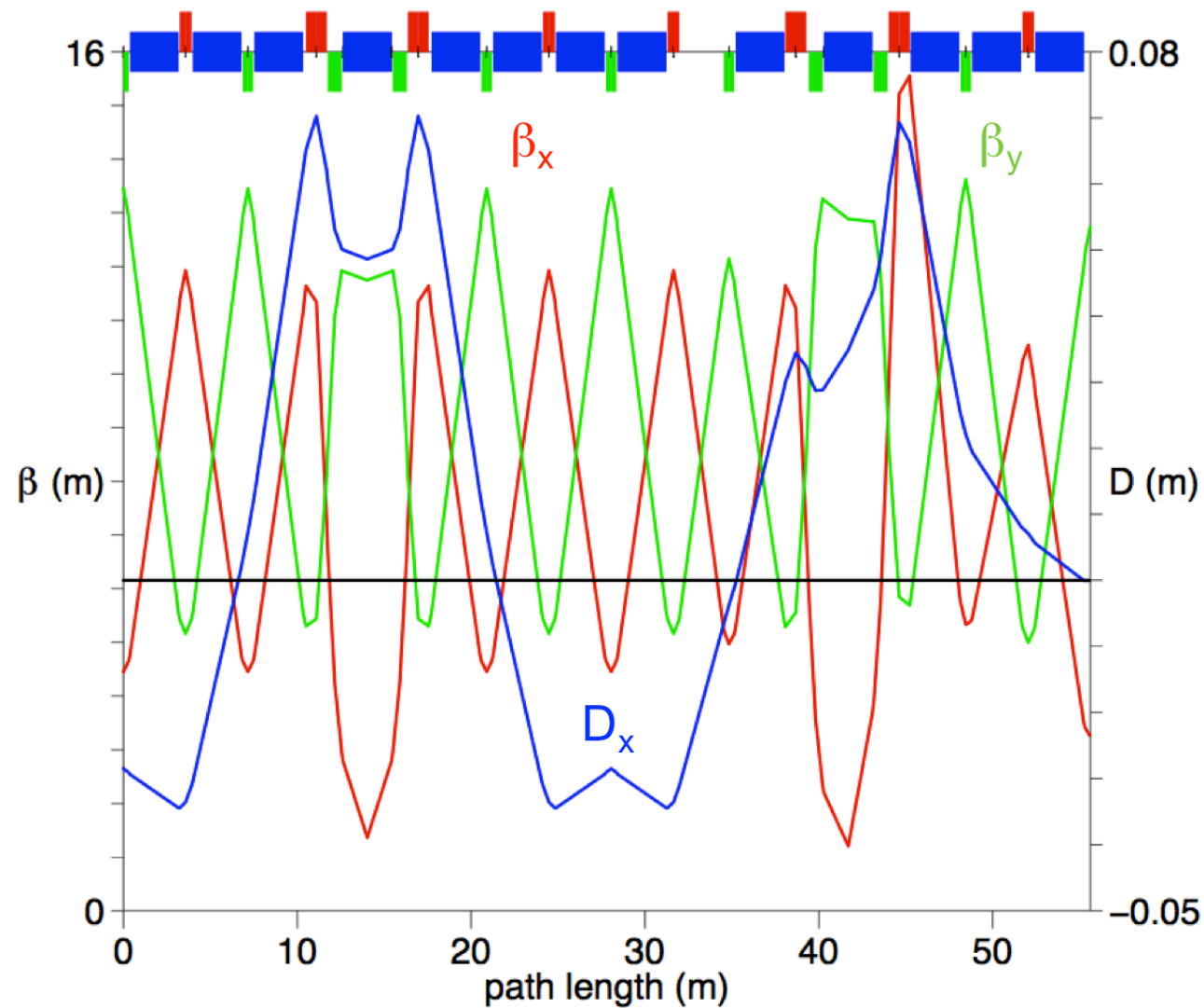
LHeC Layout



Basic arc cell of the LHeC with $\alpha=0$



Achromatic cell with missing dipole scheme



Small emittance strong focusing

Synchrotron Integrals

For separated functions:

$$I_1 = 0.19008E-01$$

$$I_2 = 0.89124E-02$$

$$I_3 = 0.12642E-04$$

$$I_4 = 0.38244E-07$$

$$I_{5X} = 0.10262E-07$$

$$EPX = 6.0829 \text{ nm rad}$$

Synchrotron Integrals

For the combined function:

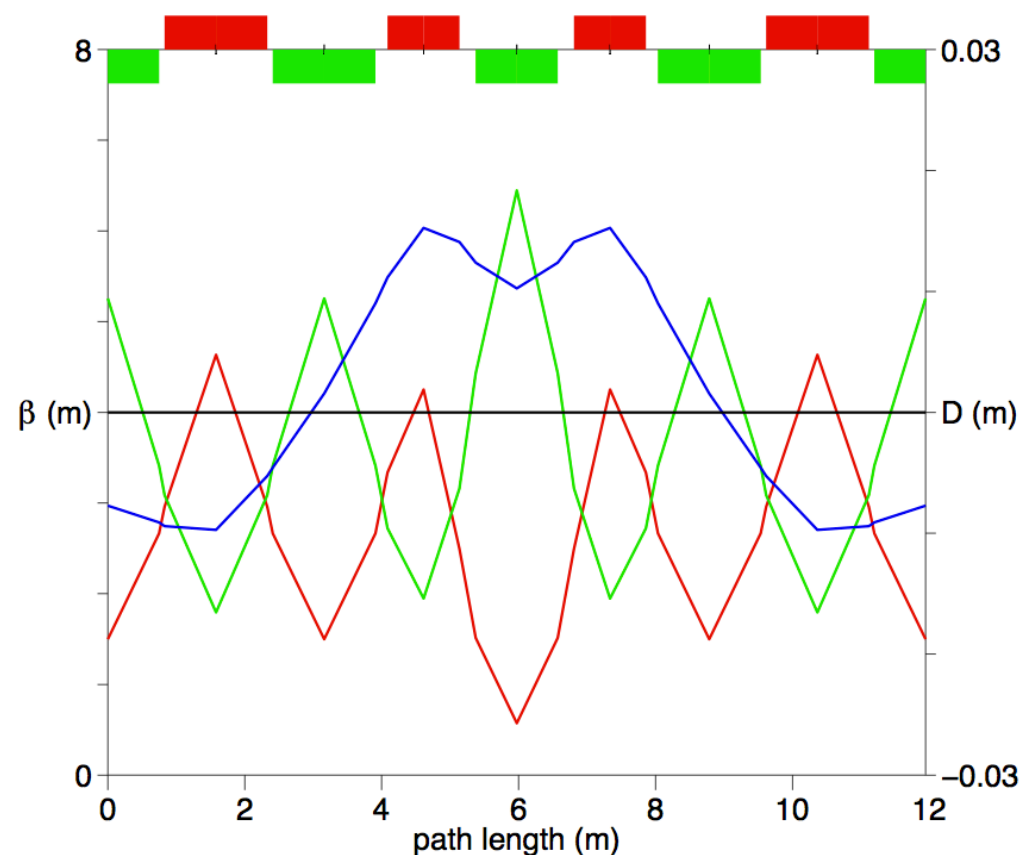
$$I_1 = 0.55866E-02$$

$$I_2 = 0.69494E-02$$

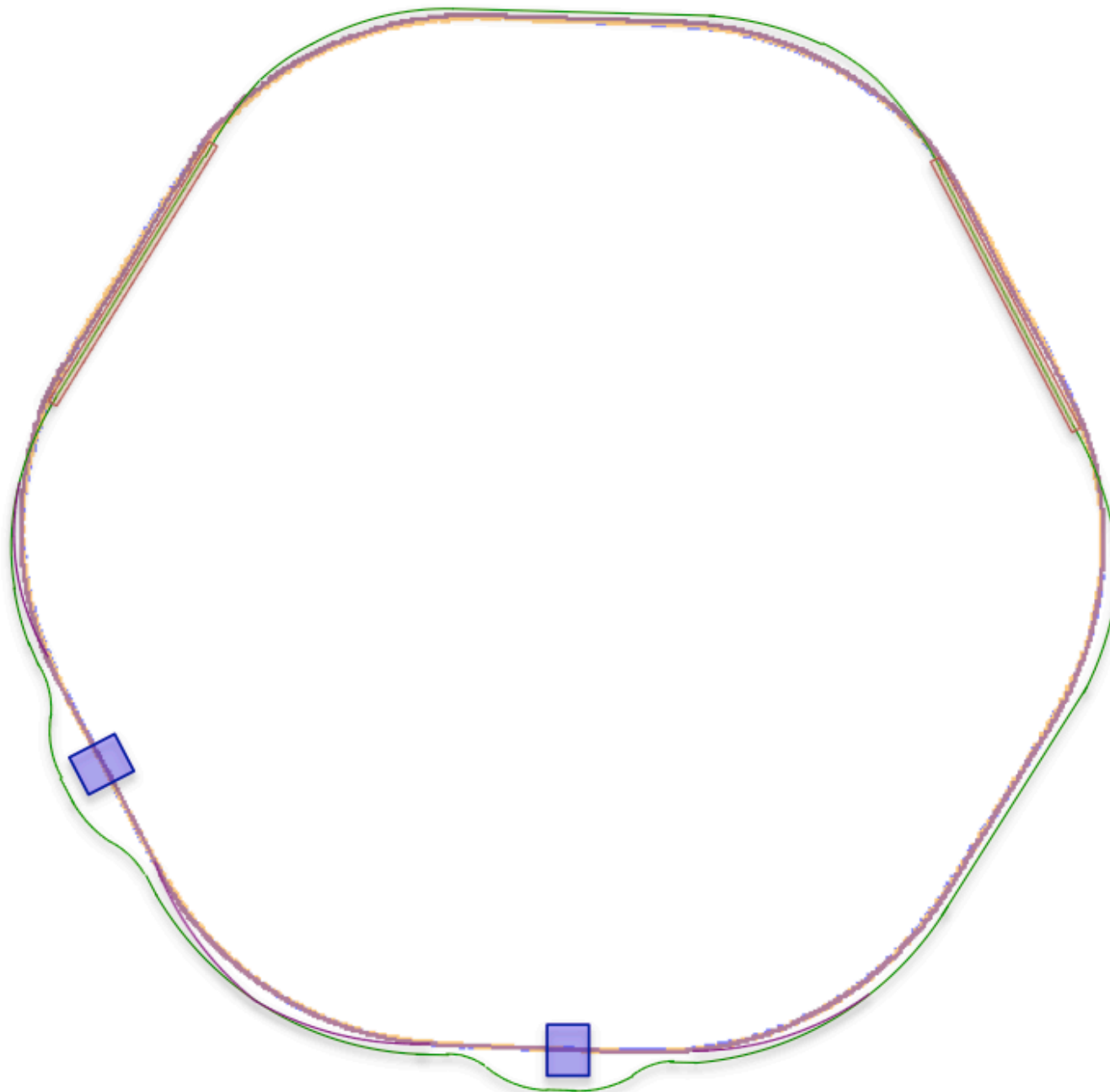
$$I_3 = 0.76864E-05$$

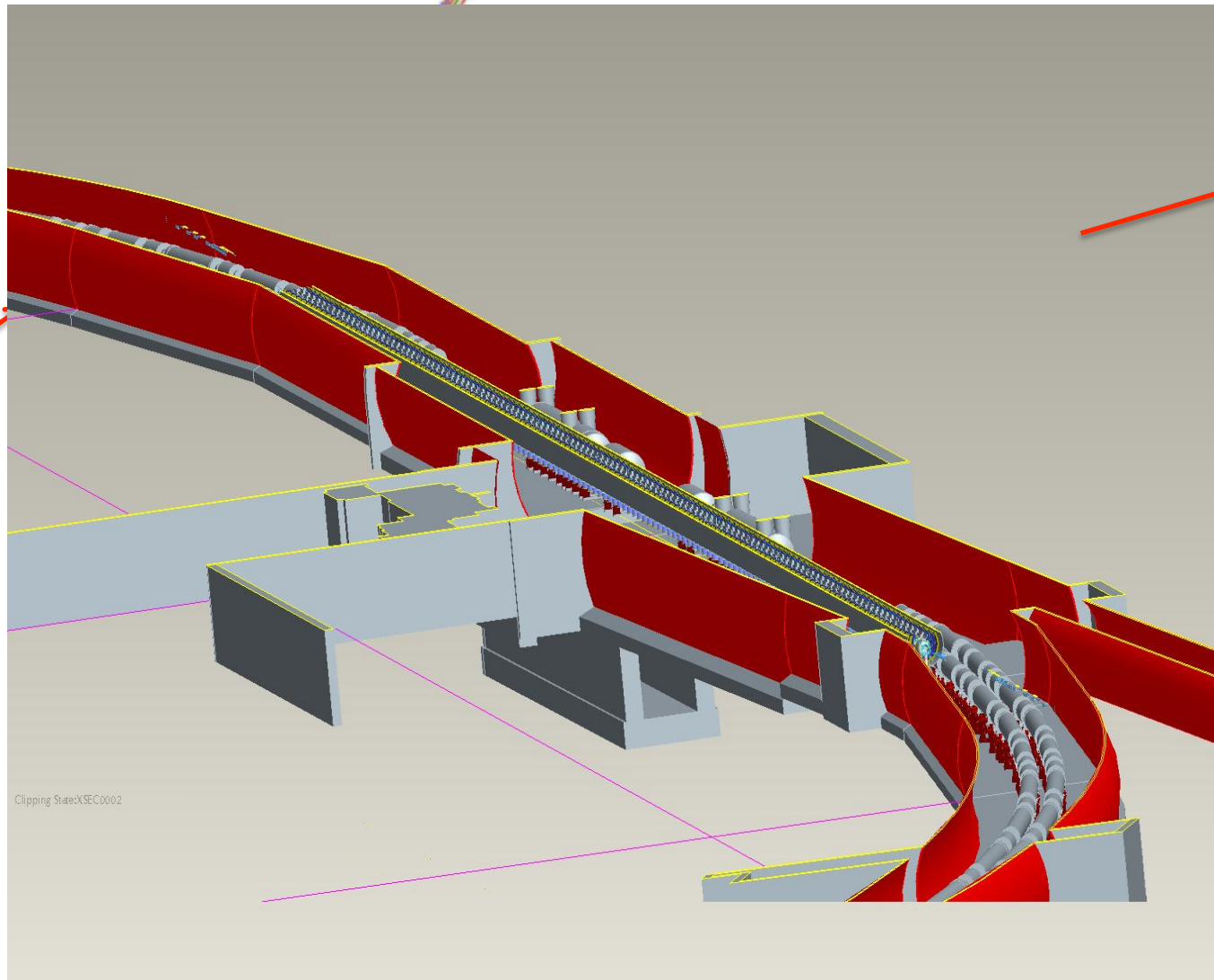
$$I_4 = 0.13899E-01$$

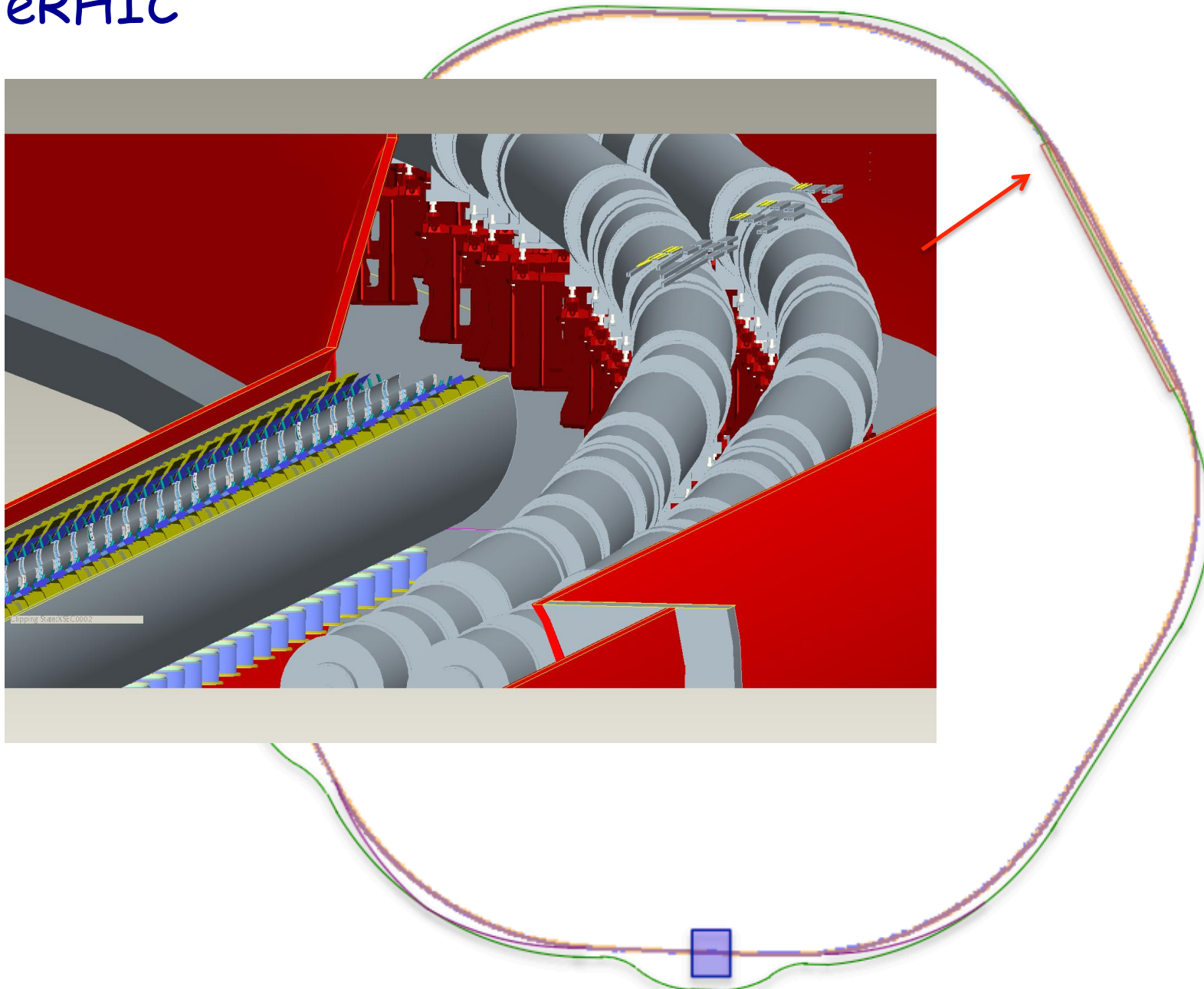
$$I_{5x} = 7.9684E-10$$



eRHIC

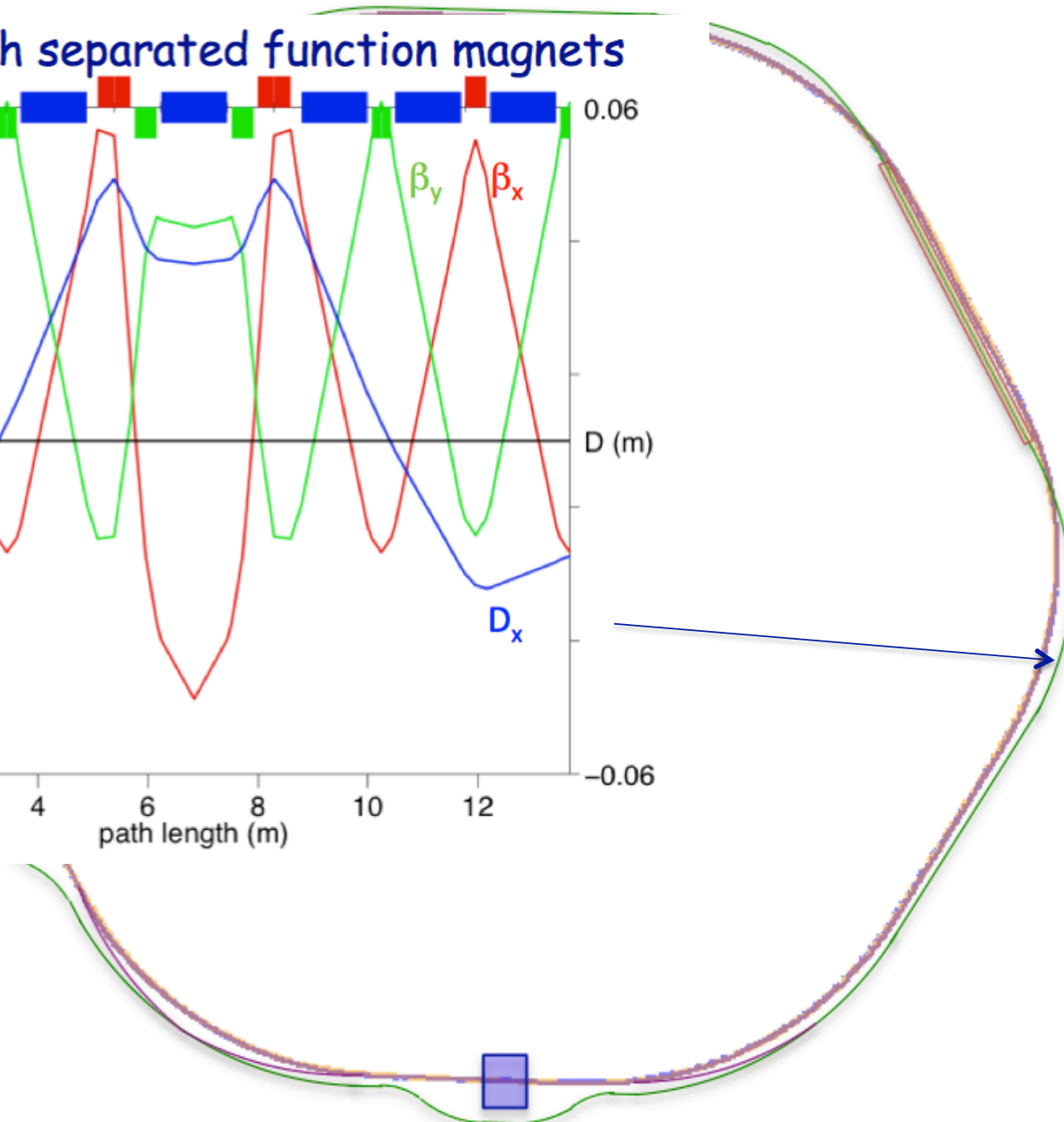
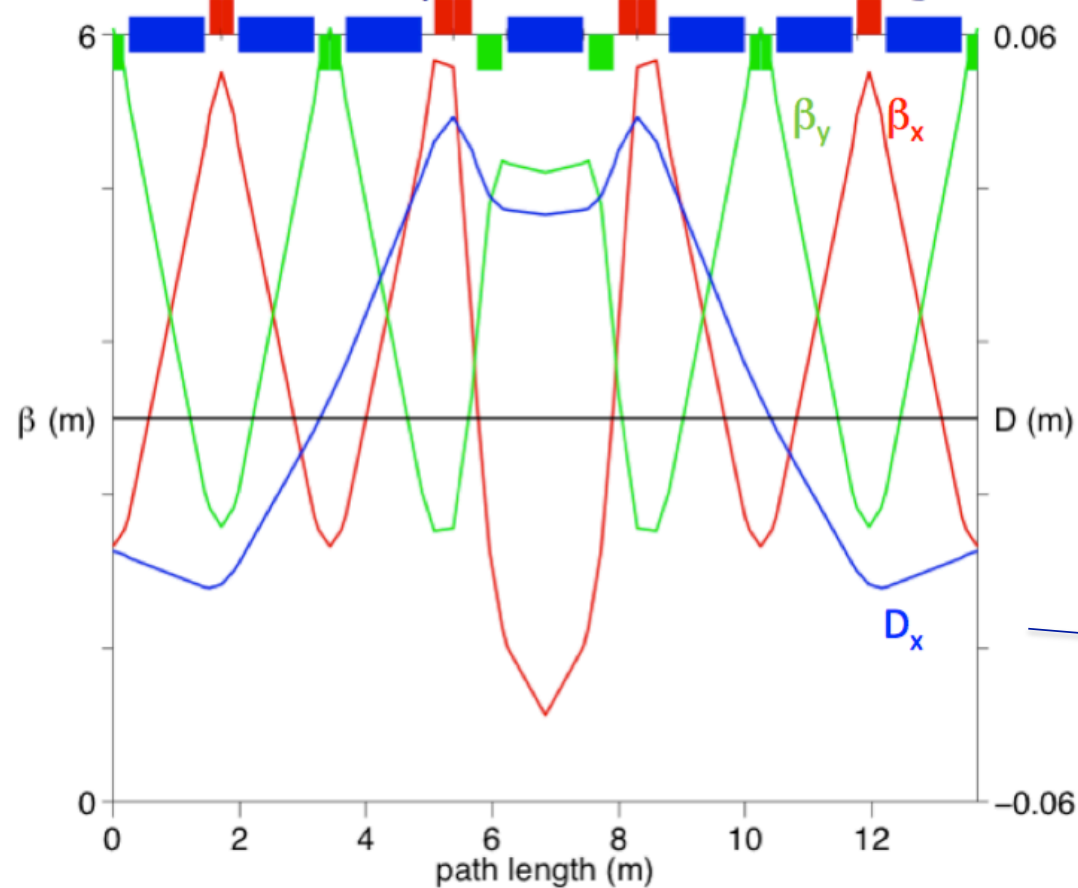


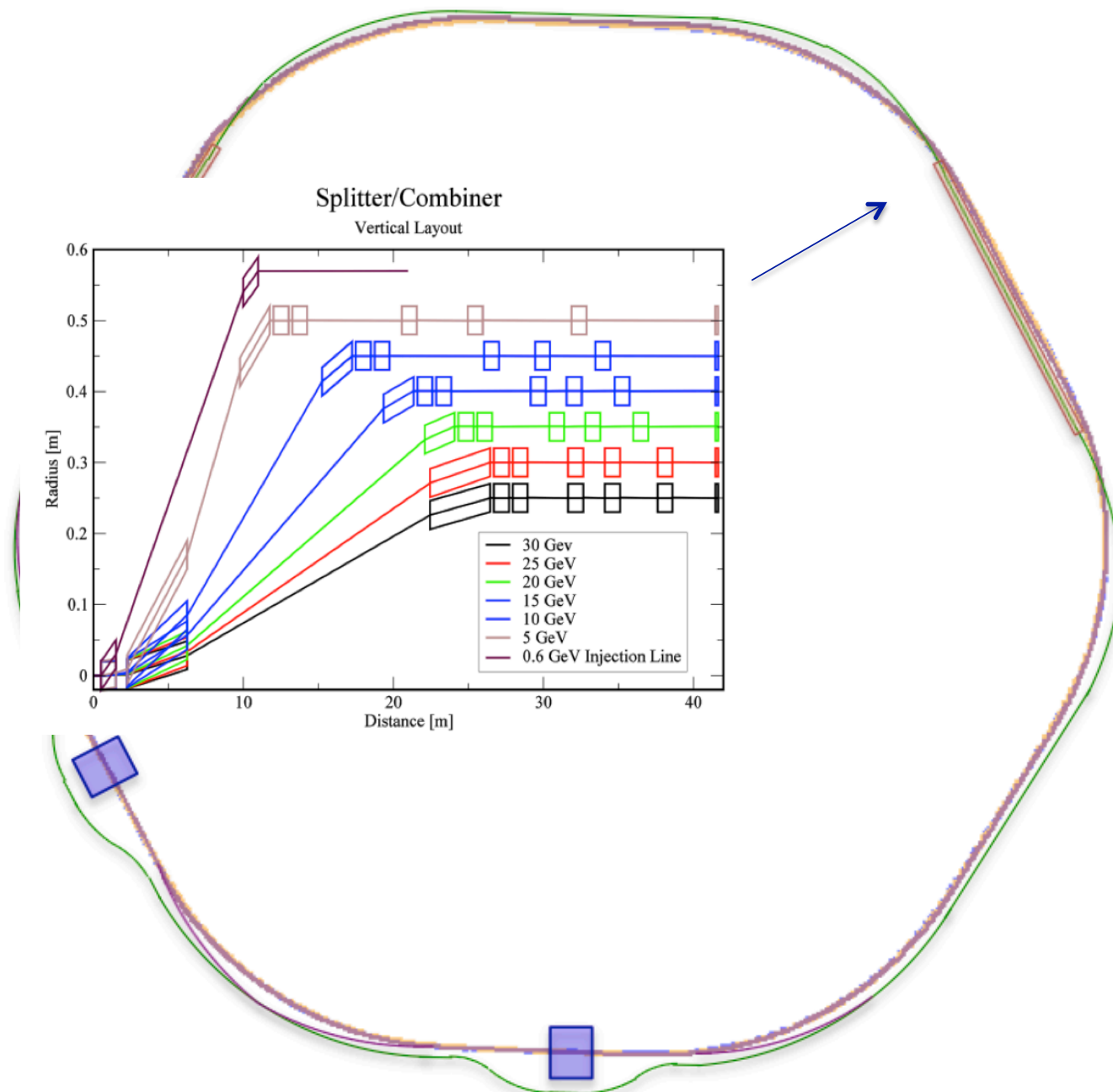


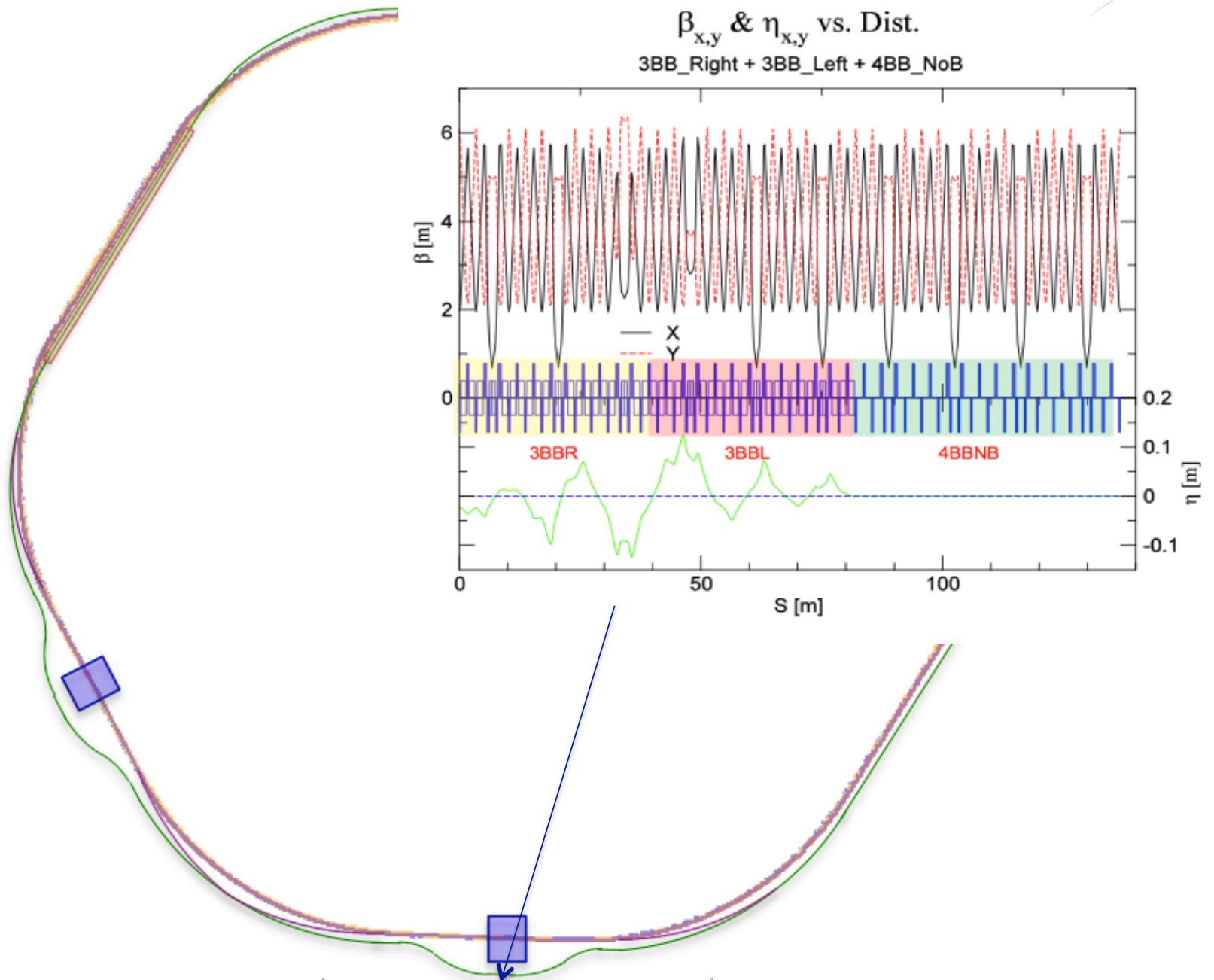


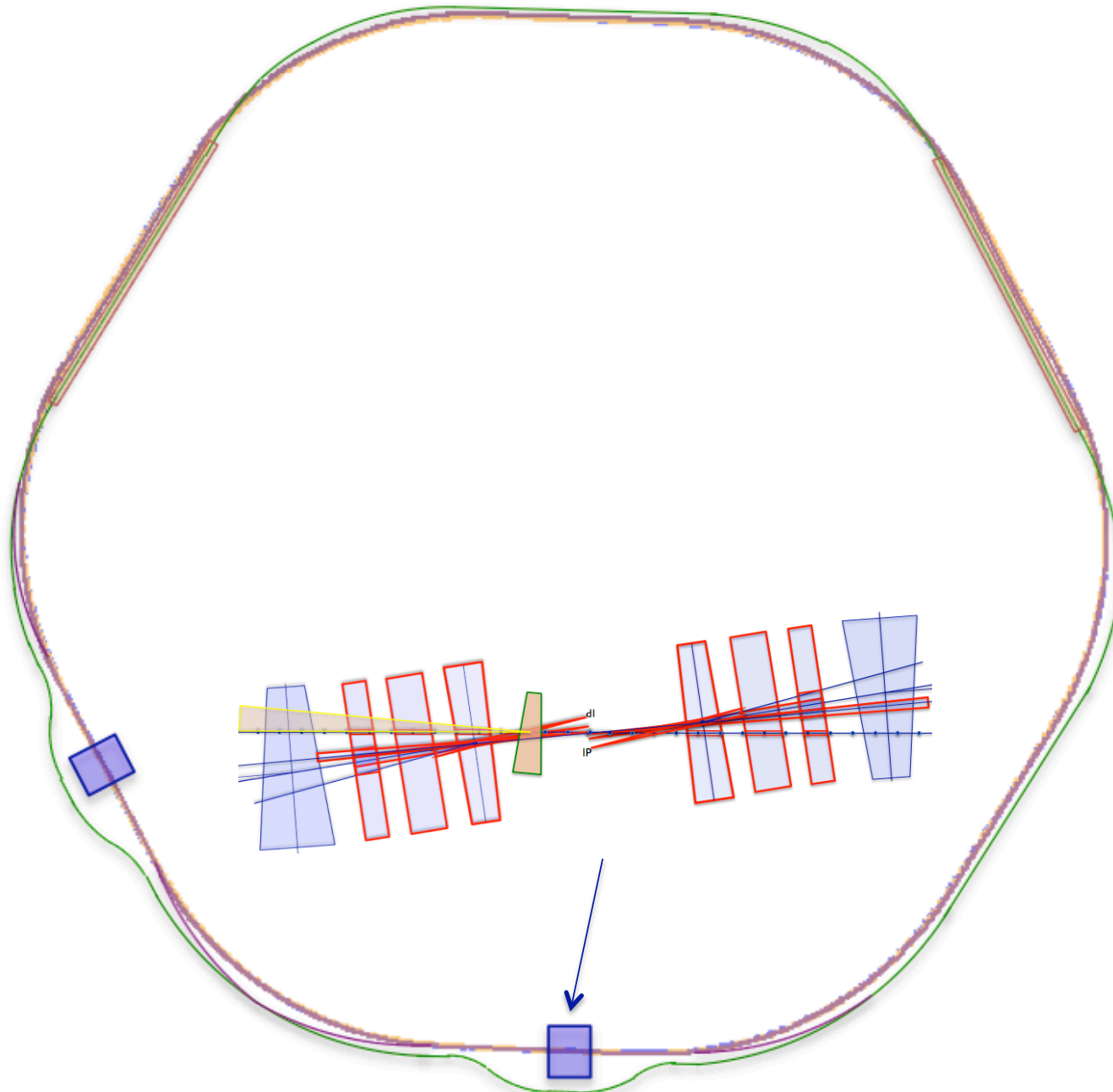
eRHIC

Arc cell with separated function magnets

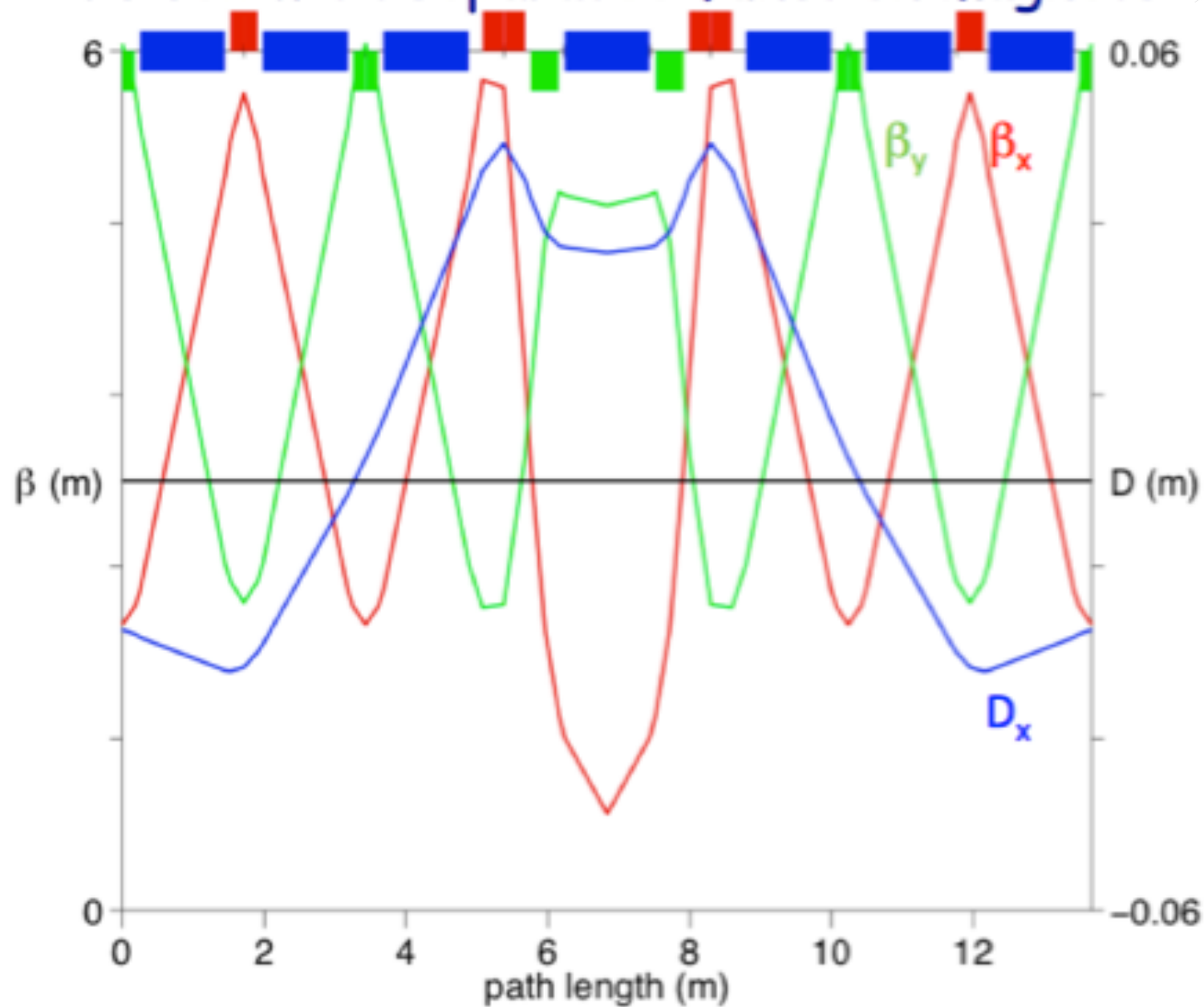




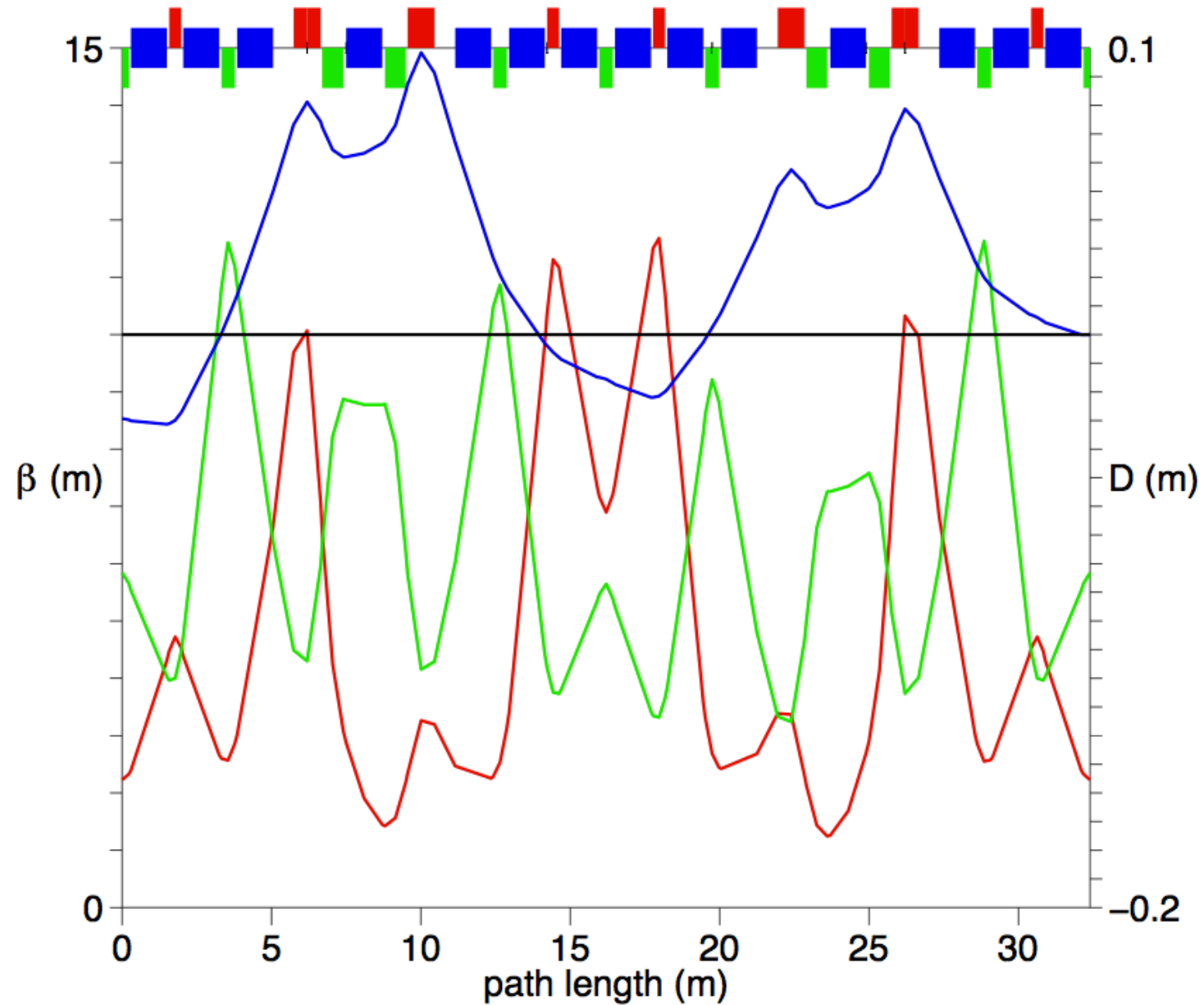




Arc cell with separated function magnets



Achromatic eRHIC cell



Arc lattice with separated function magnets

$$E_{MAX}=30.0 \text{ GeV}, BRHO = 100.069228545 \text{ Tm}$$

Dipoles:

$$L=1.2 \text{ m}, \theta=0.005123124, B=0.427222589 \text{ T},$$

$$R=234 \text{ m (12 passes 7.5 GW)} - 182 \text{ dipoles per sextant}$$

Quadrupoles:

$$L_{fodo}= 0.40 \text{ m}, G_f = 191.3245 \text{ T/m}, G_d = -164.3118 \text{ T/m}$$

$$L_{qf3} = 0.60 \text{ m}, G_f = 212.739 \text{ T/m}$$

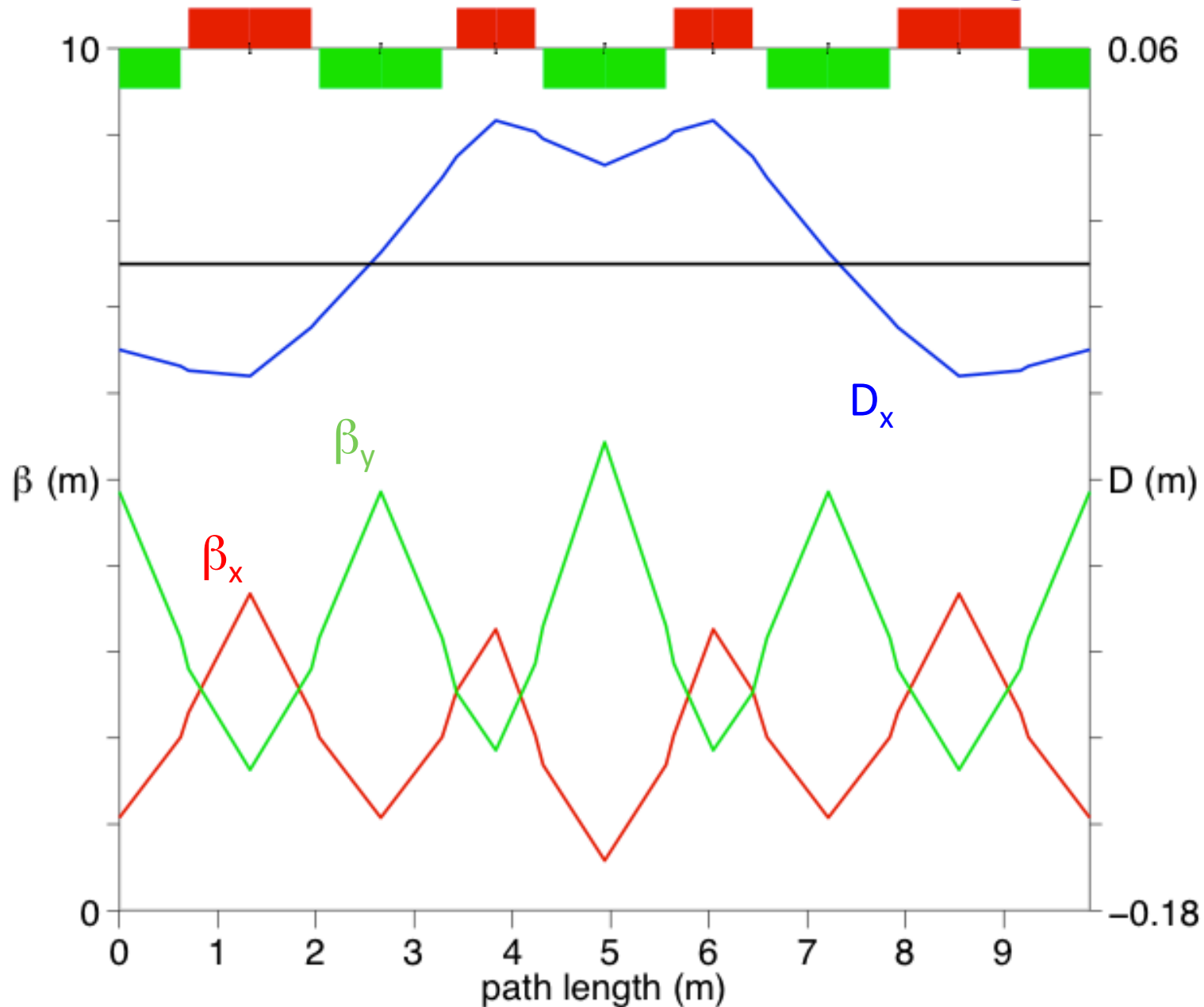
$$L_{qd2} = 0.44 \text{ m}, G_d = -202.53 \text{ T/m}$$

$$\text{Length of the arc cell} = 13.6717 \text{ m}$$

$$\text{Seven dipoles per cell, 26 cells} = 355.46433 \text{ m}$$

$$\text{Total dipole number per sextant } 26 \cdot 7 = 182.$$

Arc cell with combined function magnets



Arc lattice combined function magnets properties

$E_{MAX}=30.0 \text{ GeV}$, $BRHO = 100.0692 \text{ Tm}$

Combined Function Magnets:

$L=1.2 \text{ m}$, $\theta=0.00356$, $B=0.28481 \text{ T}$,

$R=351 \text{ m}$ (For twelve passes deposited energy is 5.0 MW)

Gradients for focusing in the FODO cells:

$G_f = 120 \text{ T/m}$ and for defocusing $G_d = -107 \text{ T/m}$.

Combined function magnets in the middle of the cell:

$L_{qf3} = 0.80 \text{ m}$, $G_f = 220 \text{ T/m}$ $L_{qd2} = 1.2 \text{ m}$, $G_d = -121 \text{ T/m}$

Length of the arc cell= 9.8740 m

$36 \text{ cells} \cdot 9.8740 = 355.46433 \text{ m}$

Total dipole number per sextant $36 \cdot (6 + 2 \cdot QLF3/BL) = 262.08$

SUMMARY

- Lattice design of the future lepton-hadron colliders LHeC and eRHIC based on an ERL, with $M_{5,6} = 0$ as multiple passage electrons through linacs requires from the arcs has been described.
- Arc lattice provide very strong focusing - small size betatron and dispersion functions.
- Linacs lattice is defined by the triplet quadrupoles of the spreaders and combiners.