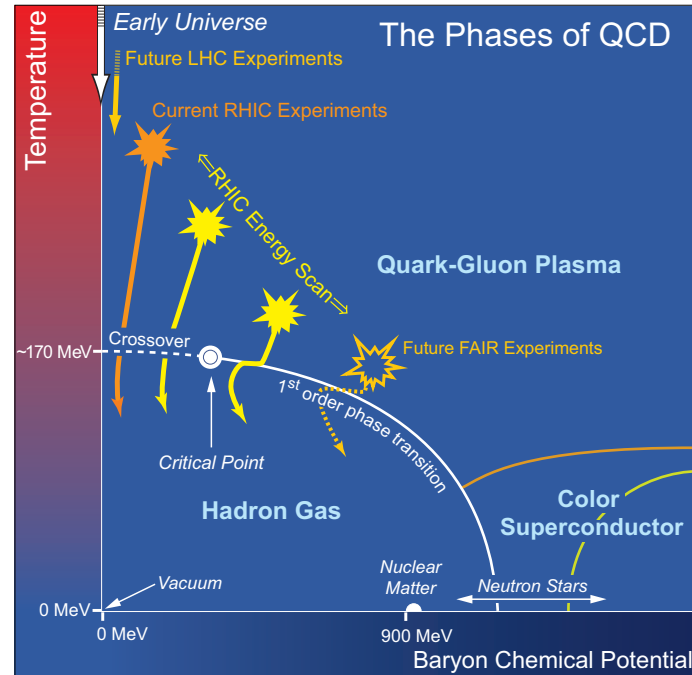


# Recent Results on Beam-beam Effects in Space Charge Dominated Colliding Ion Beams at RHIC

Christoph Montag, BNL

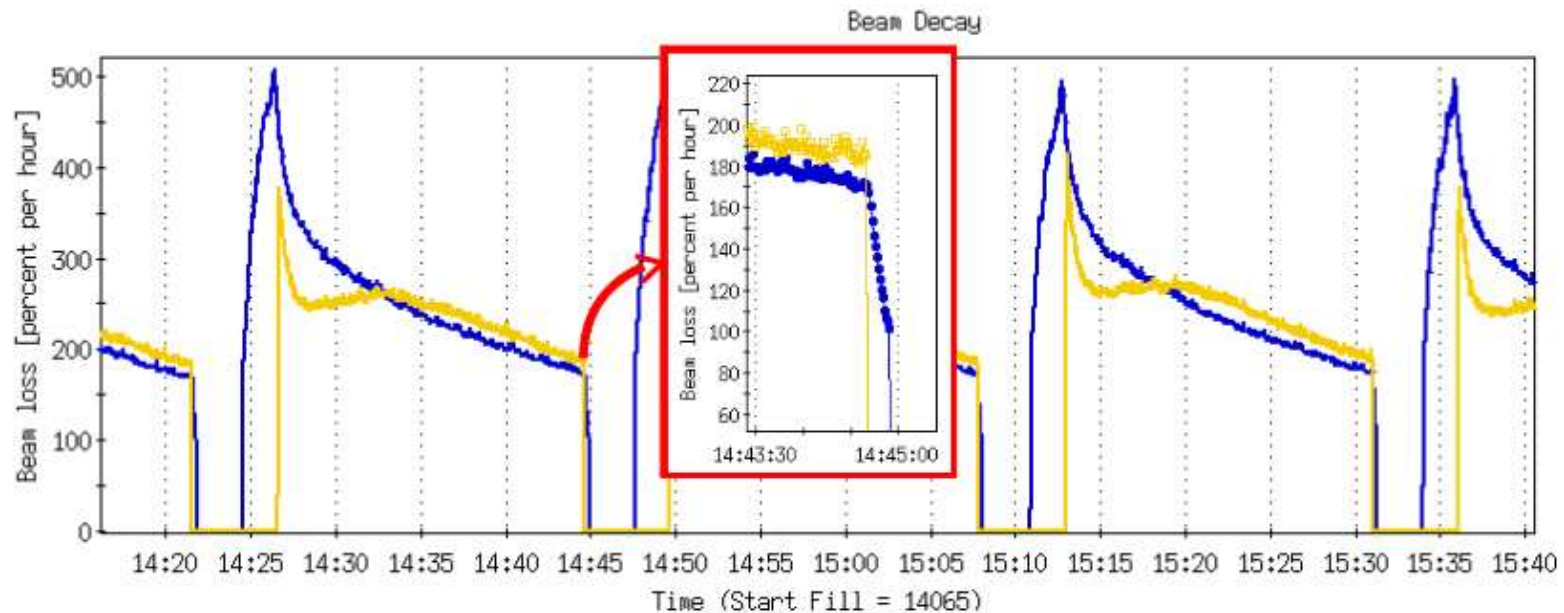
HB2014, East Lansing, MI

## RHIC as a low energy collider



Search for the critical point in the QCD phase diagram requires colliding Au beams with energies between 2.5 and 10 GeV/nucleon

## Beam decay rates during RHIC low energy run in 2010



With tunes set to  $(Q_x, Q_y) = (.13, .12)$ , Blue beam decay recovers immediately as soon as Yellow beam is dumped

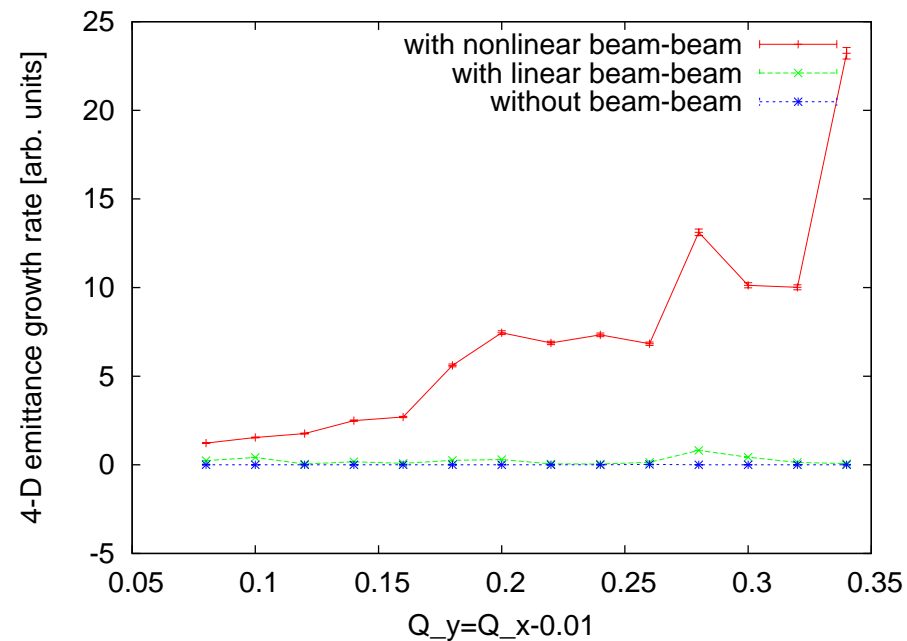
Strong beam-beam effect, though space charge tune shift is much larger ( $\Delta Q_{sc} \approx -0.05$ ,  $\xi_{bb} \approx -0.003$ )

## The tracking “toy” model

- 11 FODO cells - 10 are identical, quad strengths in 11th cell are scaled up by 3 percent to break the periodicity
- Dipoles are modeled as drifts for simplicity; thin-lens approximation for quads
- No nonlinear elements such as sextupoles
- Space charge kicks are applied at equidistant locations; based on self-consistent RMS beam size at each location

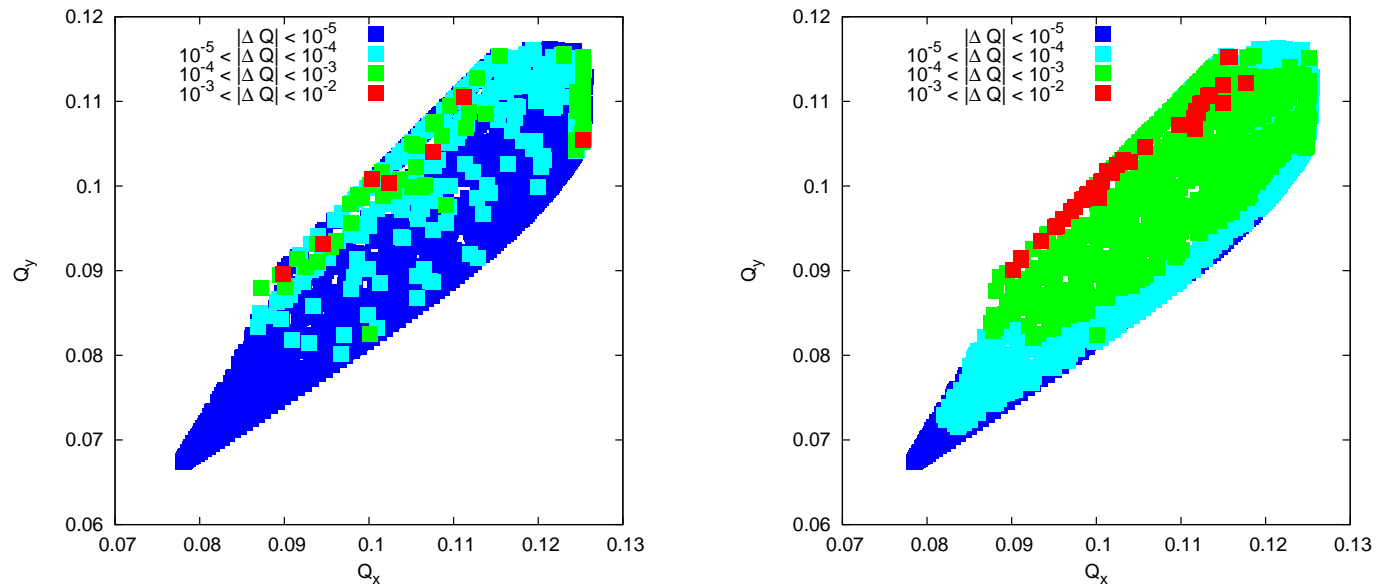
- One beam-beam kick per revolution; strong beam has self-consistent size as well
- All tracking done on-energy, no longitudinal motion
- With beam-beam:  $\Delta Q_{\text{spacecharge}} = -0.05$ ,  $\xi_{\text{beam-beam}} = -0.003$
- Without beam-beam:  $\Delta Q_{\text{spacecharge}} = -0.053$ , keeping total tune shift constant for both cases

## 4-D emittance growth rates in the “toy” model



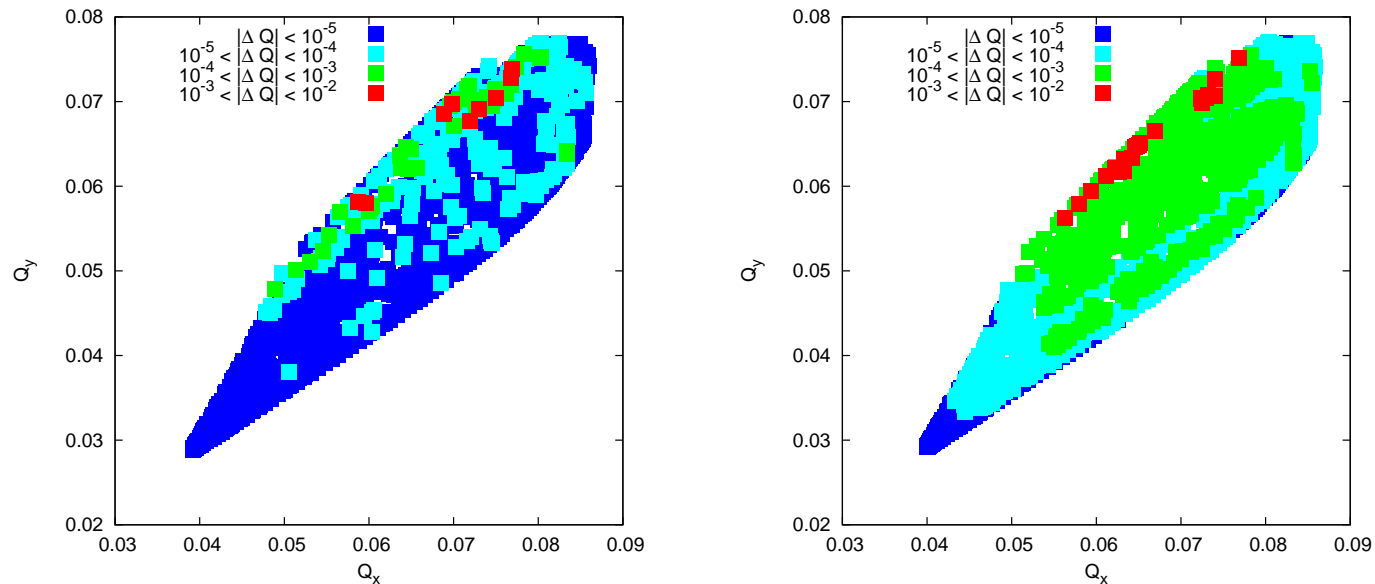
- Growth rates with beam-beam increase the further the tunes are from the integer
- Linear beam-beam lens shows no growth - effect is not just due to broken periodicity
- No growth without beam-beam

## Tune footprints at 2010 working point (.13,.12)



- Beam-beam interaction enhances tune diffusion almost everywhere
- No distinct resonances appear besides linear coupling resonance  $Q_x = Q_y$

## Tune footprints at near integer working point (.09,.08)



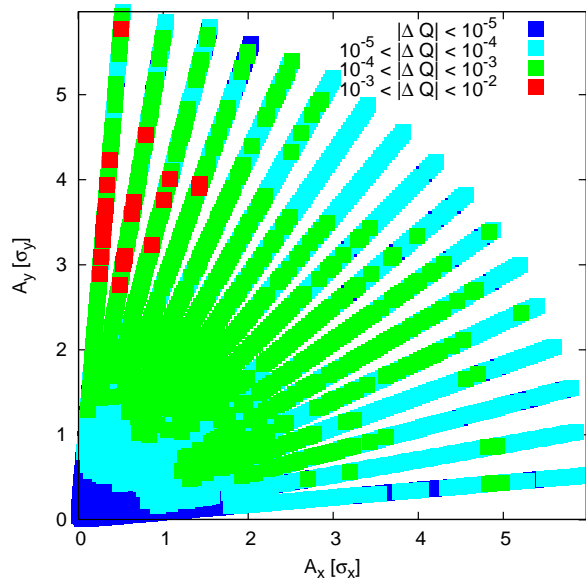
- Beam-beam interaction enhances tune diffusion almost everywhere
- No distinct resonances appear besides linear coupling resonance  $Q_x = Q_y$

Very similar to 2010 working point

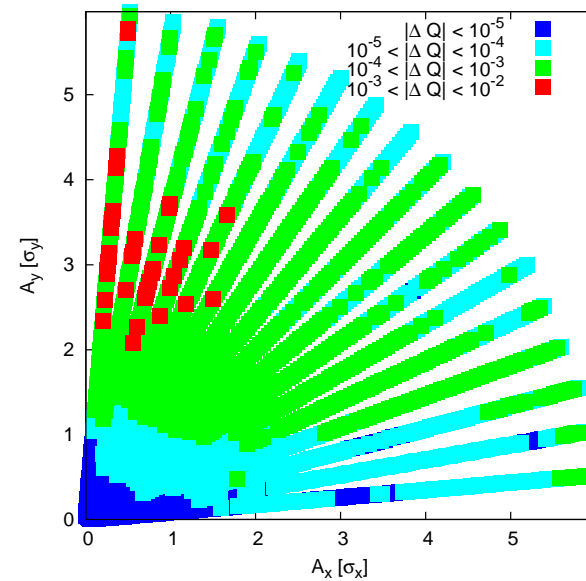


## Tune diffusion in amplitude space

(.09, .08) :



(.13, .12) :



- Tune diffusion at near integer working point appears **larger** than at 2010 working point
- **Disagreement with emittance growth results**

## MADX-SC tracking in the RHIC lattice

---

beam energy [GeV]	5.86
bunch intensity	$4 \cdot 10^{10}$
transverse rms emittance [mm mrad]	0.16
$\beta^*$ [m]	10
$\sigma_{IP}$ [mm]	1.3
RMS bunch length [m]	3.0
space charge tune shift	-0.065
beam-beam tuneshift per IP	-0.005

---

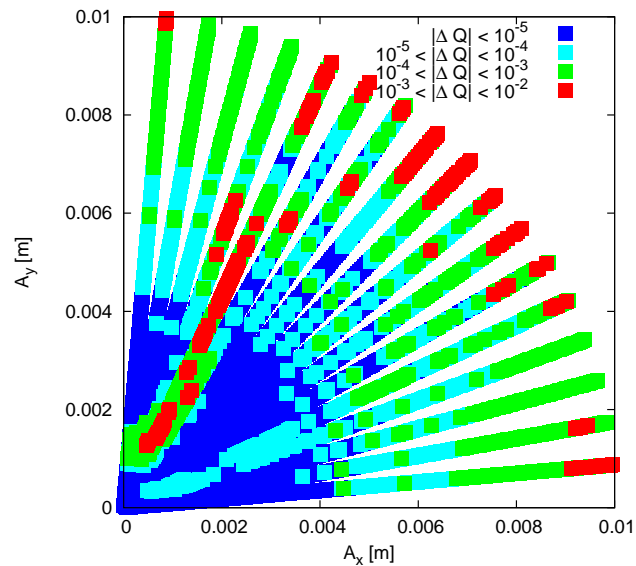
Off-momentum dynamic aperture in collision:

$5.5\sigma$  at (28.095, 30.085),  $4.5\sigma$  at (28.013, 30.012)

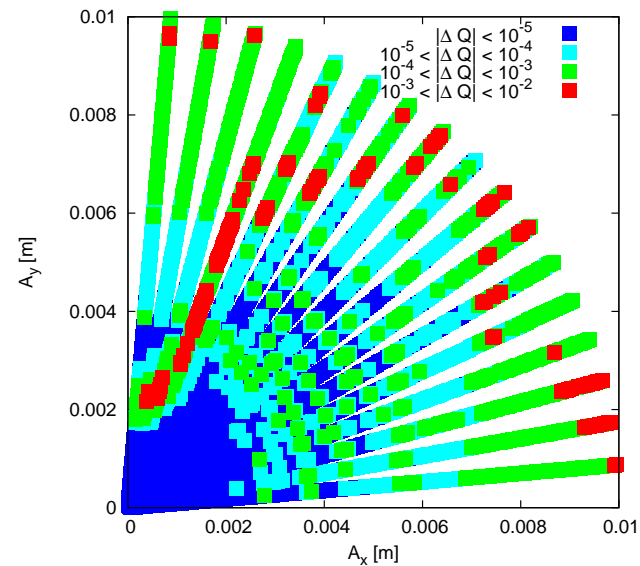
Larger dynamic aperture at near-integer working point

## Tune diffusion in the RHIC lattice

(.095, .085) :

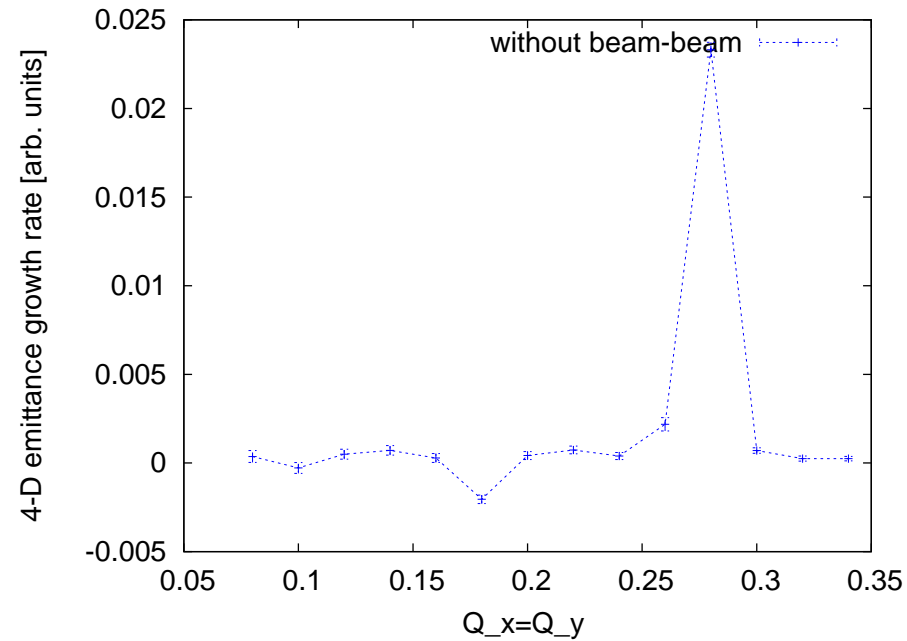


(.13, .12) :



- Tune diffusion at near integer working point **larger** than at 2010 working point - **contradicts dynamic aperture results**
- Dominated by linear coupling resonance ( $Q_x = Q_y$ )  
**Is frequency map analysis the right tool?**

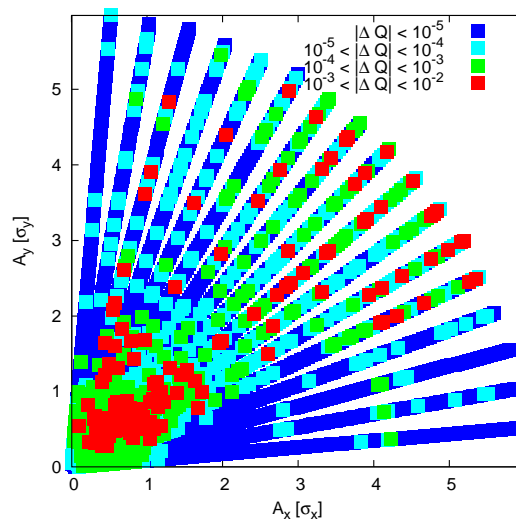
## Emittance growth on the coupling resonance ( $Q_x = Q_y$ )



Within error bars, **no emittance growth without beam-beam**

## Tune diffusion on the coupling resonance

$$(Q_x, Q_y) = (.08, .08):$$



Large tune diffusion due to coupling resonance even at very small amplitudes

Tune diffusion does not indicate amplitude diffusion

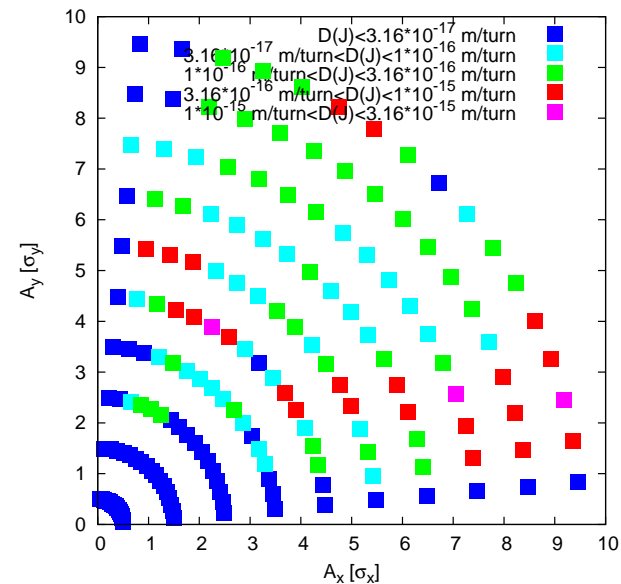
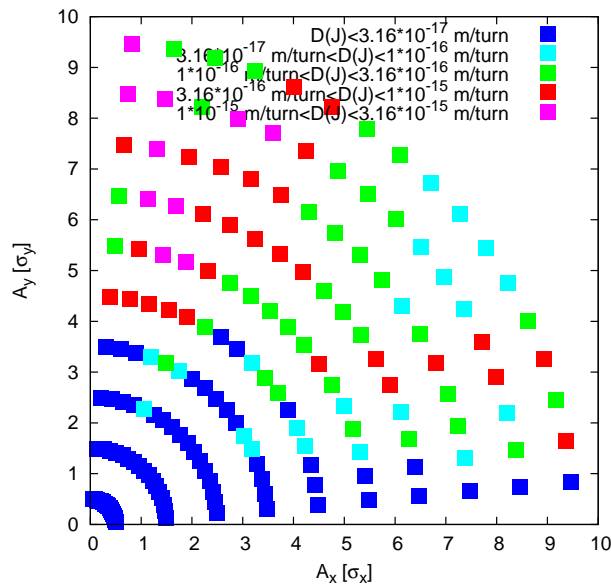
## Amplitude diffusion in “Toy Model”

- For each action  $(J_x, J_y)$ , launch 100 particles in phase space
- Track for 10000 turns
- At each turn, calculate RMS action spread  $J_{\text{RMS}}^2 = \langle (J_x - \langle J_x \rangle)^2 + (J_y - \langle J_y \rangle)^2 \rangle$ , with the average taken over the 100 particles
- Fit a straight line  $J_{\text{RMS}}$  vs. turn number; slope equals diffusion coefficient  $D(J)$

# Amplitude diffusion results

(.09, .08) :

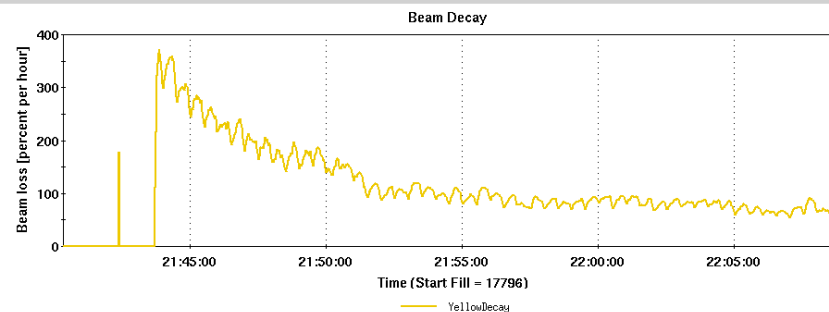
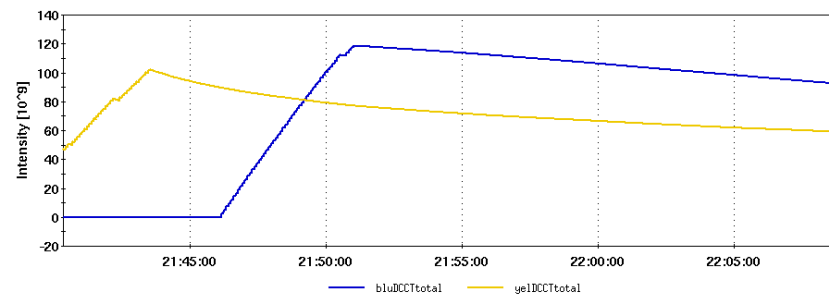
(.13, .12) :



- 2010 working point shows larger amplitude diffusion at amplitudes up to  $4\sigma$  than near-integer working point
- Consistent with emittance growth results

# Yellow beam decay during Blue beam injection

Near-integer working point (.095, .085) :

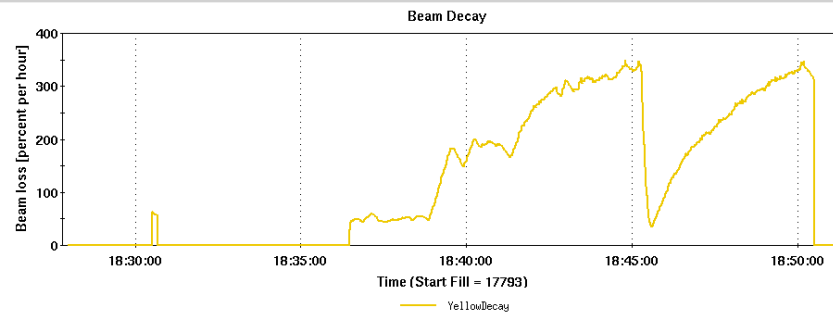
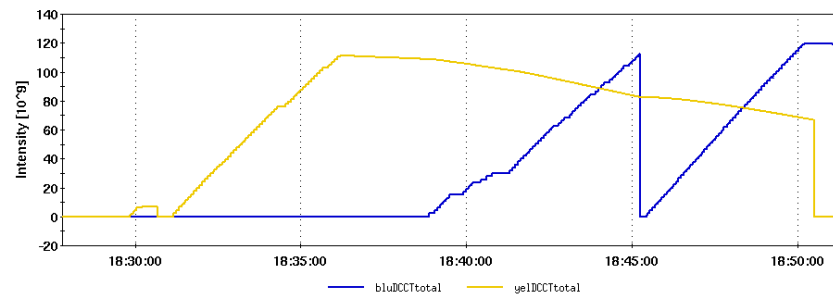


- Yellow beam decay continues to improve during Blue injection
- No significant beam-beam effect



# Yellow beam decay during Blue beam injection

2010 working point (.13, .12) :



- Yellow beam decay rises sharply during Blue beam injection
- Strong beam-beam effect

## Conclusion

- Tracking with the simple model reproduces observed beam-beam effect qualitatively well
- Near-integer tunes are preferred
- Frequency map analysis shows tune diffusion even when there is no emittance growth
- Amplitude diffusion simulations show tune dependence in agreement with emittance growth data
- Significant improvement in RHIC performance with near-integer tunes during FY2014

Thanks to:

F. Schmidt, V. Kapin, M. Blaskiewicz, and many others