# DESIGN OF DIFFRACTION LIMITED LIGHT SOURCE RING WITH MULTI-BEND LATTICE ON A TORUS-KNOT

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### Abstract

We proposed a torus knot type synchrotron radiation Fring in that the beam orbit does not close in one turn but 2 closes after multiple turns around the ring. Currently, we are designing a new ring based on the shape of a (11, 3) torus knot for our future plan 'HiSOR-II.' This ring is mid-low energy light source ring with beam energy of 700 MeV.

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Recently some light source rings are achieving very low emittance that reaches a diffraction limited light by adopting a multi-bend scheme to the arc section of the ring. It is not difficult for low-mid energy VUV-SX light adopting a multi-bend scheme to the arc section of the ₹ source ring because the electron beam less than 10 nmrad can provide the diffraction limited light in the energy less ## than 10eV. However the multi-bend lattice has many ਰ families of the magnets, therefore it is not easy to decide the parameters of the lattice. Especially, it is difficult for the torus knot type SR ring because there is a lot of geometric limitation around the cross points of orbits. We present the details of the designing procedure and the present the details of the designing procedure and the specifications of the ultra-low emittance light source ring having innovatively odd shape.

INTRODUCTION

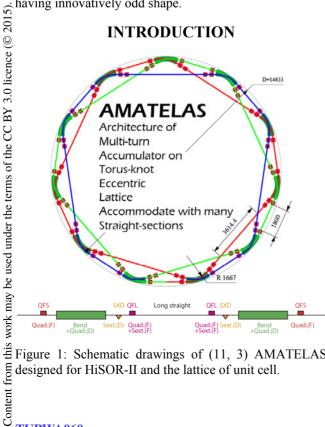


Figure 1: Schematic drawings of (11, 3) AMATELAS designed for HiSOR-II and the lattice of unit cell.

For small light source rings, it is very important to obtain a lot of straight sections in which we can install insertion devices, but it is difficult in reality because they are occupied by various magnets, RF systems or beam monitors. In this context we got a hint from the shape of the torus knot [1], and contrived the ring which had the orbit closed after multiple turns around the ring [2] and named it AMATELAS.

We are planning a new light source ring for our facility [3], therefore we are designing a new ring based on the shape of a (11, 3) torus knot for our future plan 'HiSOR-II' [4]. This ring has 11 long straight sections and we can place insertion devices efficiently by placing the elements such as quadrupole magnets near bending magnet, outside of the orbit crossing section. Furthermore, this ring has about 3 times longer closed orbit in comparison with the conventional ring, the diameter of this ring is as compact as 15 m, but its total orbit length is as long as 130 m. The (11, 3) AMATELAS designed for HiSOR-II storage ring [5] and the lattice of unit cell are shown in Figure 1, and beta or dispersion function of a unit cell is shown in Figure 2.

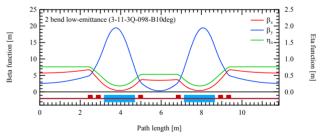


Figure 2: Optical function of (11, 3) AMATELAS for HiSOR-II storage ring.

# ULTRA-LOW EMITTANCE RING WITH MULTI-BEND LATTICE

In late years, some compact light source ring achieved ultra-low emittance of several tens of nmrad. For VUV light sources, it means that it obtains the diffraction limited light to achieve such a low emittance beam. Generally, the beam emittance to obtain the diffraction limited light is given as the following.

$$\varepsilon \leq \frac{\lambda}{4\pi}$$

2: Photon Sources and Electron Accelerators **A05 - Synchrotron Radiation Facilities**  If energy of the light from undulator is 10 eV, this equation shows that emittance should be less than about 10 nmrad. We judged emittance of this size to be possible by adopting the multi-bend lattice, and we started the design ultra-low emittance light source ring for HiSOR-II [6][7].

#### Multi-bend Lattice

In the original lattice shown in Figure 1, it has two bending magnets in one unit cell. It is advantageous to lower emittance that the bend is divided into more bends, however, we decided to adopt the multi-bend lattice having 4 bending magnets for reasons of the geometric size of this ring. There are many variations to length of magnets or drift spaces between the magnets in lattices having 4 bends with defocusing quadrupole field in one cell, but we notice that placement is not so much easy from necessity to place on a torus-knot shape.

The schematic draws of the lattices are shown in Figure 3. In this figure, (a) shows the original double-bend lattice, (b) is the 4-bends multi-bend lattices for the (11, 3)-AMATELAS.

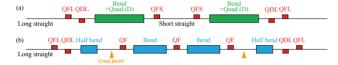


Figure 3: Multi-bend type cells compared with double-bend lattice. (a) is original double-bend lattice. (b) shows multi-bend lattice for (11,3)-AMATELAS.

#### Geometry

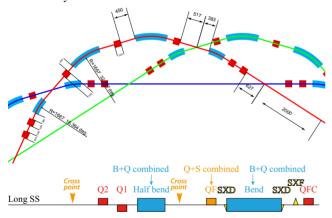


Figure 4: Geometry of unit cell of HiSOR-II and lattice of half of unit cell.

In original double-bend type lattice, beam orbit crosses in the bending magnets, but it is necessary to consider where it should cross in these multi-bend lattices. As for the simplest geometry, all magnets of arc section are placed in the outside of the crossing section, however actually it is impossible to have enough length.

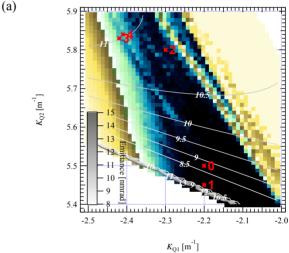
Finally, we decide that it is the most suitable to place a crossing at the drift space between the bending and quadrupole magnet at the end of arc. Figure 4 shows a

geometry of unit cell of (11, 3)-AMATELAS with multibend lattice for HiSOR-II.

Further, the sextupoles are necessary to correct the chromaticity. Two SXFs are placed between bend and QFC, and QFs are combined function magnets that have quadrupole and sextupole field. Defocus SXDs are combined to the ends of poles of two bending magnets.

## K-survey and Operating Point

Because AMATELAS has many straight sections for insertion devices, it is necessary to consider influence by the undulators. Therefore we adopt a lattice of achromat system. A dispersion function is determined by the K-value of bends and quadrupole in an arc section, from half bend to half bend, accordingly its three parameters are almost decided by achromatic condition. Therefore quadrupole doublets Q1 and Q2 are added the outside of the arc to give the variability of the horizontal and vertical beta functions.



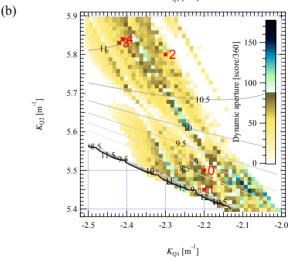


Figure 5: Result of K-survey. (a): dynamic aperture at the centre of long straight section without alignment errors, (b): with alignment errors. Contour lines in each graph show natural emittance.

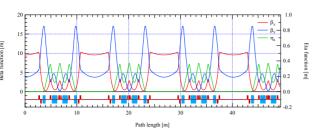
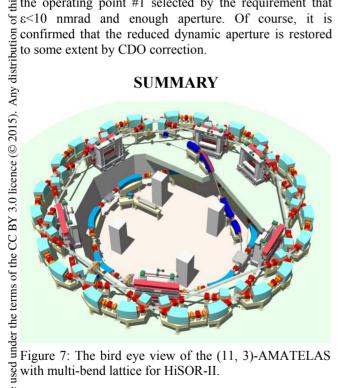


Figure 6: Beta functions and dispersion function in 1/3 turns of ring at operating point #1.

Figure 5 shows the results of K-value survey by the quadrupole doublets which provides two free parameters to choose operating point. Figure (a) shows dynamic aperture at the centre of long straight section in the Kmap of two quadrupoles Q1 and Q2. The sextupoles to correct the chromaticity are supposed in the strength that  $(\xi_x, \xi_y) = (+1, +1).$ 

Figure (b) shows dynamic aperture with alignment Figure (b) shows dynamic aperture with alignment errors to all magnets. It is estimated the errors that transverse shift is 0.1 mm and axial tilt is 0.1 mrad in this

The contour lines in each figure show natural emittance. Red markers show candidate of operating points, and Figure 6 shows the optical functions in 1/3 turns of ring at E the operating point #1 selected by the requirement that ₹ ε<10 nmrad and enough aperture. Of course, it is



with multi-bend lattice for HiSOR-II.

We are designing the light source ring based on the torus-knot shape as our future plan HiSOR-II. We can get smaller emittance and may get diffraction limited light in the VUV region adopting a multi-bend lattice to this ring.

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As a result of considering in various lattices in the linear dynamics, we are able to make the lattice that reached emittance is 8.10 nmrad as our target. Figure 7 shows the bird eye view of the accelerator complex including the (11, 3)-AMATELAS with multi-bend lattice for HiSOR-II, and the main parameters are shown in Table 1.

Table 1: The Main Parameters of (11, 3) AMATELAS with Multi-Bend Lattice for HiSOR-II Storage Ring

Orbit shape	(11,3) Torus knot
Perimeter	50.868 m
Orbit length	147.517 m
Beam energy	700 MeV
Straight sections	4.000 m ×11
Betatron tune	(16.649, 8.150)
Chromaticity	(+1.0, +1.0)
Natural emittance	8.10 nmrad
Ring current	300 mA
RF voltage	500 kV
Coupling	10.0 %
Harmonic number	50
RF frequency	101.6 MHz
Touschek life time	3.9 hours

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