

PARTICLE TRACKING SIMULATION WITH SPACE CHARGE EFFECTS FOR AN INDUCTION SYNCHROTRON

AND PRELIMINARY APPLICATION TO THE KEK DIGITAL ACCELERATOR

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Abstract

In order to study the beam behaviour of the induction synchrotron which features low energy injection, a dedicated particle tracking simulation code with a 2.5D space charge field solver, which takes into account of the boundary condition, has been developed. The beam dynamics included in this code are discussed and simulation results assuming parameters of the KEK Digital Accelerator are presented. This code will help to understand the various features of the beam behaviour in the present beam commissioning



and serve as a tool for the design of the future induction synchrotrons.

Scheme Design $\vec{x} = (x, xp, y, yp, z, dpp)$ $x(s) \xrightarrow{K_{sc}} x(s)' \xrightarrow{M} x(s + \Delta s)$ $\vec{x}_{sc} = (0, \frac{\Delta s \cdot Qe}{\gamma_0^2 p_0 \beta_0 c} E_x, 0, \frac{\Delta s \cdot Qe}{\gamma_0^2 p_0 \beta_0 c} E_y, 0, \frac{\Delta s \cdot Qe}{\beta_0^2 E_{sc}} E_z)$

2.5D Space Charge Solver



Preliminary Application



Finite method for Poisson's equation



 $\phi(\Delta + x, y) + \phi(x, \Delta + y) - 4\phi(x, y) + \phi(x - \Delta, y) + \phi(x, y - \Delta)$

 $=-\frac{\rho(x,y)}{\Lambda^2}$ $\mathcal{E}_{_{0}}$

Boundary Matrix

Summary & Future work

A general simulation code considering the beam induced space charge

Potential Charge density fields with boundary conditions for the induction synchrotron.



✓ A 2.5D "slice-by-slice" scheme and space charge solver

Preliminary application to the KEK-DA.

> Further study with the simulation to understand the beam behaviour in

the KEK-DA ring will be continued and this simulation code can also be

applied to the future induction synchrotron's design and study.



