

# Synchrotron frequency shift as a probe of the CERN SPS reactive impedence

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# Outline

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Introduction and motivations

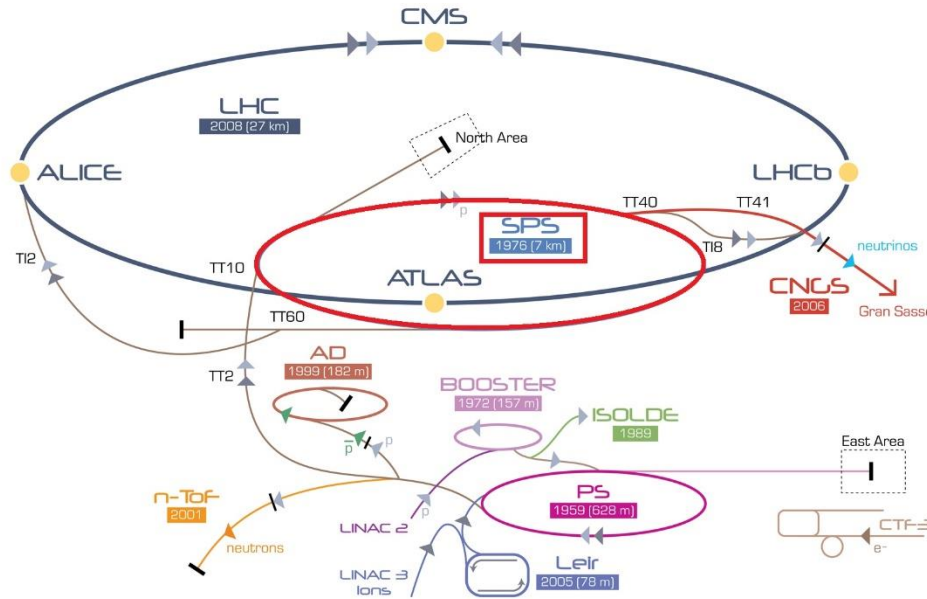
Measurements

Simulations

Analytical results

Conclusions

# Introduction and motivations



- ❑ The **HL-LHC project** at CERN requires an **increase of intensity**, but **intensity requirements cannot be fulfilled** for the moment in the **SPS**, one of the reason being **longitudinal instabilities**.
- ❑ A **detailed impedance model** is under development in order to simulate intensity effects and **identify the source of the instabilities**.
- ❑ This **model was tested** against sets of measurements **to proof its accuracy**.

# Quadrupole frequency shift

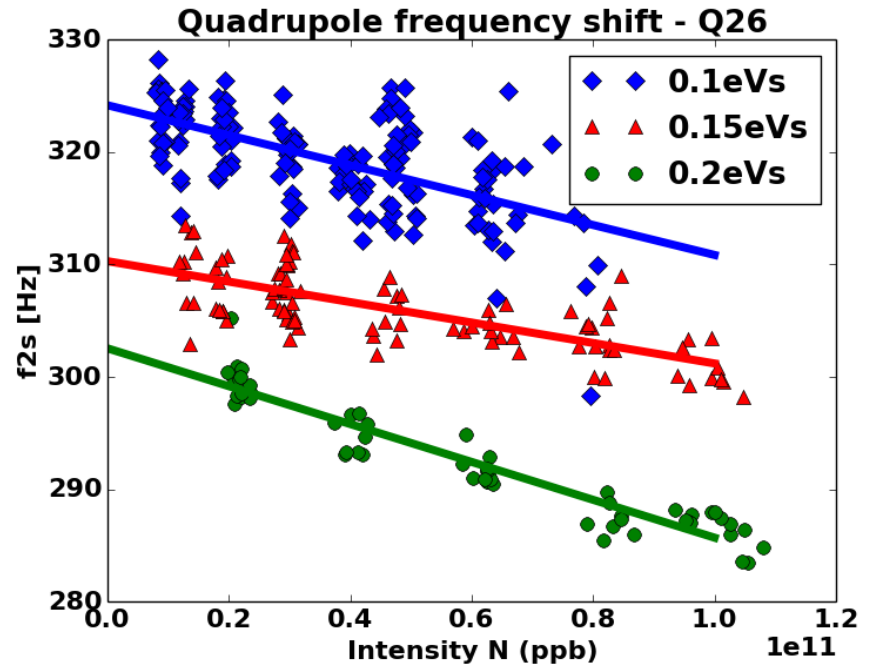
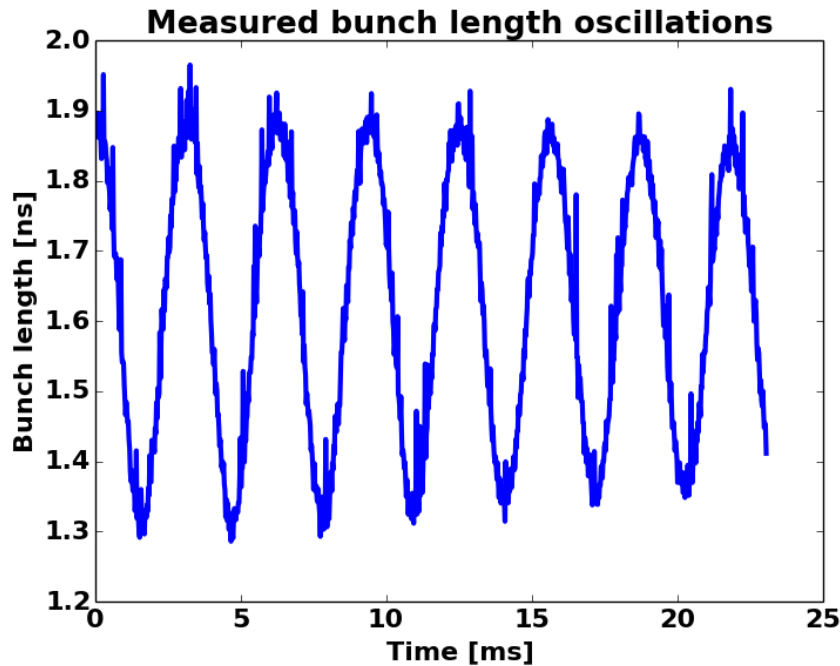
- **Bunch length oscillations** (quadrupolar  $m = 2$ ) at injection in the SPS (26 GeV/c, **above transition**) are measured and analyzed in order to measure the **synchrotron frequency shift as a function of intensity**.
- This shift is due to the convolution of the **reactive part of the impedance** and the bunch spectrum, and is divided in two contributions : the **incoherent frequency shift** (from the stationary bunch distribution) and the **coherent frequency shift** (from the perturbation) [1]

$$f_{s,m}(N_b) \approx m f_s^{(0)} + m \Delta f_{inc}(N_b) + \Delta f_{coh}(m, N_b)$$

- Measurements and simulations were compared in order to test the current SPS impedance model, and a **dependence on emittance (~ bunch length) and distribution type** was observed and analyzed.

# Measurement method

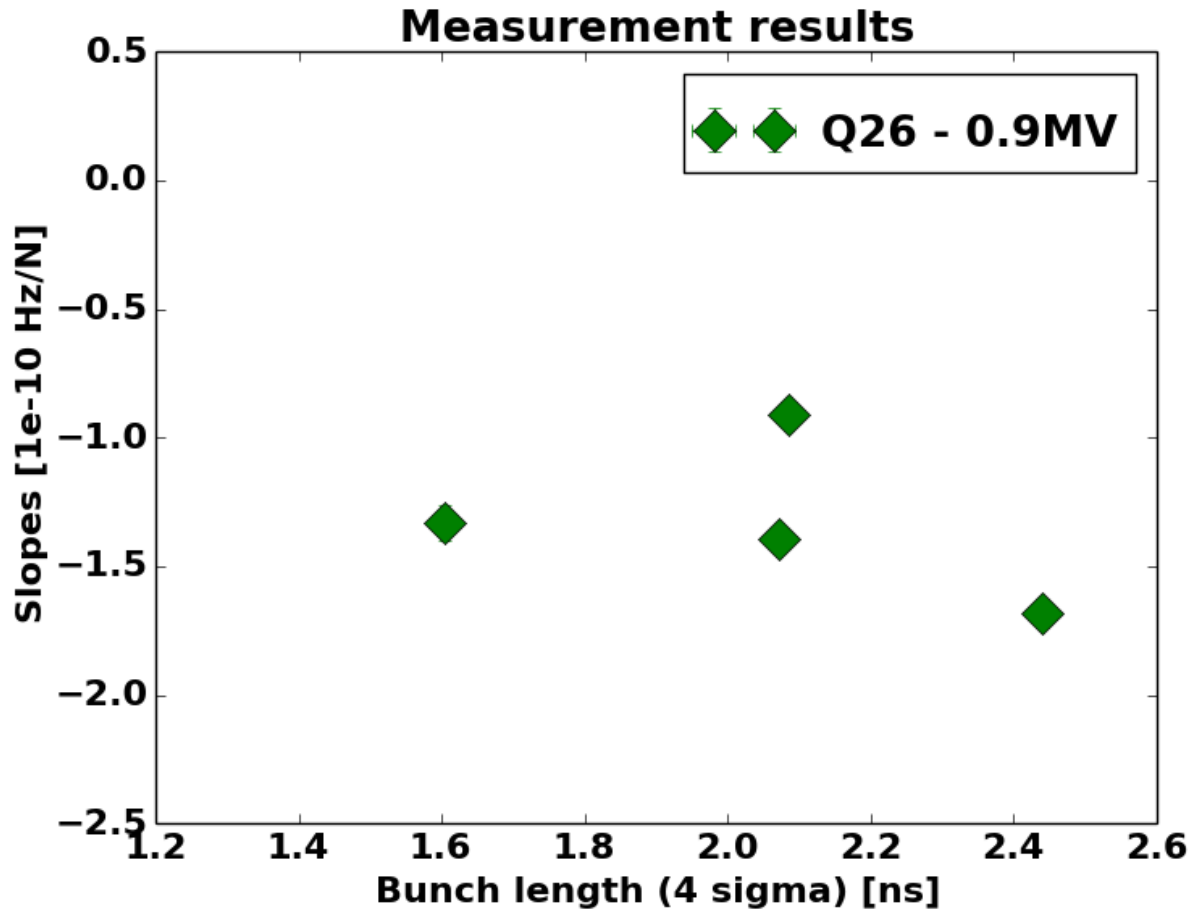
- ❑ A mismatch bunch is injected in the SPS and its quadrupole oscillations are measured and analyzed



- ❑ Bunch length is defined as  $\tau = 4\sigma_{RMS}$

- ❑ Scanning intensities ( $1 \cdot 10^{10}$  to  $8 \cdot 10^{10}$ ) and emittances (0.1 eVs to 0.2 eVs)

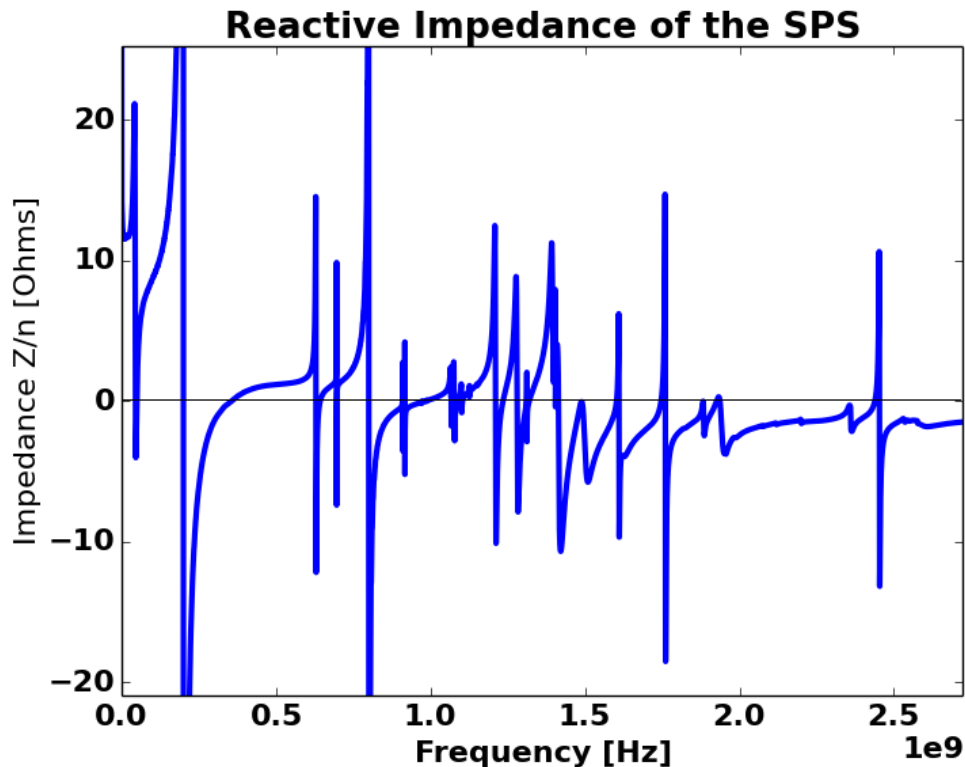
# Measurement results – Q26



- Each point in simulations corresponds to the slope of the quadrupole frequency shift as a function of intensity, for bunches of the same bunch length.

# Impedance model

## □ Actual SPS impedance model [2]

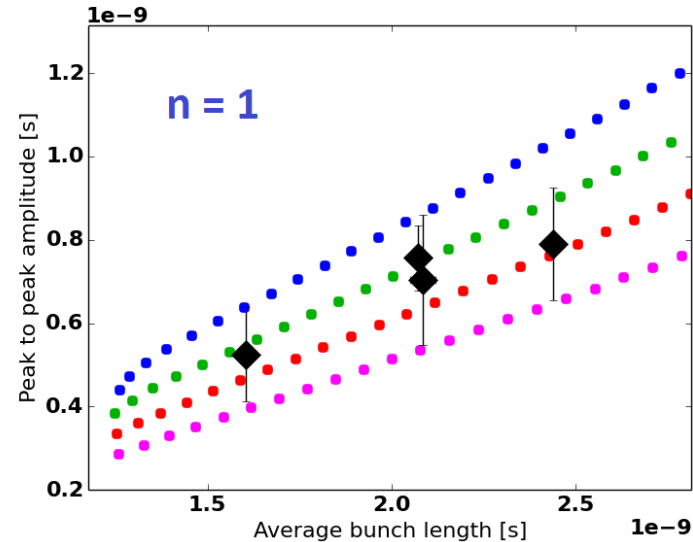
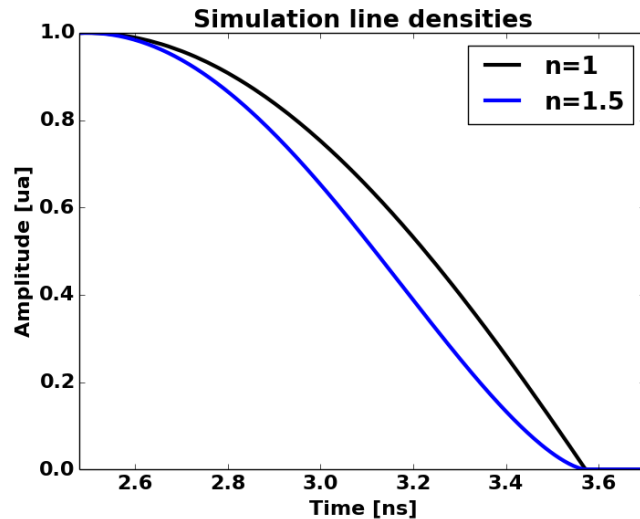


Main reactive impedance ( $\Im[Z/(f/f_0)]$ ):

- Kickers (inductive,  $5.5\Omega$ )
- Vacuum flanges (inductive,  $0.5\Omega$ )
- RF systems (capacitive)
- Space charge (capacitive,  $-1.0\Omega$ ) [3]

# Simulation method

- Using **BLoND simulation code** [4]



- Binomial profile at injection

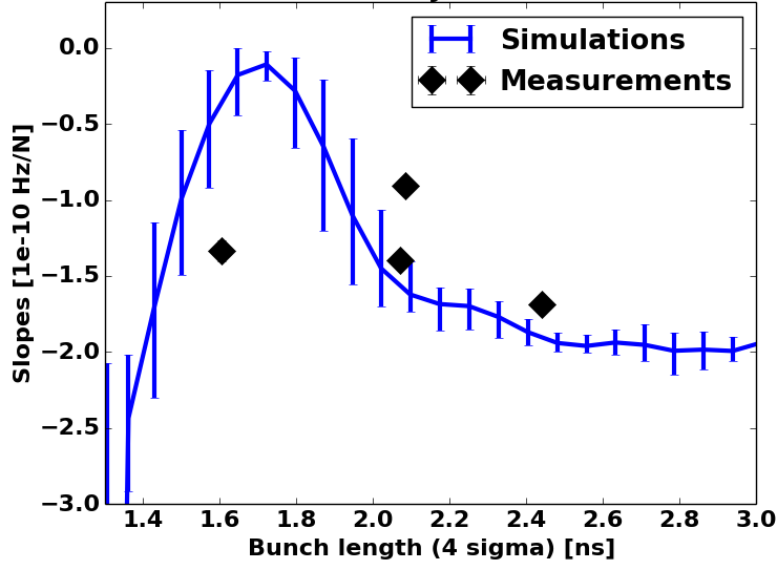
$$\lambda(t) = \lambda_0 \left[ 1 - \left( \frac{t}{\tau} \right)^2 \right]^n ; n = 1: \textit{Parabolic line density}$$

- The **bunch length  $\tau$** , the **intensity** and the **momentum spread are scanned**, in order to cover the full panel including measurements

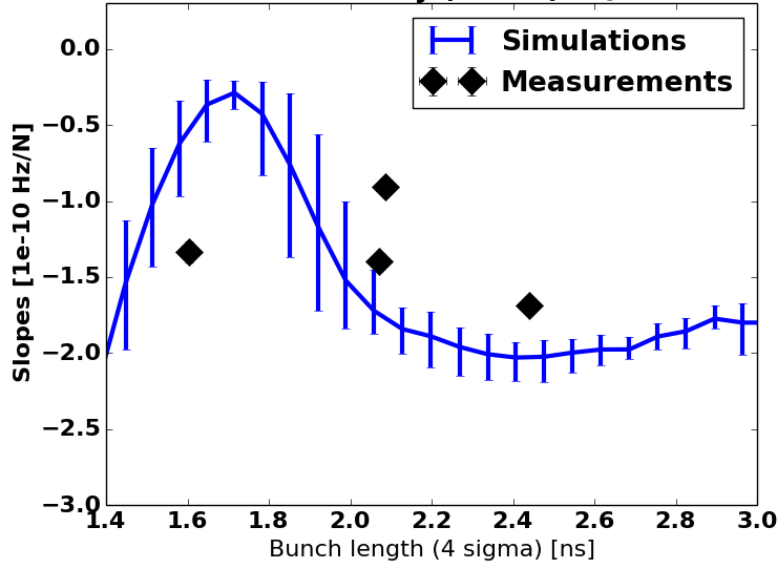


# Simulation results – Q26

Binomial line density ( $n=1$ ) - Q26 0.9MV

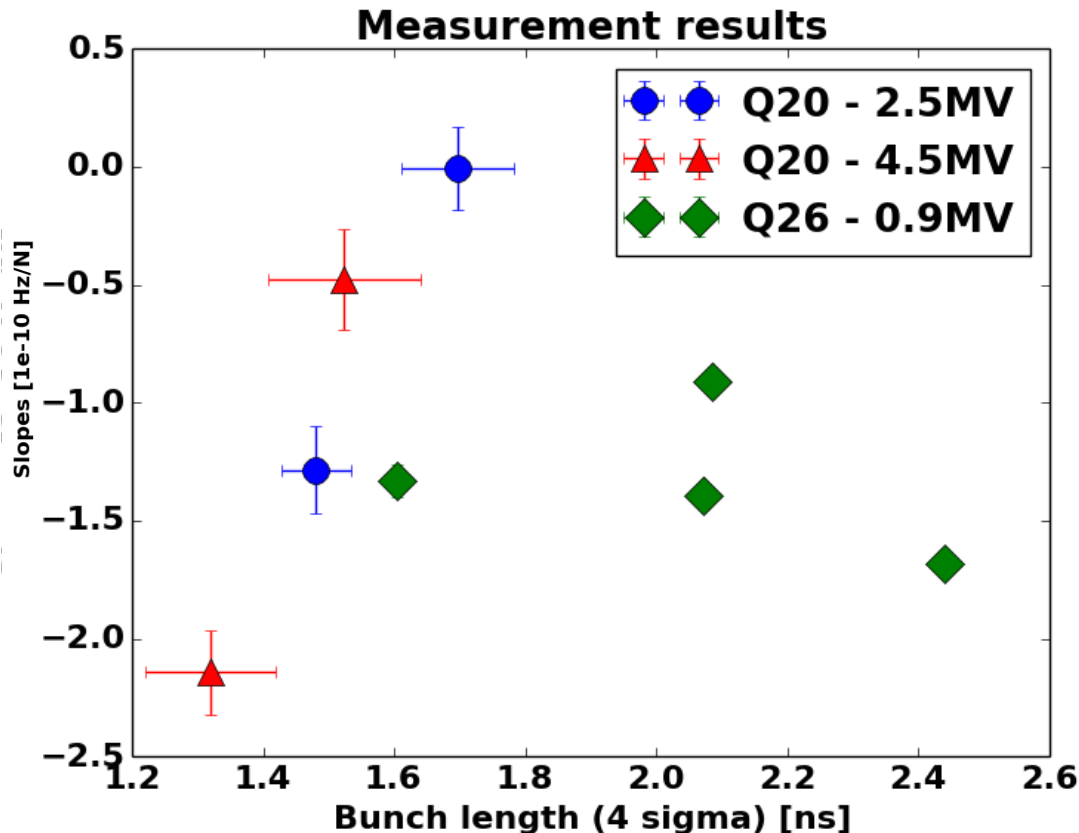


Binomial line density ( $n=1.5$ ) - Q26 0.9MV



- ❑ A **non monotonous dependence** of the slope as a function of bunch length is observed in simulations
- ❑ The **error bars** in simulations corresponds to the range due to the different **momentum spreads**
- ❑ The **maximum is reduced** by **increasing  $n$**  in the binomial distribution.
- ❑ The simulations give a **good agreement** with measurements.

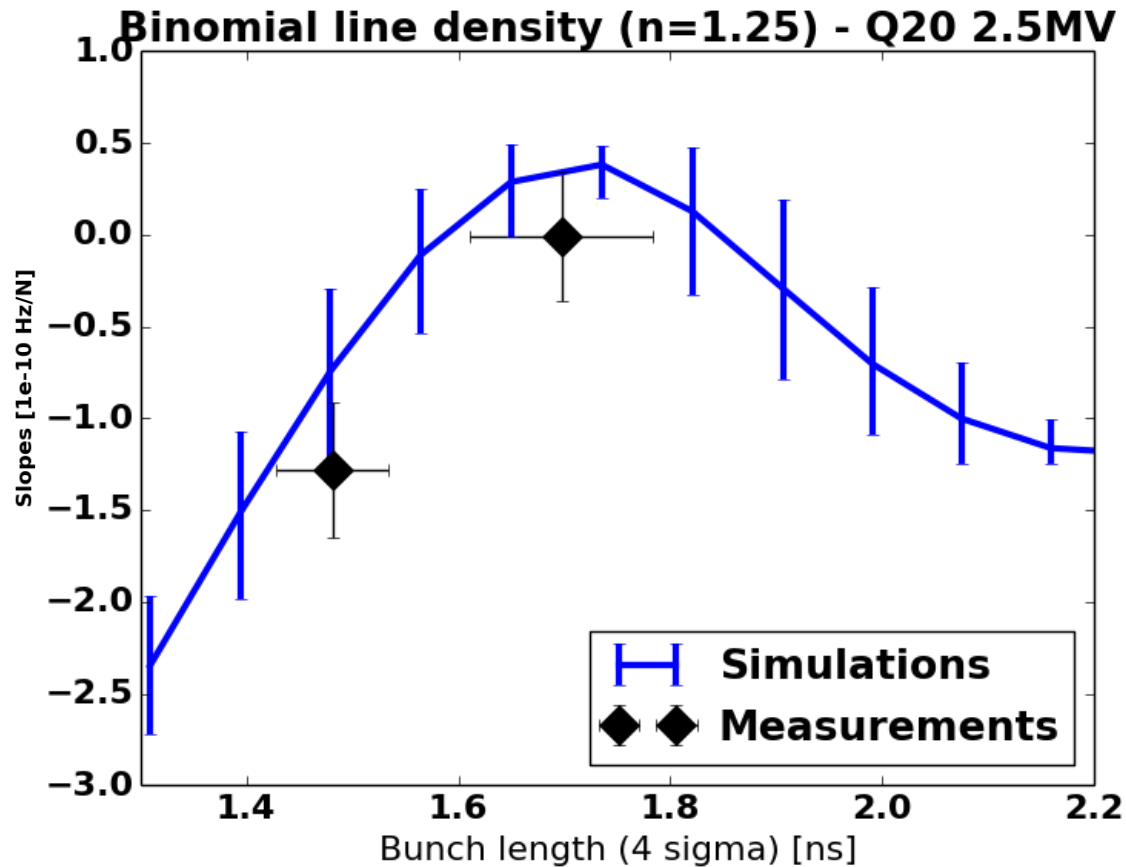
# Measurement results – Extended



□ Two different optics: Q26 and Q20 (slopes were **scaled to Q26 – 0.9MV** in order to be compared on the same plot).

□ **The Q20 measurements reveals the maximum around  $\tau = 1.7\text{ns}$ .**

# Simulation results – Q20



- The **same properties** were seen with simulations and measurements with the **Q20 optics**.

# Incoherent frequency shift

- Numerical computation of the **incoherent frequency shift** [5]
- This shift is due to the **stationary spectrum** of the bunch

$$f_s(N) \approx f_s^{(0)} \left( 1 + \frac{\alpha N Z_1}{2} \right)$$

$$Z_1 = \int_{-\infty}^{+\infty} \frac{df}{f_0} \sigma_0(f) \Im(Z(f)) \frac{J_1(f \hat{t})}{f_0 \hat{t}/2}$$

$f_s^{(0)}$  : synchrotron frequency

$Z_1$  : effective impedance

$\sigma_0$  : stationary bunch spectrum

$\hat{t}$  : single particle oscillations amplitude

- Above transition,  $\alpha < 0$ , so **inductive impedance give  $Z_1 > 0$**  so the **slope is steeper** (vice-versa for capacitive impedance)

# Coherent frequency shift

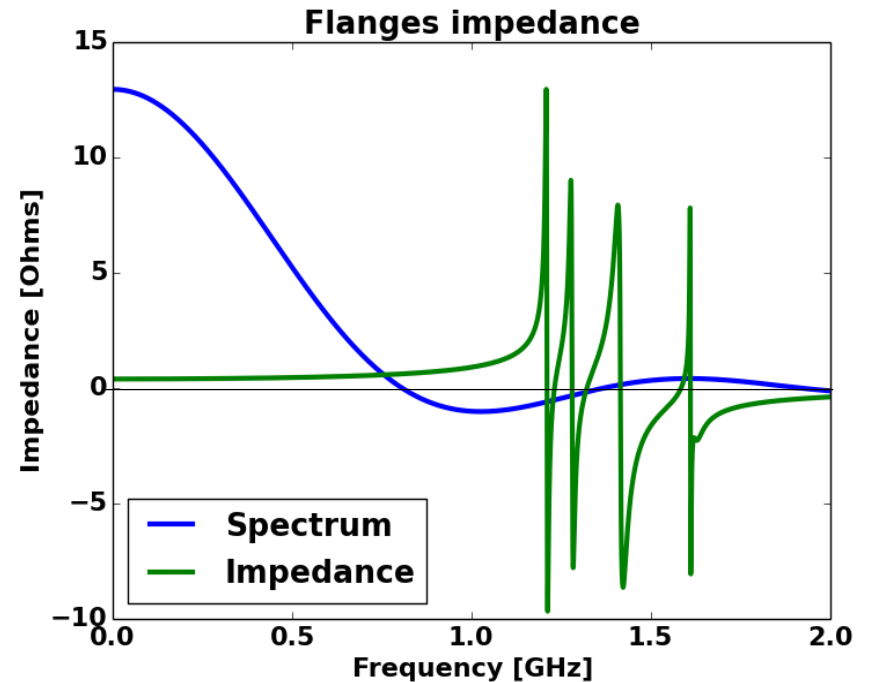
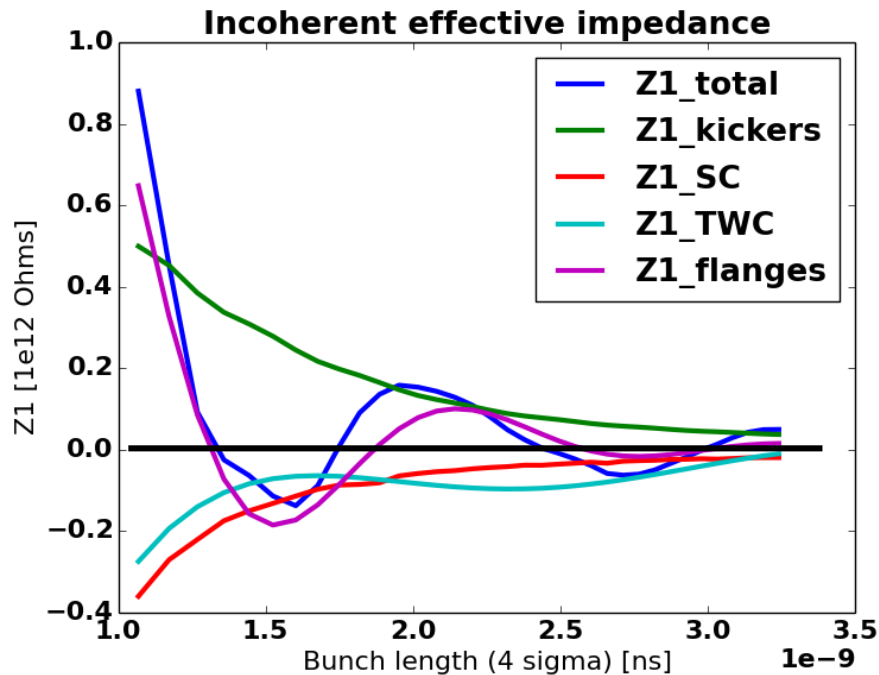
- **Coherent frequency shift** was estimated for the quadrupolar case and has a **non negligible effect** on the slope [6].

$$f_{2s} \approx 2f_s + \beta N Z_2$$

$$Z_2 = \frac{\sum_{p=-\infty}^{p=+\infty} h_2 \frac{Z}{p}}{\sum_{p=-\infty}^{p=+\infty} h_2} ; p = \frac{f}{f_0} ; h_2 = \frac{J_{5/2}(p\omega_0\tau)^2}{p\omega_0\tau}$$

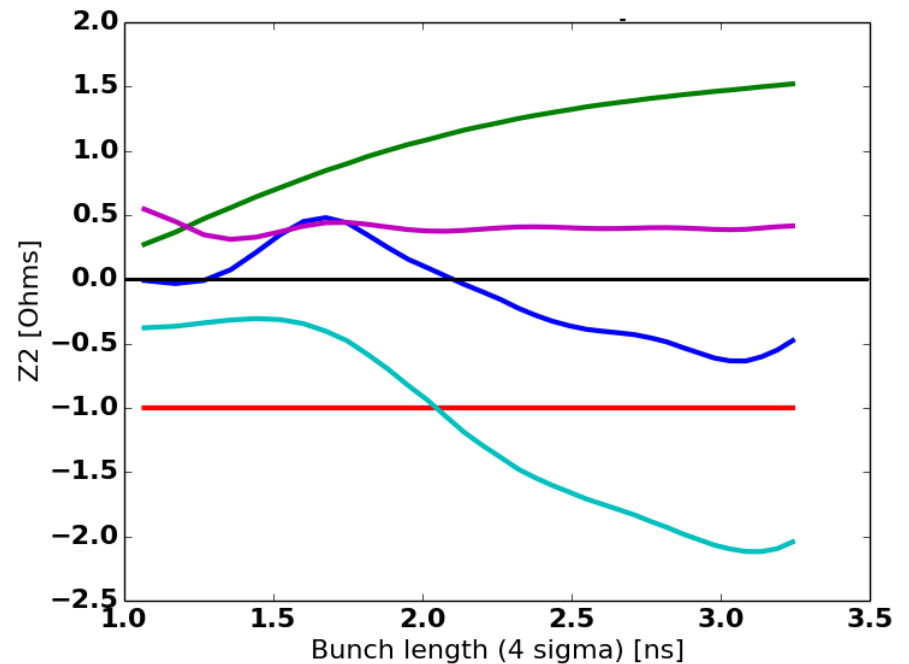
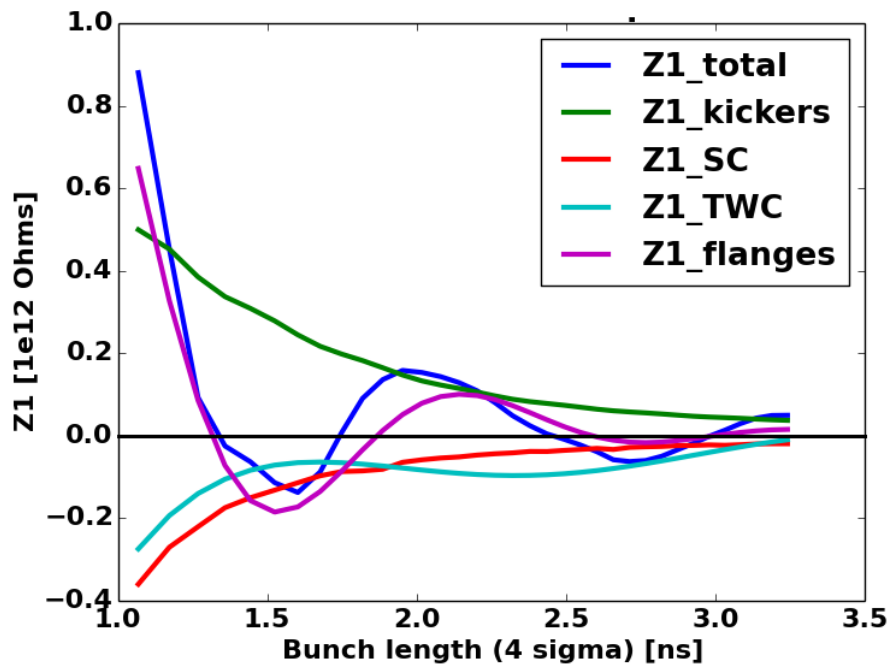
- The **coherent shift goes in the opposite direction than the incoherent shift** (capacitive impedance leads to a steeper slope and vice-versa), and is **due to the perturbation** on the bunch distribution with respect to the stationary bunch distribution.
- Note that analytical formulas are valid for small perturbations from stationary case, but **large deviations exist in measurements**.

# Parabolic spectrum



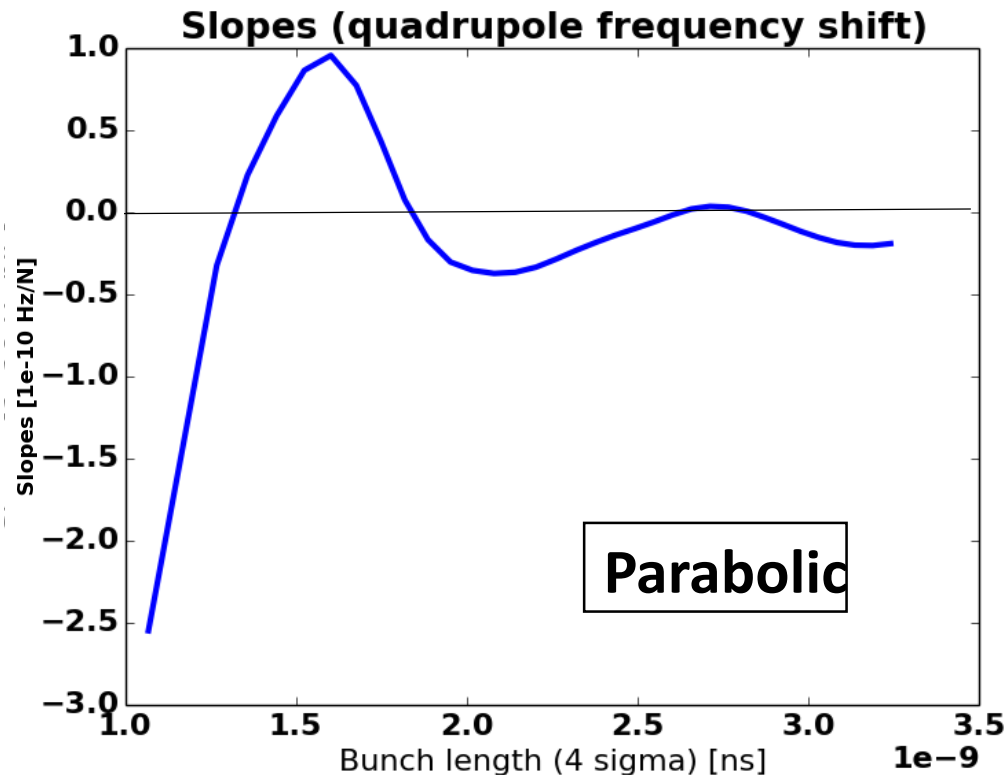
□ The impedance type (inductive vs. capacitive) changes as a function of bunch length for the flanges due to the negative lobe of the parabolic spectrum, turning inductive impedance into effective capacitive impedance.

# Effective impedance



- The effective impedances have a **dependence on bunch length**, due to the **flanges for  $Z_1$  (incoherent)**, and due to the **RF systems and the kickers for  $Z_2$  (coherent)**

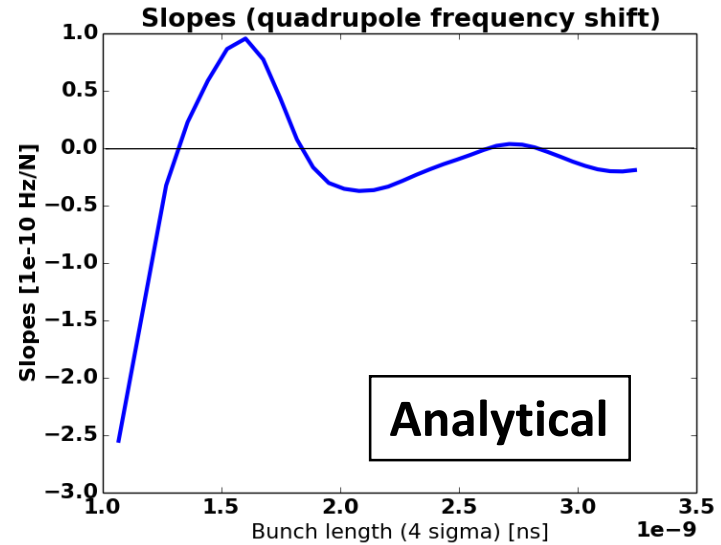
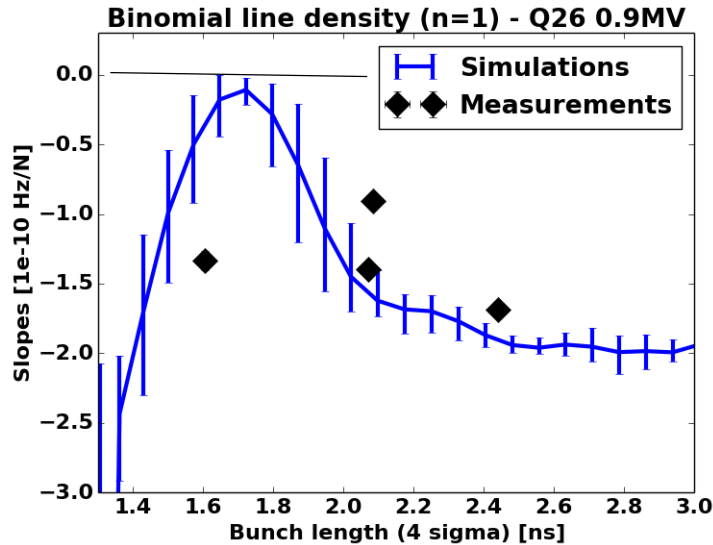
# Analytical results – Slope



- The slope is computed with incoherent and coherent shift.
- The **parabolic** distribution is sampling **inductive or capacitive depending on the bunch length**



# Conclusions



- ❑ The incoherent quadrupole frequency shift has a dependence on bunch length due to the coupling with high frequency impedances (flanges), while the coherent shift dependence is due to the RF systems and the kickers.
- ❑ More measurements are foreseen by **generating a small mismatch by increasing the RF voltage** in the SPS, in order to have **smaller perturbations**.
- ❑ Measurements at **higher energies** are planned in order to **eliminate the space charge** impedance.
- ❑ Information on the synchrotron frequency shift are needed in order to apply **emittance blow-up with RF noise**. The dependency with bunch length is to be known in order to apply correctly the RF noise.

# References

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- [1] J. L. Laclare, “Bunched Beam Coherent Instabilities”, CERN 87-03, p.264, CAS Proceedings, (1987).
- [2] J. Varela Campelo, C. Zannini, B. Salvant, «SPS Impedance Model Update», Meetings of the LIU-SPS Beam Dynamics Working Group, CERN, Geneva, Switzerland (2014), <http://paf-spsu.web.cern.ch/paf-spsu/meetings/2008.htm>
- [3] L. Wang, «The geometry effect of the space charge impedance LSC code», ICFA mini-Workshop on “Electromagnetic wake fields and impedances in particle accelerators” , Erice, Italy, 2013
- [4] BLoND code: <https://github.com/dquartul/BLoND/>
- [5] K. Y. Ng, «Physics of Intensity Dependent Beam Instabilities», Ed. World Scientific Publishing, 2006
- [6] A. Chao, «Physics of Collective Beam Instabilities in High Energy Accelerators», Ed. John Wiley & Sons, 1993