

Comparison of Different Simulation Codes with UNILAC Measurements for High Beam Currents



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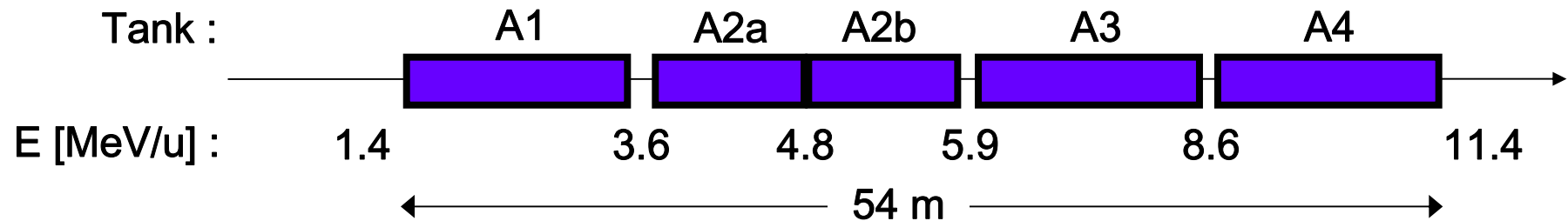
R. Tiede, *Goethe University of Frankfurt a.M., Germany*

- Introduction and set-up
- Reconstruction of initial distribution
- Comparison of measurements and simulations
- Beam matching with space charge
- Octupolar space charge driven resonance
- Summary

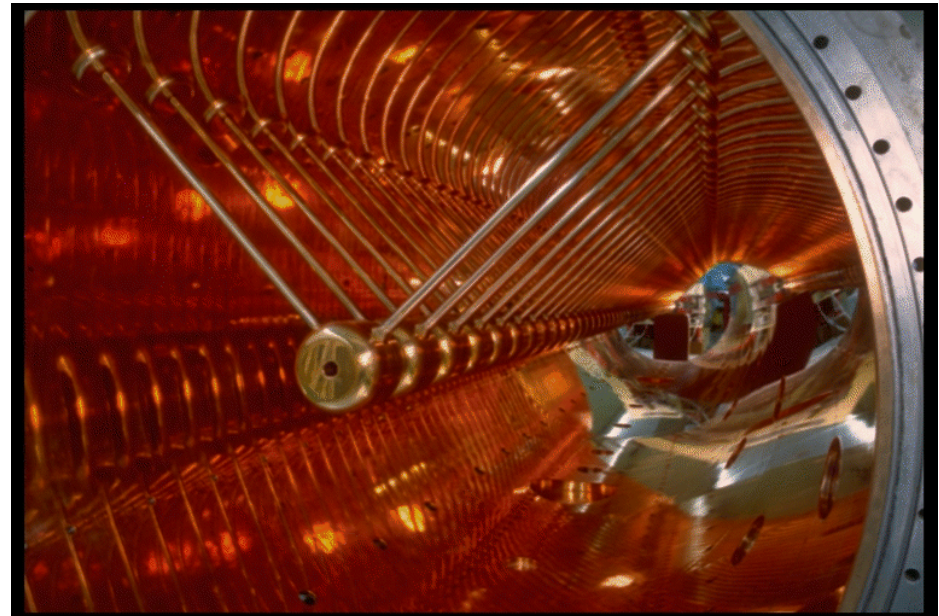
Phys. Rev. ST Accel. Beams **11**, 094201 (2008)

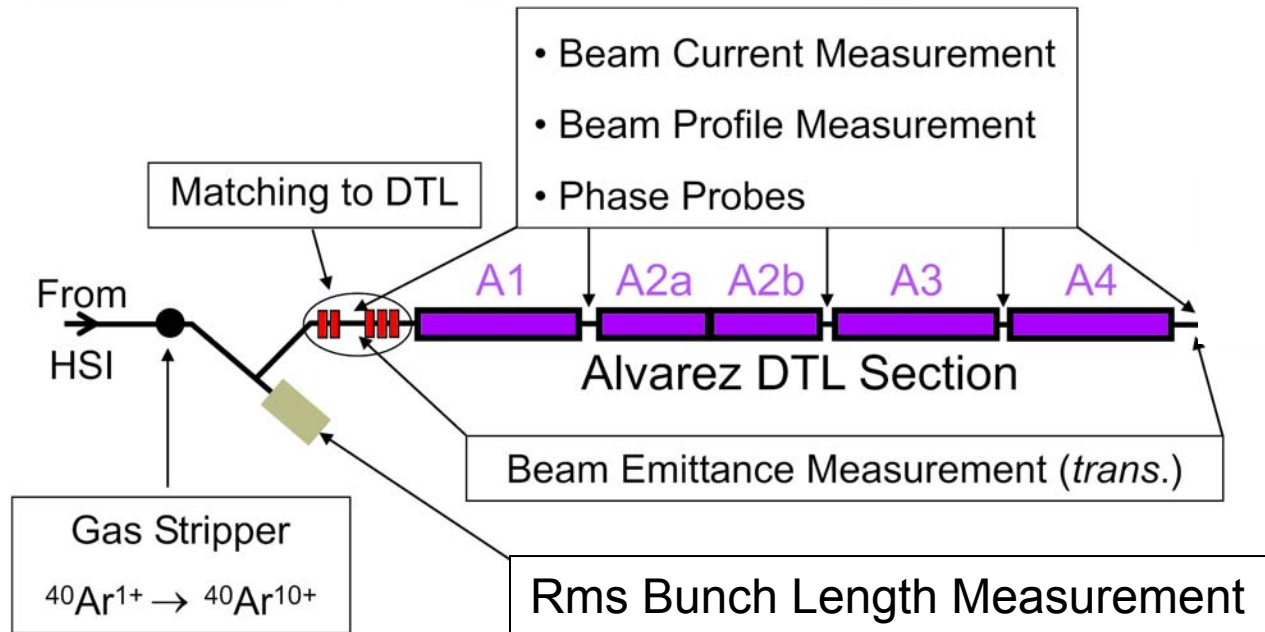
Phys. Rev. ST Accel. Beams **12**, 054204 (2009)

Phys. Rev. Lett. **102**, 234801 (2009)

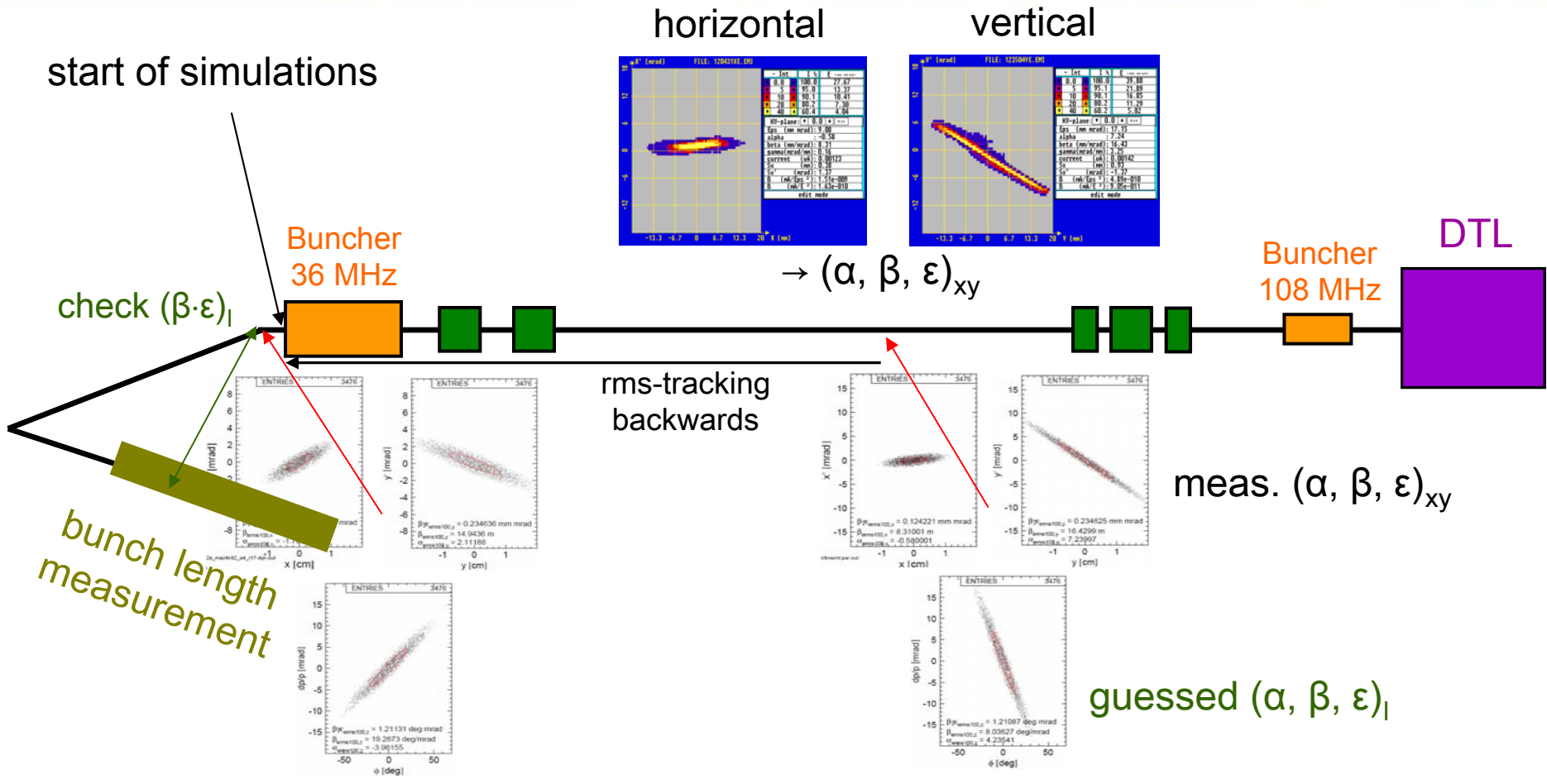


- 5 independent rf-tanks
- 108 MHz
- 192 rf-cells
- F-D-D-F focusing
- inter-tank focusing : F-D-F
- synchr. rf-phases $-(30^\circ, 30^\circ, 30^\circ, 25^\circ, 25^\circ)$

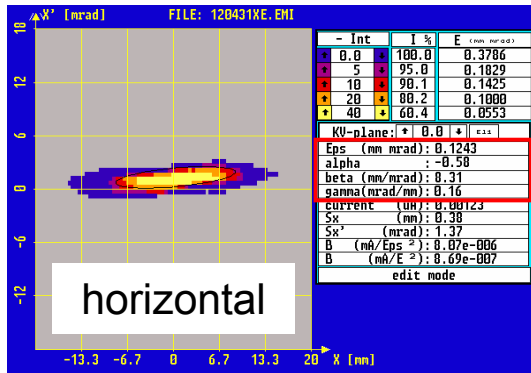




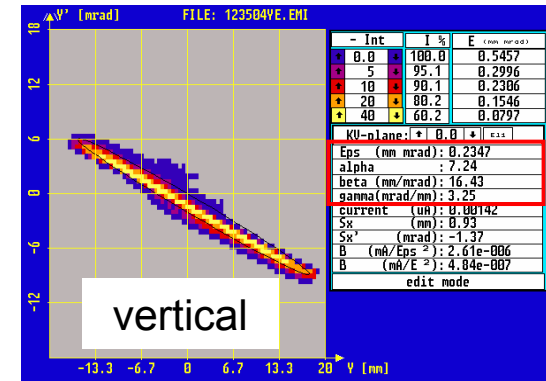
- set beam current to 7.1 mA of $^{40}\text{Ar}^{10+}$
- measure hor., ver. emittance, and long. rms-bunch length at DTL entrance
- set DTL transverse phase advance to values from 35° to 130° (undepressed)
 - tune depression varied from 14% (130°) to 43% (35°)
- measure transmission, hor., and ver. rms-emittance at DTL exit



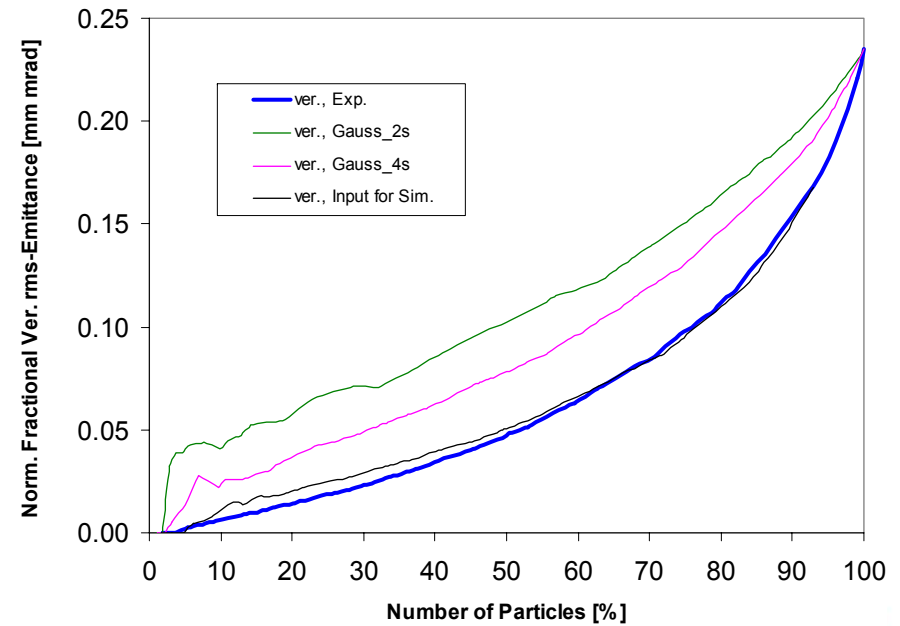
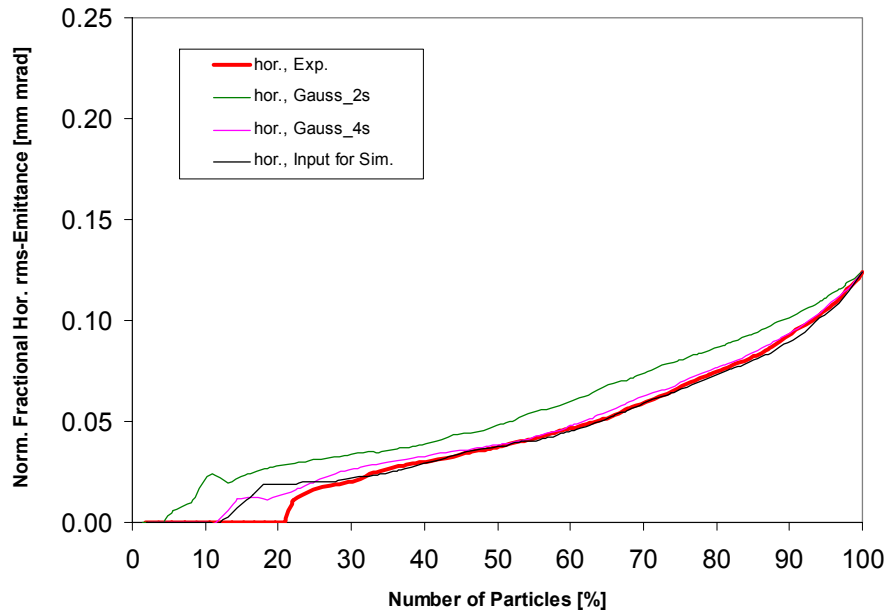
1. selfconsistent KV backtracking, i.e. finding $(\alpha, \beta, \epsilon)_1$ that fit to measured bunch length
2. verification by sims whether applied machine settings give full transmission w/o tails



measured in front of DTL



measured initial distribution inhabits different amount of halo horizontally and vertically





- Gauss, Lorentz, Waterbag, KV distributions do not fit the measured amount of halo
- several functions tried in order to fit halo in both planes
- function found as:

$$\frac{dN}{dV} = f(X, X', Y, Y', \Phi, \delta P/P)$$

$$\tilde{R}^2 = X^2 + X'^2 + Y^{1.2} + Y'^{1.2} + \Phi^2 + (\delta P/P)^2$$

$$f(\tilde{R}) = \frac{a}{2.5 \cdot 10^{-4} + \tilde{R}^{10}}, \quad \tilde{R} \leq 1$$

$$f(\tilde{R}) = 0, \quad \tilde{R} > 1,$$

applying different powers for different planes, the amount of halo can be reproduced in each plane separately



initial distribution

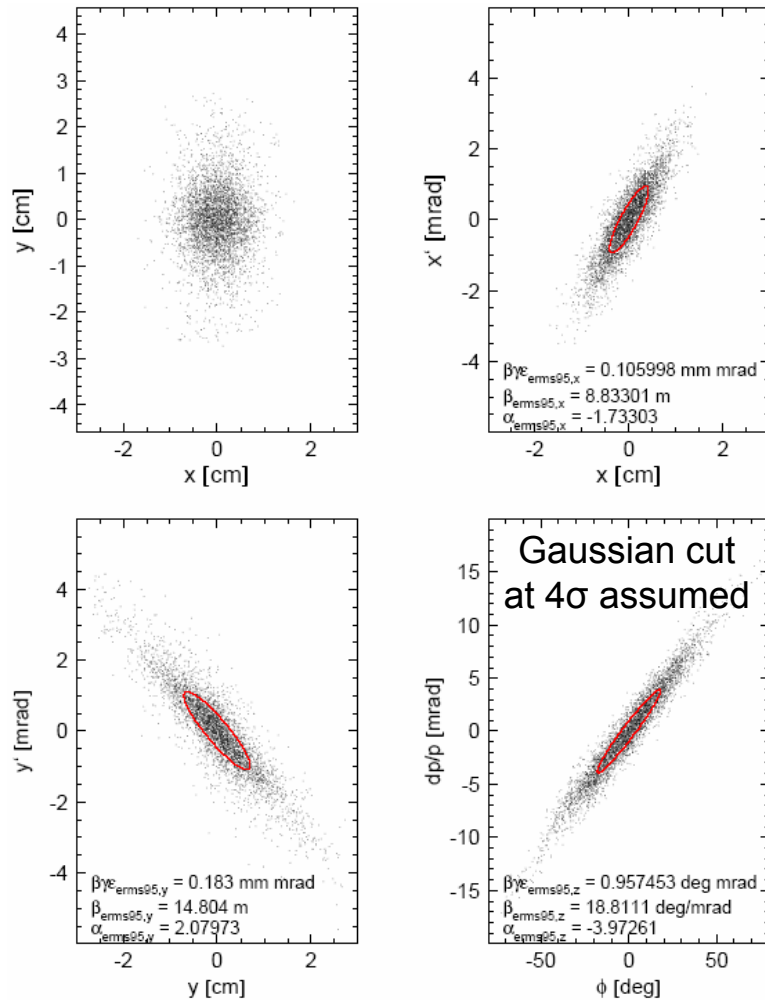
simulations with four different codes as used by the participating labs:

DYNAMION (GSI)

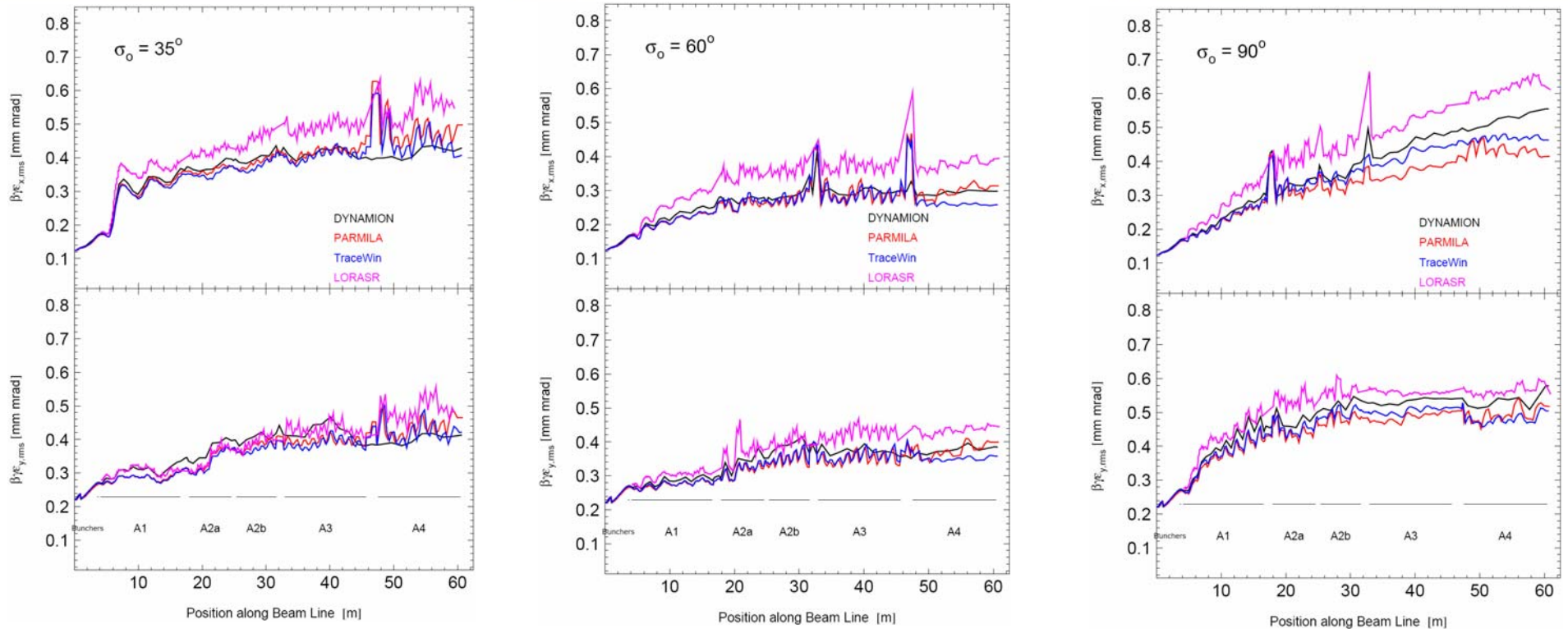
PARMILA (SNS)

TraceWin (CEA/Saclay)

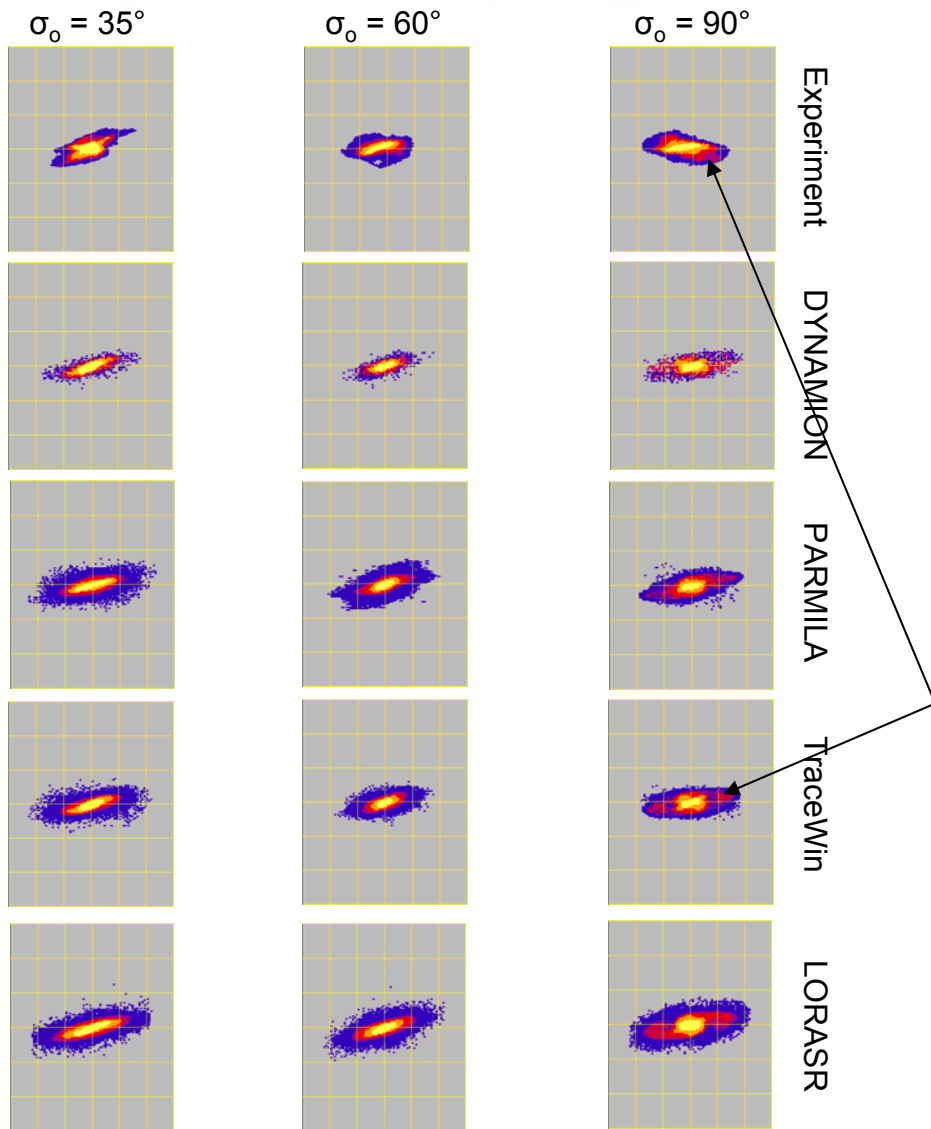
LORASR (Univ. of Frankfurt)



| | Solver | Boundaries | No. of Part. | CPU Time | Rf-Gap |
|----------|----------------|------------|------------------|----------|------------------|
| DYNAMION | 3D-part.-part. | open | $4.3 \cdot 10^3$ | 20 h | tracking |
| PARMILA | PICNIC-3D | open | $2 \cdot 10^5$ | 30 min. | non-linear kicks |
| TraceWin | PICNIC-3D | open | $2 \cdot 10^5$ | 30 min. | non-linear kicks |
| LORASR | PICNIC-3D | open | $2 \cdot 10^5$ | 1 h | tracking |



- growth occurs mainly along first two tanks
- lowest growth at intermediate phase advances

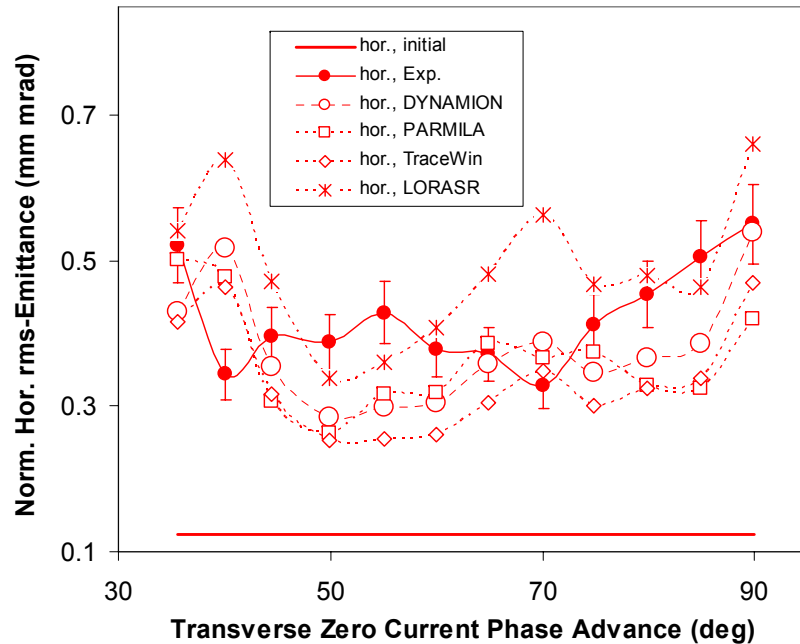


| | Int / Int_max [%] |
|--|-------------------|
| | 0 – 5 |
| | 5 – 10 |
| | 10 – 20 |
| | 20 – 40 |
| | 40 -100 |

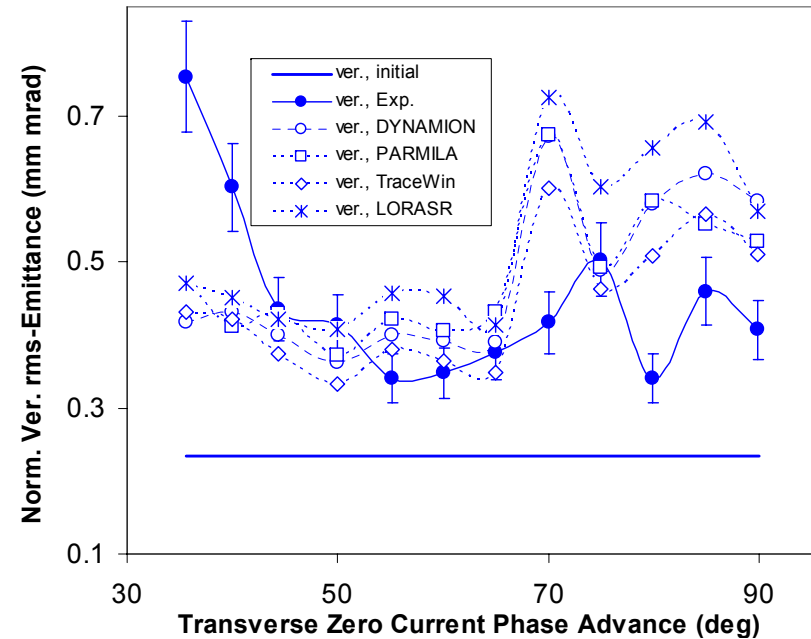
- core: good agreement (ex. 35°)
- 90°: "wings" seen in exp. & sims
- deviations at lowest densities (halo)



horizontal



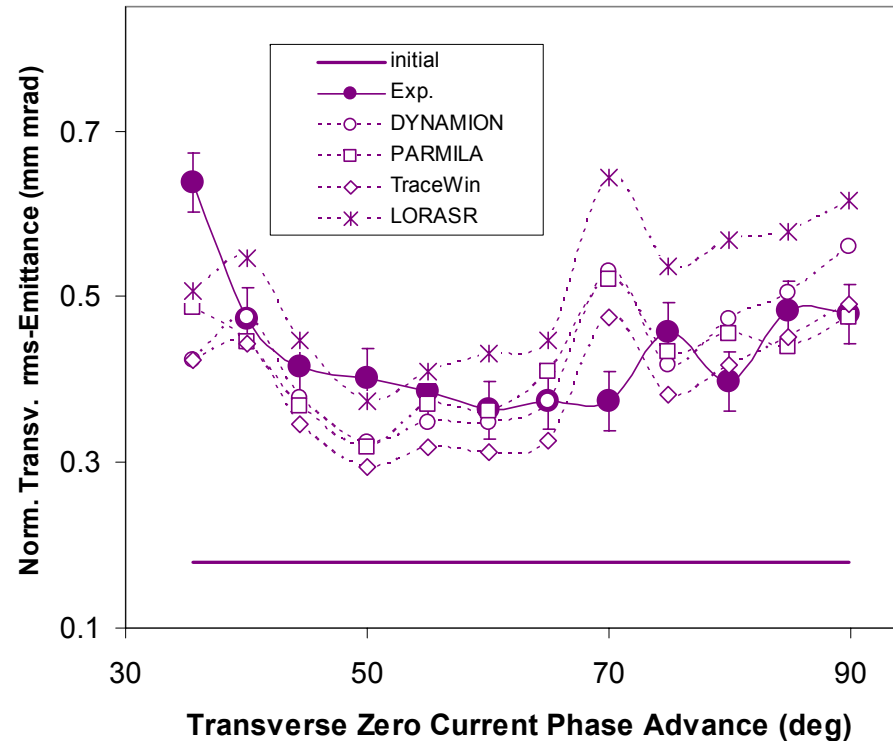
vertical



- codes reproduce the dependence on phase advance qualitatively
- differences w.r.t. to absolute final emittance values



(horizontal + vertical) / 2



- quantitative agreement among codes better for the sum of transverse emittances
- reduced fluctuation of data points w.r.t. average behavior
- experimental data within bandwidth of codes



matching including space charge is based on rms envelope tracking following a system of coupled diff. eqs*

horizontal
$$a_x'' + \kappa_x(s)a_x - \frac{\epsilon_{r,x}^2}{a_x^3} - \frac{3K_3(1-f)}{(a_x + a_y)a_z} = 0$$

vertical
$$a_y'' + \kappa_y(s)a_y - \frac{\epsilon_{r,y}^2}{a_y^3} - \frac{3K_3(1-f)}{(a_x + a_y)a_z} = 0$$

and

rms beam sizes
ext. foc. strengths

beam emittance
beam current

longitudinal
$$a_z'' + \kappa_z(s)a_z - \frac{\epsilon_{r,x}^2}{a_z^3} - \frac{3K_3f}{a_x a_y} = 0$$

We have defined a three-dimensional space-charge parameter

$$K_3 = \frac{qI\lambda}{20\sqrt{5}\pi\epsilon_0 mc^3 \gamma^3 \beta^2} \quad [m]$$

*Th. Wrangler: "RF Linear Accelerators", Wiley Interscience, p. 278, (1998)



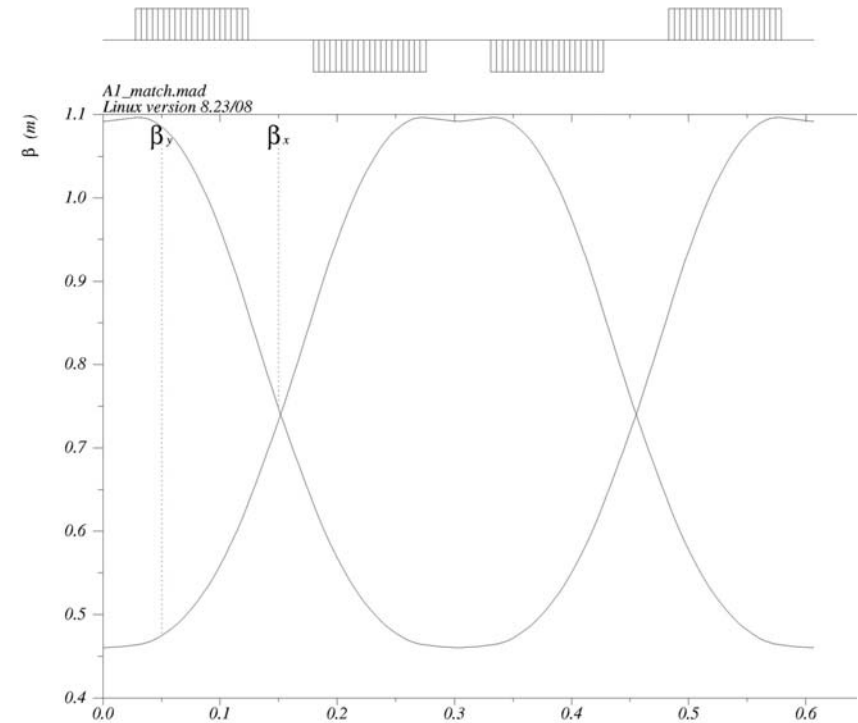
at entrance to first DTL cell (rms):

- $\epsilon_x, \epsilon_y, \epsilon_z$ given by initial distribution
- $\beta_{x,i}, \beta_{y,i}, \beta_{z,i}$ guessed at first iteration
- $\beta_{x,i}, \beta_{y,i}, \beta_{z,i}$
- $\alpha_{x,i} = \alpha_{y,i} = \alpha_{z,i} = 0$!!!

rms tracking through complete F-D-D-F
DTL cell including 4 rf-kicks

obtain $\beta_{x,f}, \beta_{y,f}, \beta_{z,f}$ at cell exit

new iteration: $\beta_{x,i} = (\beta_{x,i} + \beta_{x,f}) / 2, \dots$



convergence after ≈ 25 iterations,
i.e. < 1 sec CPU time



- Twiss parameters at entrance to matching section are known (α_i, β_i)
- Twiss parameters at exit of section (α_f, β_f) depend on seven variables ($f_1 \dots f_7$)
- mismatch at DTL entrance from T. Wanglers definition; $\Delta\alpha = \alpha_f - \alpha_{\text{per}}$

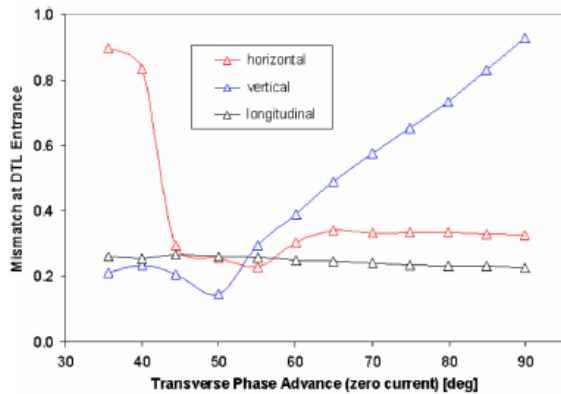
$$M = \left[1 + \frac{\Delta + \sqrt{\Delta(\Delta + 4)}}{2} \right]^{1/2} - 1$$

$$\Delta = (\Delta\alpha)^2 - \Delta\beta\Delta\gamma,$$

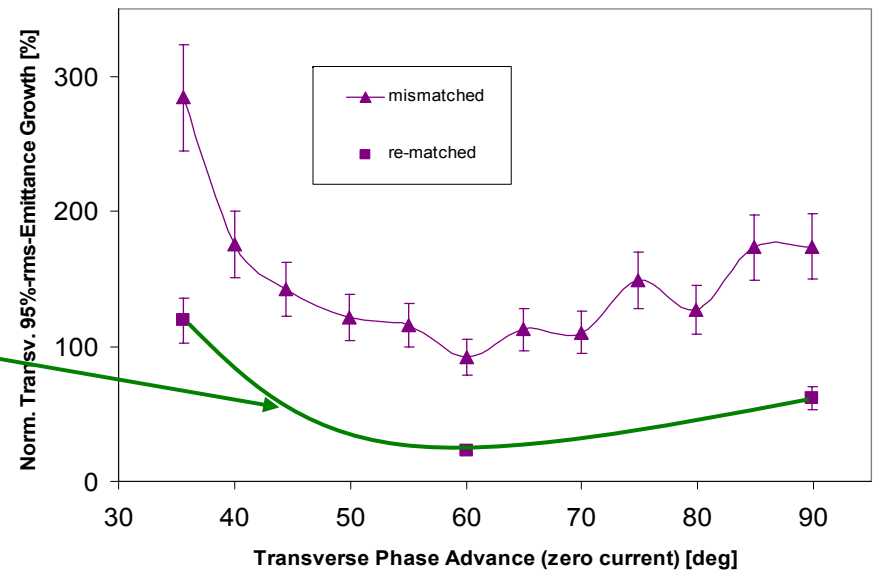
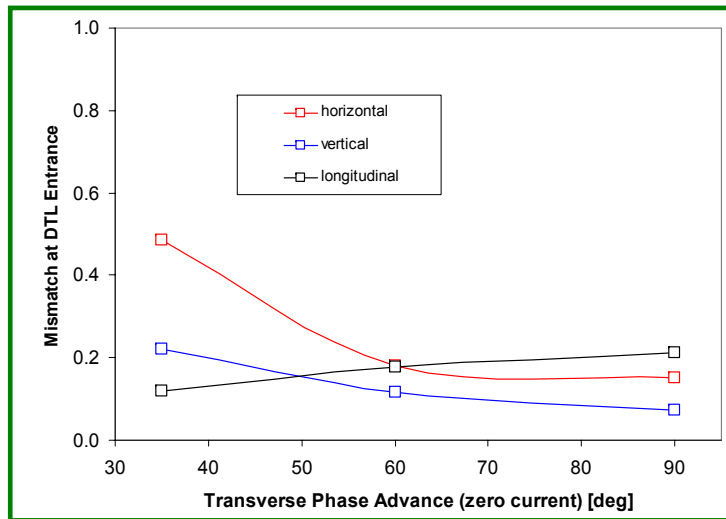
- define function $F(f_1 \dots f_7) := M_x^3(\dots) + M_y^3(\dots) + M_z^3(\dots)$
- find ($f_1 \dots f_7$) that minimize F using *powell* routine from "Num. Recipes in C"



evaluation of mismatch of last measurement :

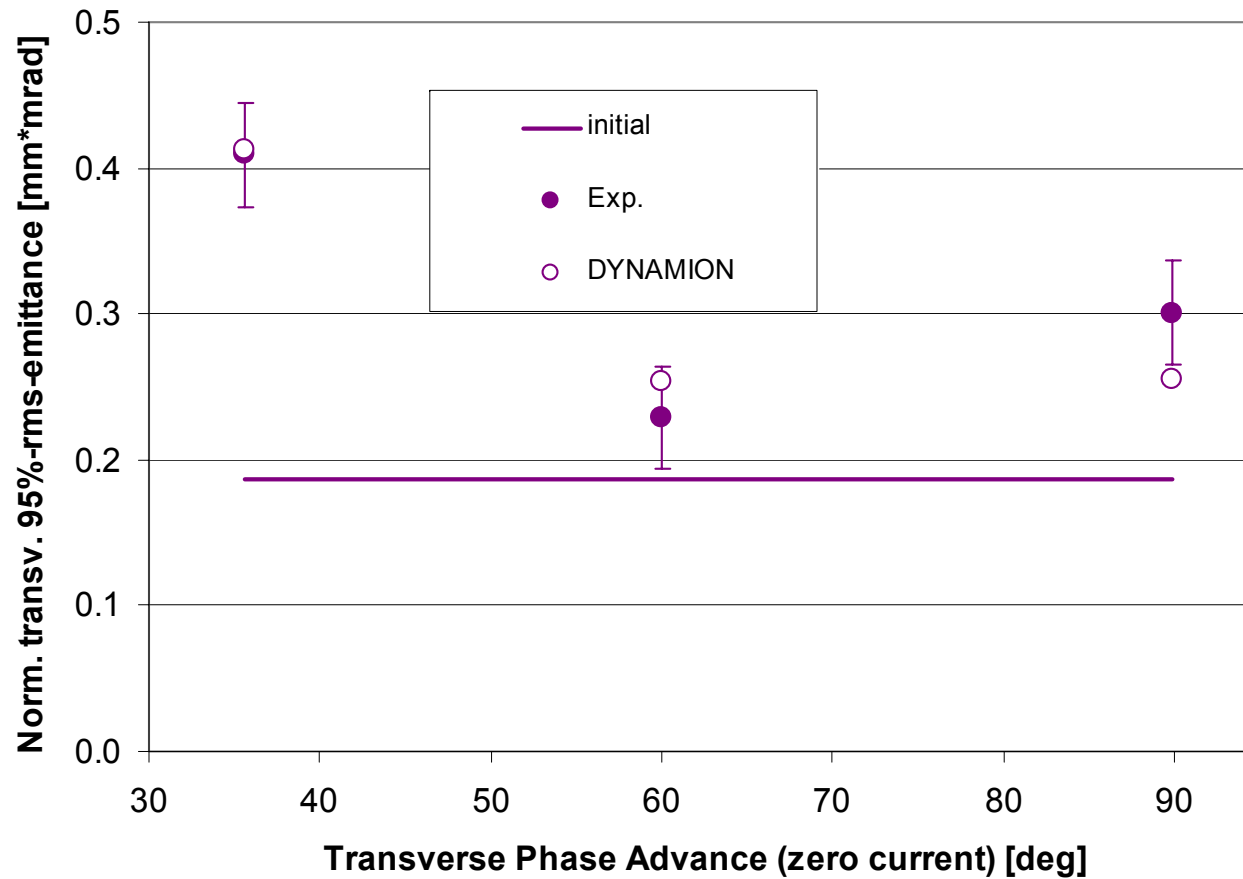


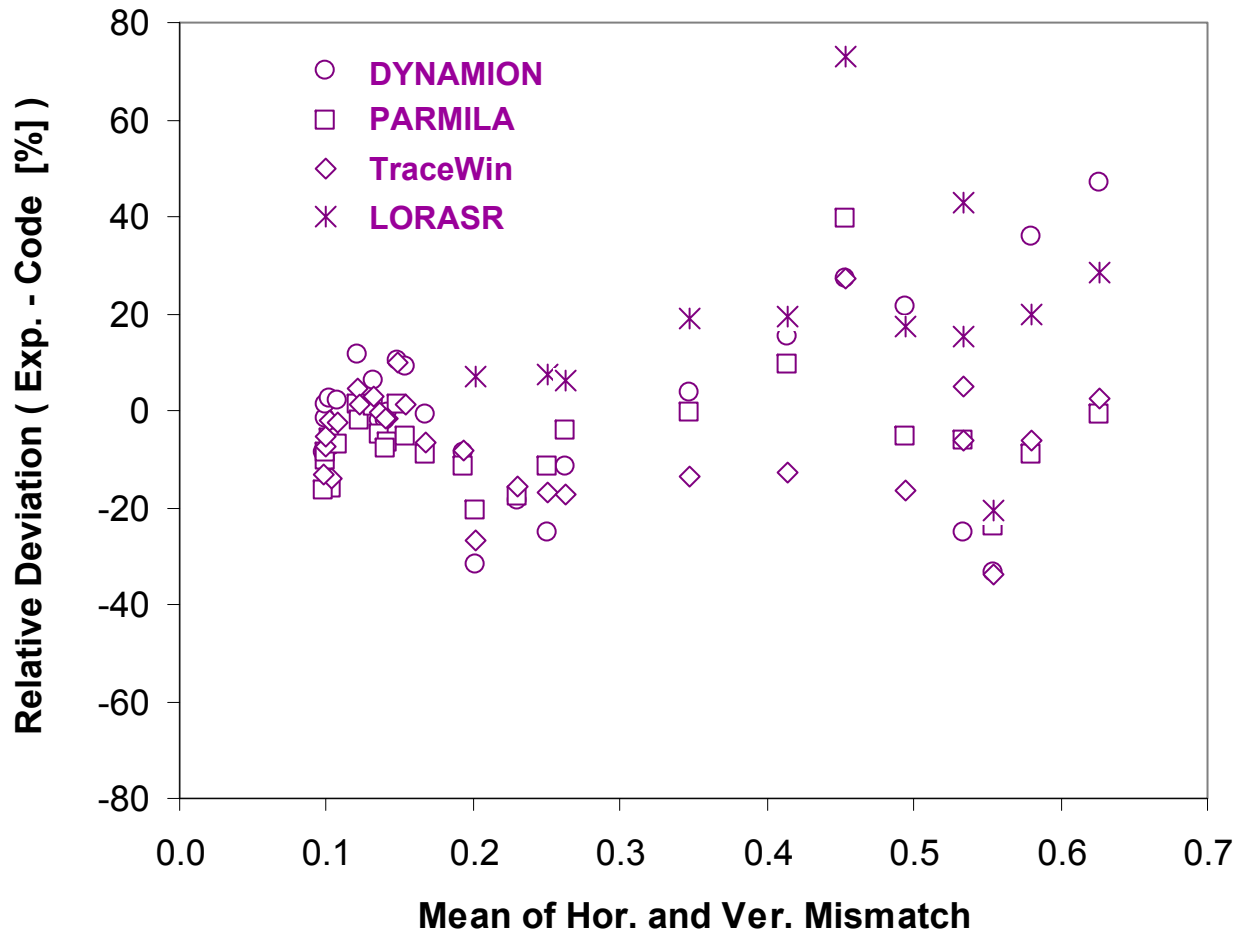
applying matching routine





reduced mismatch :







- assumption of a periodically breathing beam envelope with phase advance σ_{env}
- envelope has radial symmetry
- single particle experiences:
 - constant external focusing with σ_o
 - electric field of breathing envelope

envelope charge density depends on radius r :

$$\rho(r) = \rho_o(s) \cdot \left[1 - \frac{r^2}{R(s)^2} \right], \quad r \leq R(s) \quad \text{density component (r}^2\text{), } r^{\geq 4} \text{ neglected}$$

creating a field :

$$E_r = \frac{18 \cdot I}{\pi \epsilon_o \cdot R(s)^2 \beta c} \left[r - \frac{r^3}{2R(s)^2} \right], \quad r \leq R(s) \quad \text{octupolar field component (r}^3\text{)}$$



single particle motion driven by two components :

$$r'' = -\sigma_o^2 r + \frac{e \cdot q}{A \cdot m_u} \cdot E_r$$

↑
external quad focusing

↙
field from envelope (perturbation)

perturbed oscillator equation :

$$r'' + \sigma_o^2 r = a \cdot r^3 \cdot e^{i\sigma_{env}s} \quad \text{frequency of external perturbation from envelope breathing}$$

solution by ansatz :

$$r(s) \sim e^{-i\sigma_o s}$$

Plugging into oscillator equation :

$$r'' + \sigma_o^2 r \sim a \cdot e^{i(\sigma_{env} - 3\sigma_o)s}$$

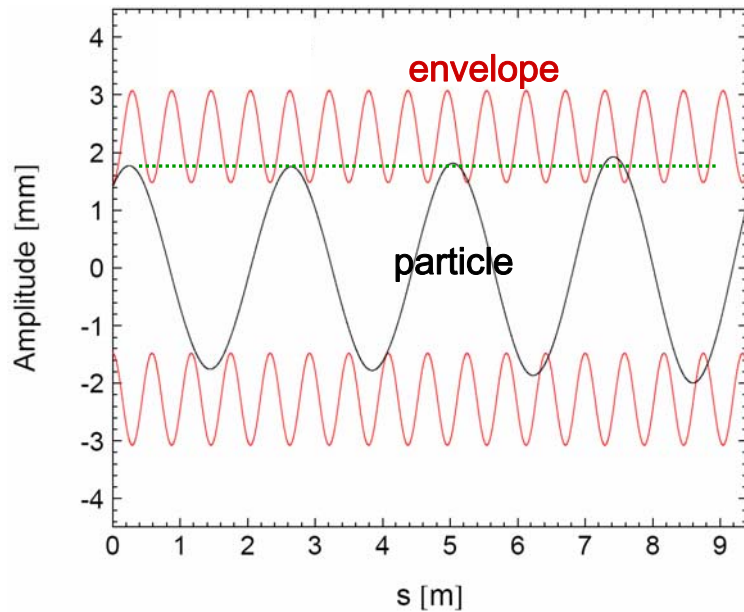
$$\text{resonance condition : } \sigma_{env} = 4\sigma_o$$

→ envelope oscillates 4 times faster than single particle



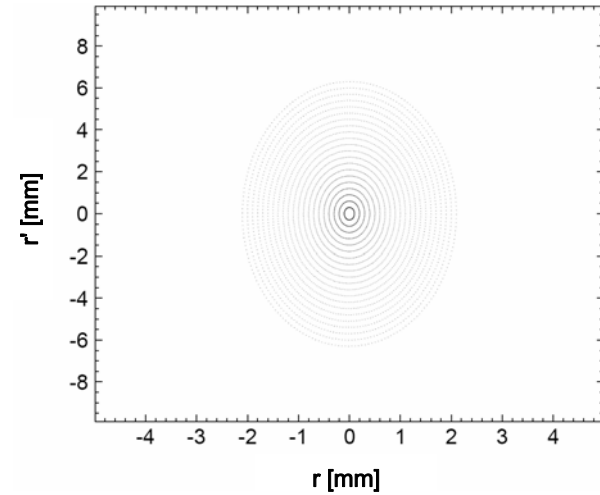
$f_{\text{oscillation}}(\text{envelope}) = 4 * f_{\text{oscillation}}(\text{particle})$

→ resonant excitation of single particle

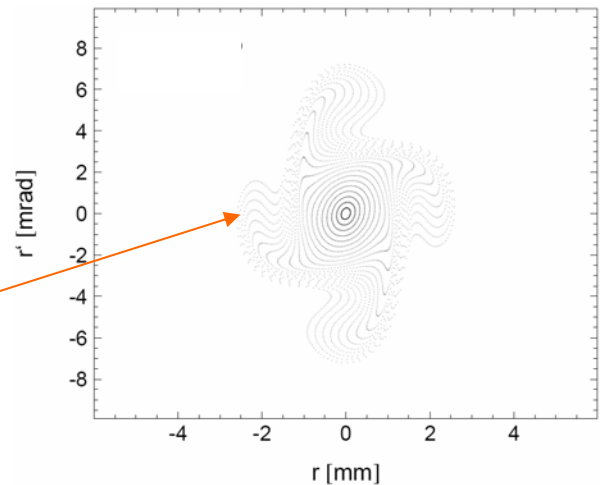


4 arms: characteristic feature of octupolar resonance

initial phase space distribution

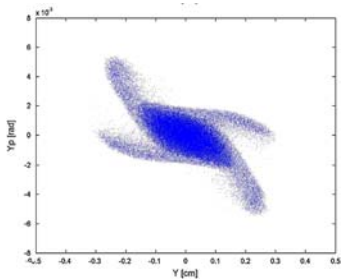


final phase space distribution



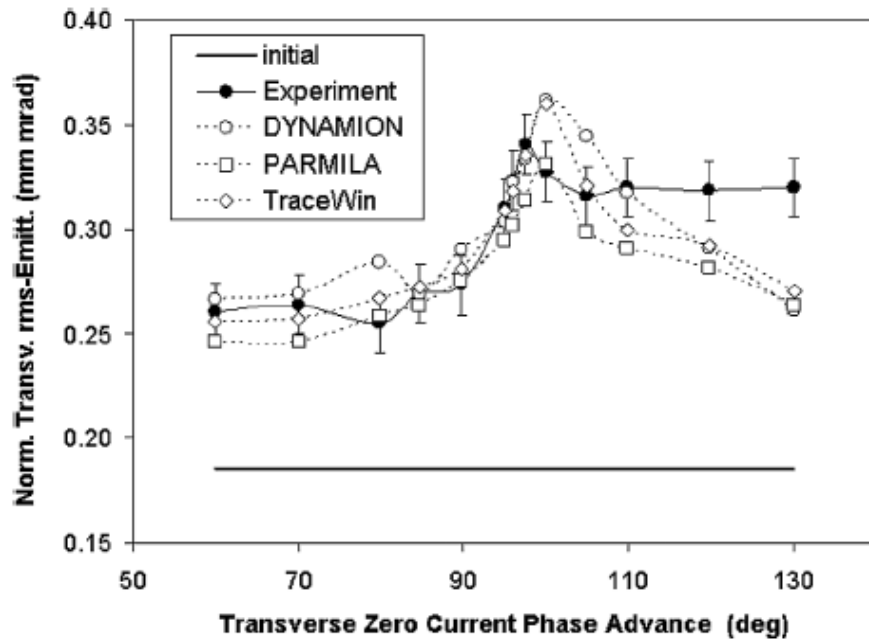
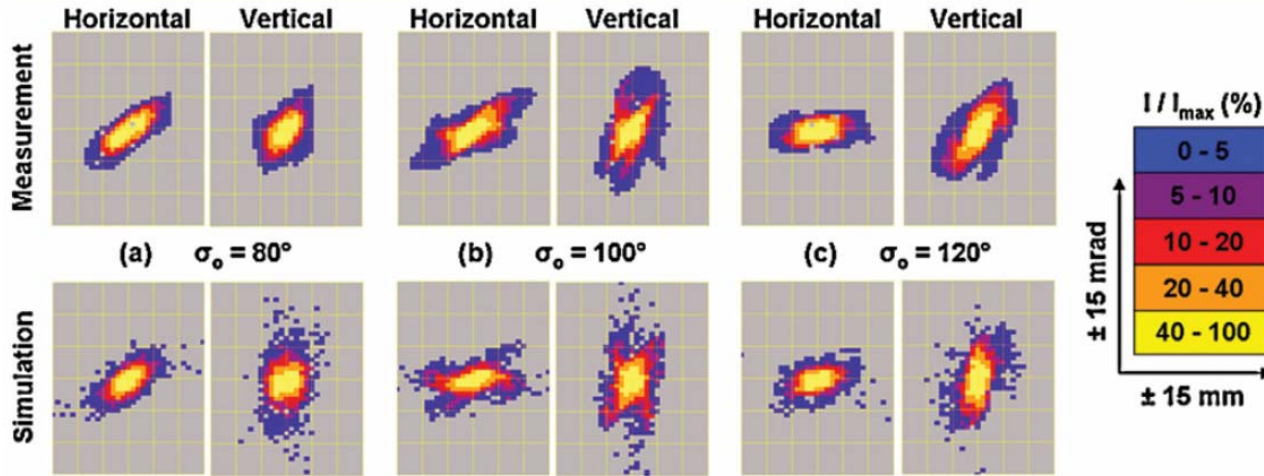


- never observed directly worldwide (linac nor ring) due to insufficient machine/beam control
- requires very small mismatch to assure envelope periodicity
- cannot be seen behind multi-tank DTL due to inter-tank mismatch
- simulations by D. Jeon (SNS) suggested to measure this resonance at GSI UNILAC



Experiment at GSI UNILAC :

- install beam emittance measurement unit after first DTL tank
- measure phase space distributions and rms emittances

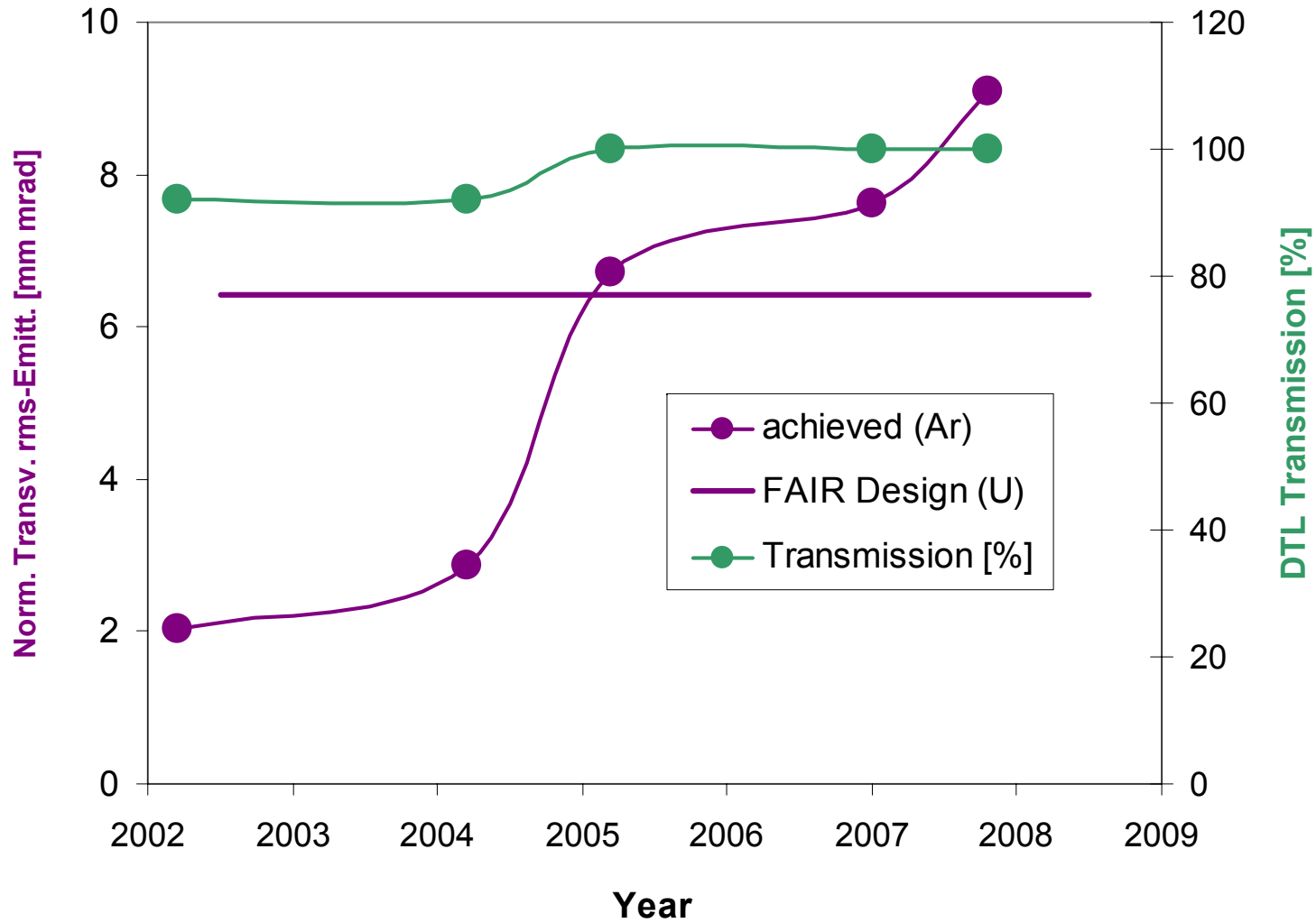


- 4 arms were observed
- strong emittance growth was observed



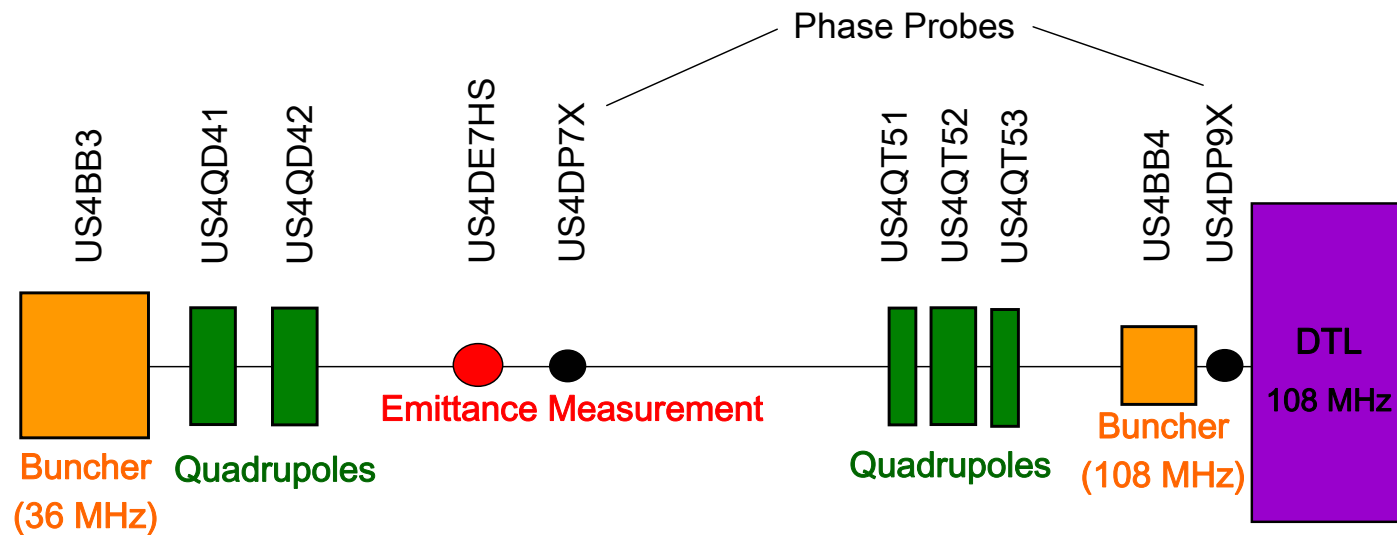
- **Codes describe well the behavior of sum of hor. and ver. emittances**
- **Within single planes:**
 - **considerable differences among codes**
 - **agreement between measurements and codes is just fair**
- **Reliability of codes increases with quality of matching**
- **Differences among codes decrease with quality of matching**
- **Agreement with measurements does not depend on number of particles**
- **Experimental evidence for octupolar space charge resonance in linear accelerator**







- after periodic solution assumed to be known
- section prior to DTL needs to be set to exactly match this solution
- seven available knobs: five quadrupoles, 2 bunchers



- seven variables to minimize one value → sum of mismatches in hor., ver. and long.
- envelope equations + numerical recipes (Powell routine) can do the job (theoretically)



| Input | | |
|-------------------------------------|--|----------|
| I_mean [emA]: | | 9.5 |
| q: | | 10.0 |
| A: | | 40.00 |
| beta_rel: | | 0.054638 |
| rf-freq [MHz]: | | 108.408 |
| unnorm. hor. rms-emit. [mm mrad]: | | 3.0 |
| meas. hor. beta-func. [m]: | | 5.33 |
| meas. hor. alpha: | | 2.09 |
| unnorm. ver. rms-emit. [mm mrad]: | | 2.25 |
| meas. ver. beta-func. [m]: | | 11.49 |
| meas. ver. alpha: | | 4.94 |
| unnorm. long. rms-emit. [deg mrad]: | | 50.0 |
| meas. long. beta-func. [deg/mrad]: | | 22.175 |
| meas. long. alpha: | | 3.379 |
| MAZ of first A1 cell: | | 4.5 |
| During US4-emitt. measurement: | | |
| Strength of US4QD41 [1/m]: | | 2.139 |
| Strength of US4QD42 [1/m]: | | -2.090 |
| Strength of US4QT51 [1/m]: | | 0.905 |
| Strength of US4QT52 [1/m]: | | -2.839 |
| Strength of US4QT53 [1/m]: | | 2.911 |
| Slider of US4BB3 [V]: | | 4.0 |
| Slider of US4BB4 [V]: | | 0.0 |

Best fitting settings are:

$q_{US4QD41} = 1.982 \text{ 1/m}$
 $q_{US4QD42} = -1.852 \text{ 1/m}$
 $q_{US4QT51} = 0.833 \text{ 1/m}$
 $q_{US4QT52} = -3.254 \text{ 1/m}$
 $q_{US4QT53} = 2.659 \text{ 1/m}$
 $sl_{BB3} = 4.278 \text{ V}$
 $sl_{BB4} = 0.881 \text{ V}$

Output

Best fitting Twiss parameters are:

$\beta_x = 1.847 \text{ m}$
 $\alpha_x = 0.104$
 $\beta_y = 0.887 \text{ m}$
 $\alpha_y = 0.050$
 $\beta_l = 3.073 \text{ deg/mrad}$
 $\alpha_l = -0.458$

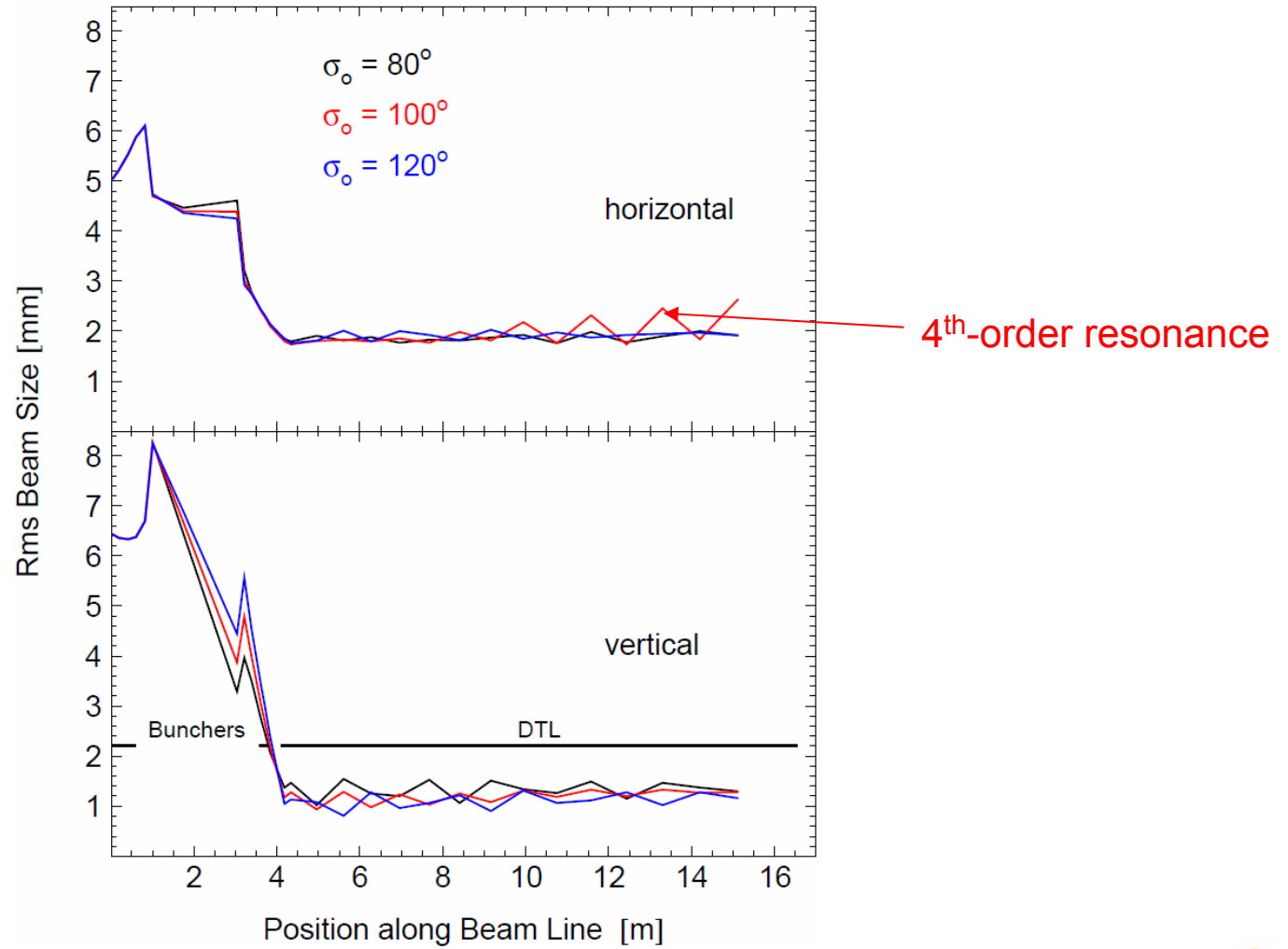
remaining mismatch: 0.02

Periodic solution before 1st gap of Alvarez Tank I:

$\beta_x = 1.85 \text{ m}, \quad \alpha_x = 0.10, \quad D\Phi_x = 29.7^\circ$
 $\beta_y = 0.89 \text{ m}, \quad \alpha_y = 0.05, \quad D\Phi_y = 26.6^\circ$
 $\beta_l = 2.40 \text{ }^\circ/\text{mrad}, \quad \alpha_l = -0.11, \quad D\Phi_l = 34.7^\circ$

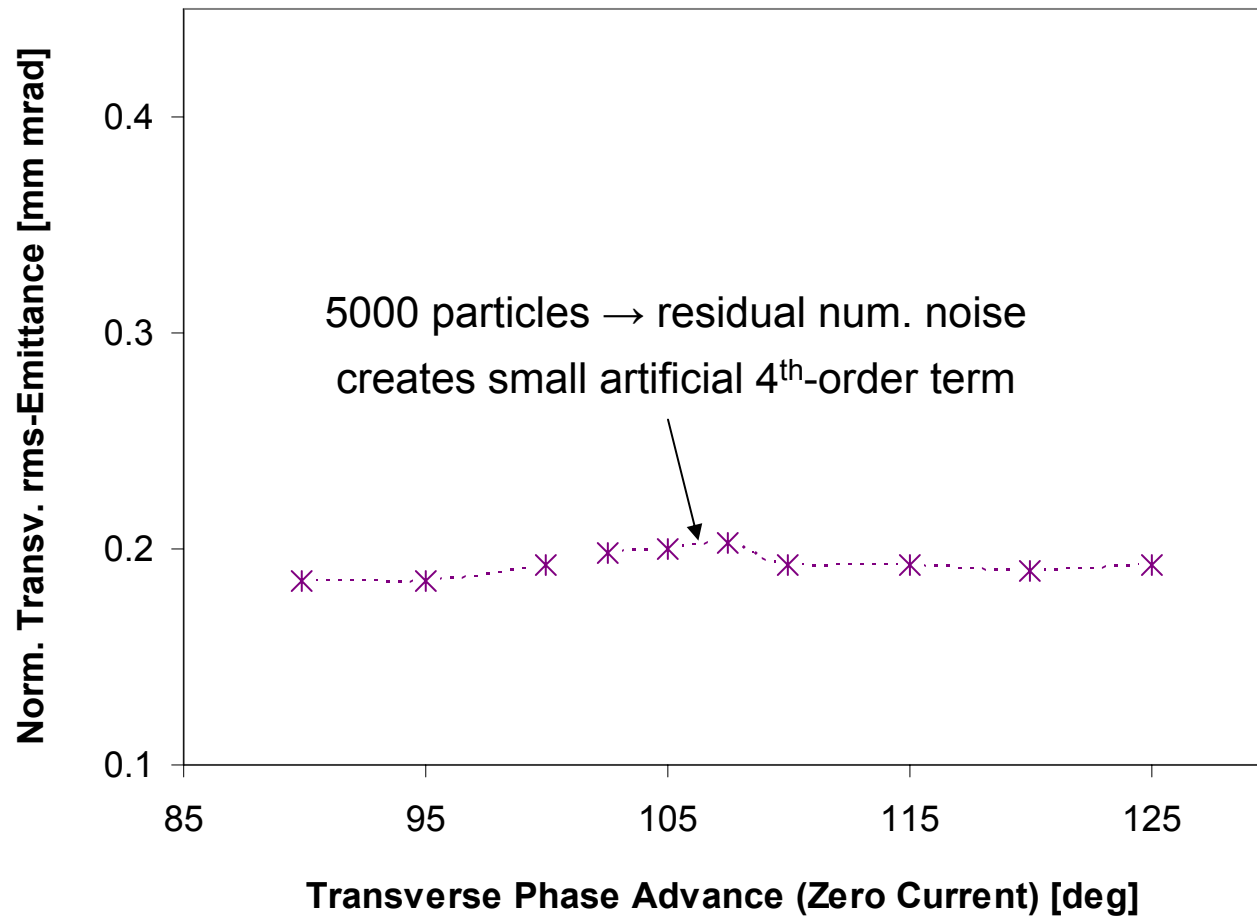


Simulated envelopes → no instability at $\sigma_o > 90^\circ$





Simulation with KV distribution → no significant growth
(KV has no 4th-order potential term)



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| Telefon | +18314572200 |
| Fax | +18314572221 |
| E-Mail | westcliffinn@foursisters.com |
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| Ankunft | Freitag, 28. August 2009, anreise 15:00 – 20:00 |
| Abreise | Sonntag, 30. August 2009, abreise 08:00 – 12:00 |
| Anzahl | 1 Zimmer |

Gesamtpreis **US\$ 550.00**

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| ✓ Steuer (10%) | US\$ 50.00 + |
| Gesamtpreis für dieses Zimmer | US\$ 550.00 |

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- In dem Zimmer ist Platz für ein Zustellbett/Babybett.

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|  | Kompakt Dodge Caliber Automatic oder vergleichbar 4 Passagiere, 2 Taschen, 2/4 Türen |  | € 27.6 /Tag | BUCHUNG |
|  | Zwischengröße Chrysler Sebring Automatic oder vergleichbar 5 Passagiere, 4 Taschen, 2/4 Türen |  | € 28.49 /Tag | BUCHUNG |

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