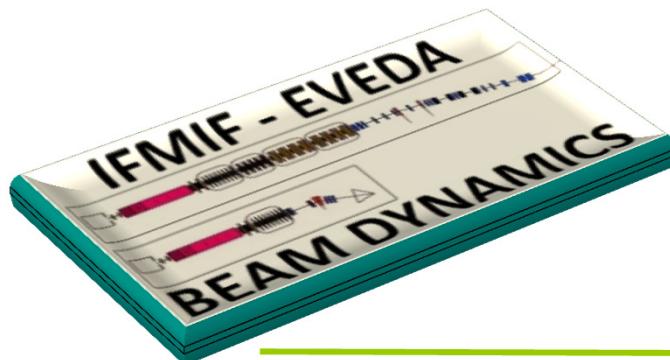


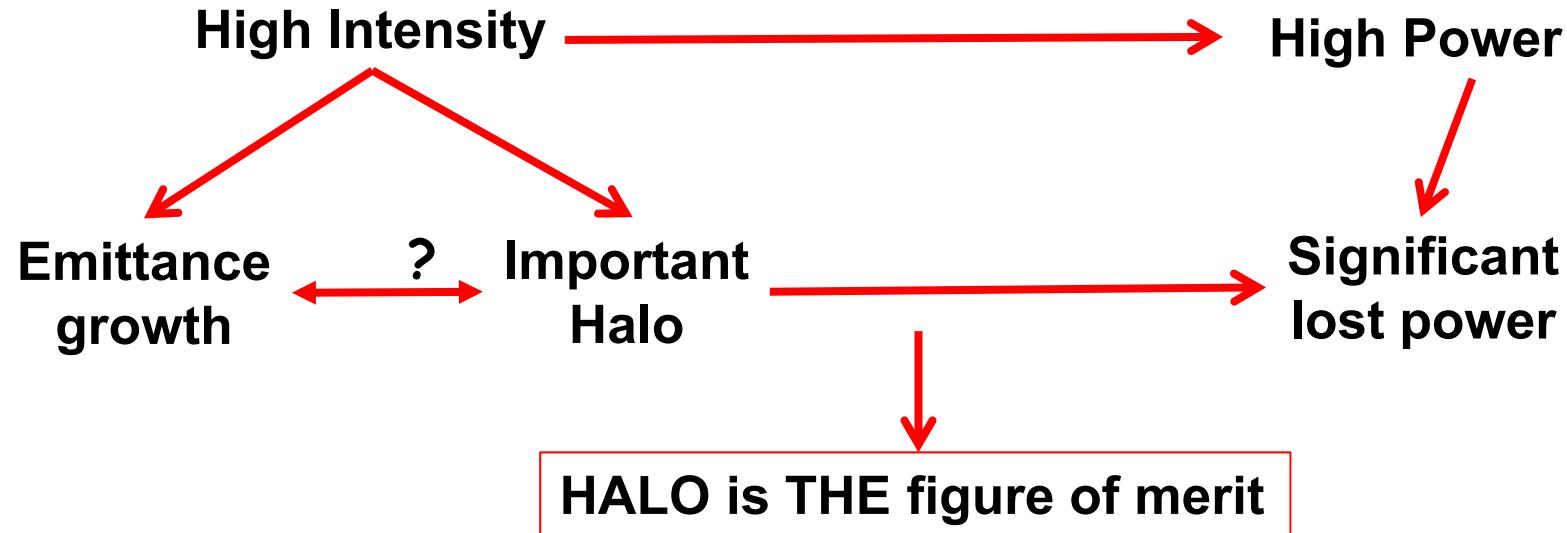


# *Introduction to the Discussion: Beam Halo Definitions and its Consequences*

P. A. Phi NGHIEM et al.



HB2012 - Beijing



BUT: what is Halo ? precisely and quantitatively ?

Lattice optimisation and beam measurement:  
what and how much to improve and to measure ?

Is there a connection with emittance growth ?

## ALLEN & WANGLER, PRSTAB,5,124202 (2002)

The halo parameter contains additional information as to the beam state, since we find that it is possible to have emittance growth without halo growth (however, halo growth always implies emittance growth). As with emittance, the halo parameter is invariant under linear forces. Thus, halo growth is necessarily the result of nonlinearities.

### HALO'03: no consensus for a definition of the halo

But then the most used: Definition based upon  
comparison between "far" and "close" beam center

4<sup>th</sup> / 2<sup>nd</sup> moment (Wangler & Crandall and Allen & Wangler)  
n / 1 sigma

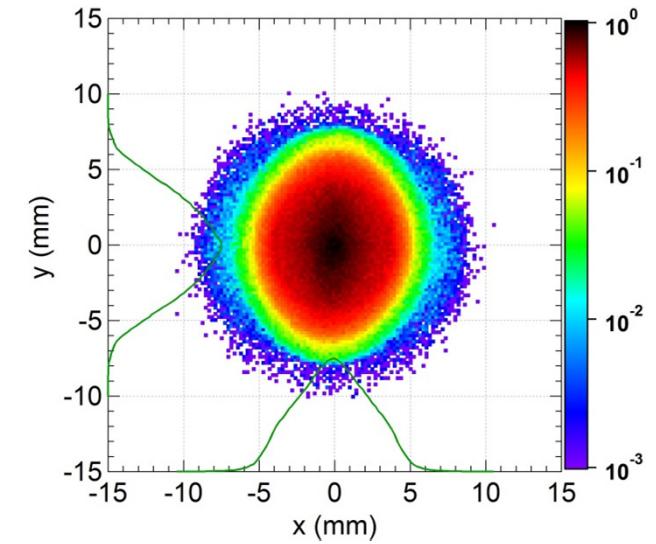
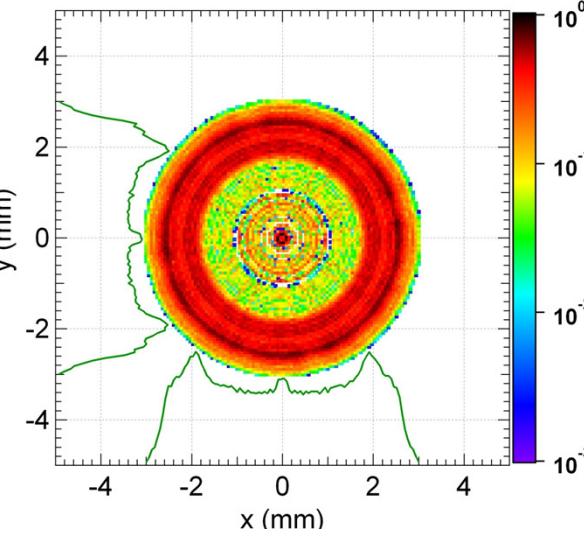
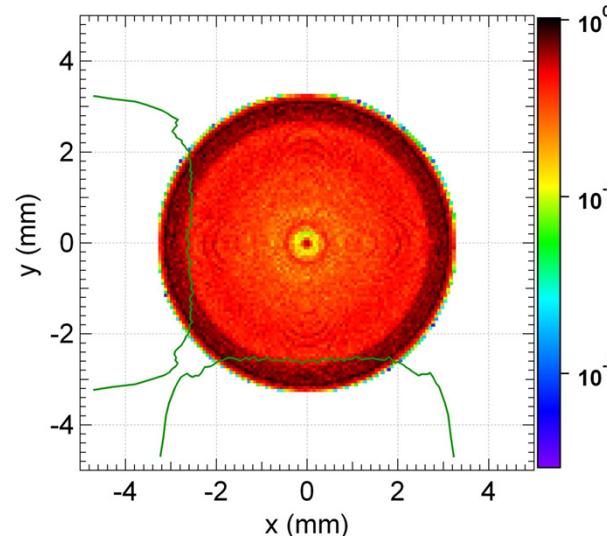
...

→ an idea of the relative importance of the halo

Inconvenience:

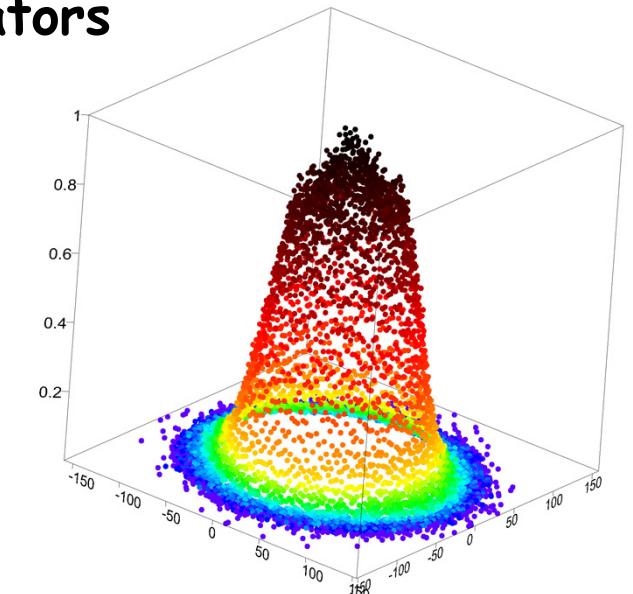
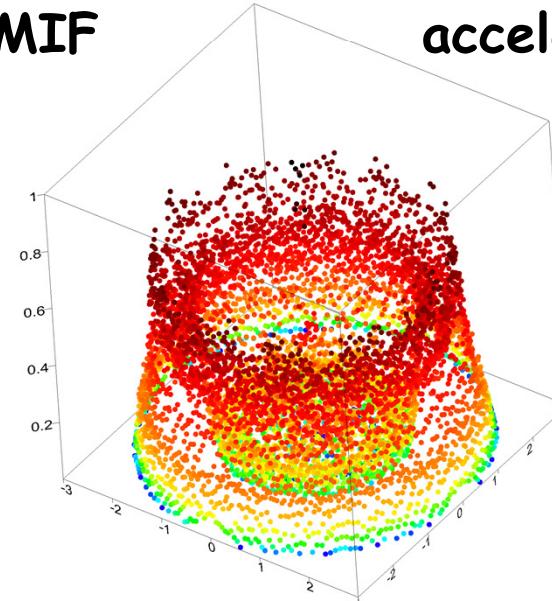
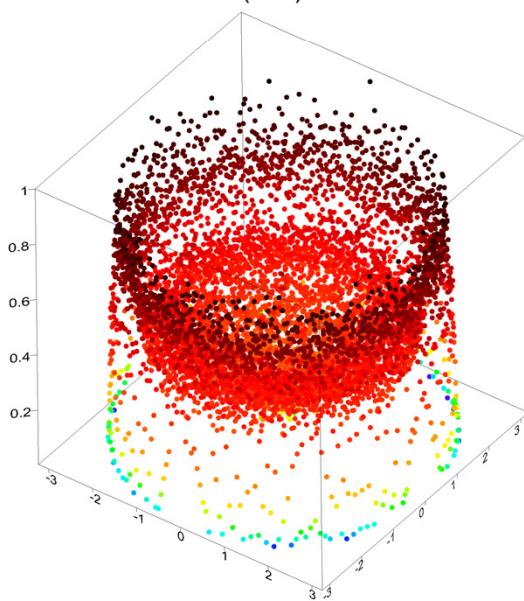
- abstract parameter
- not a value specifying the halo itself
- decide in advance where should be the halo, where should be the core

## Various situations



IFMIF

accelerators



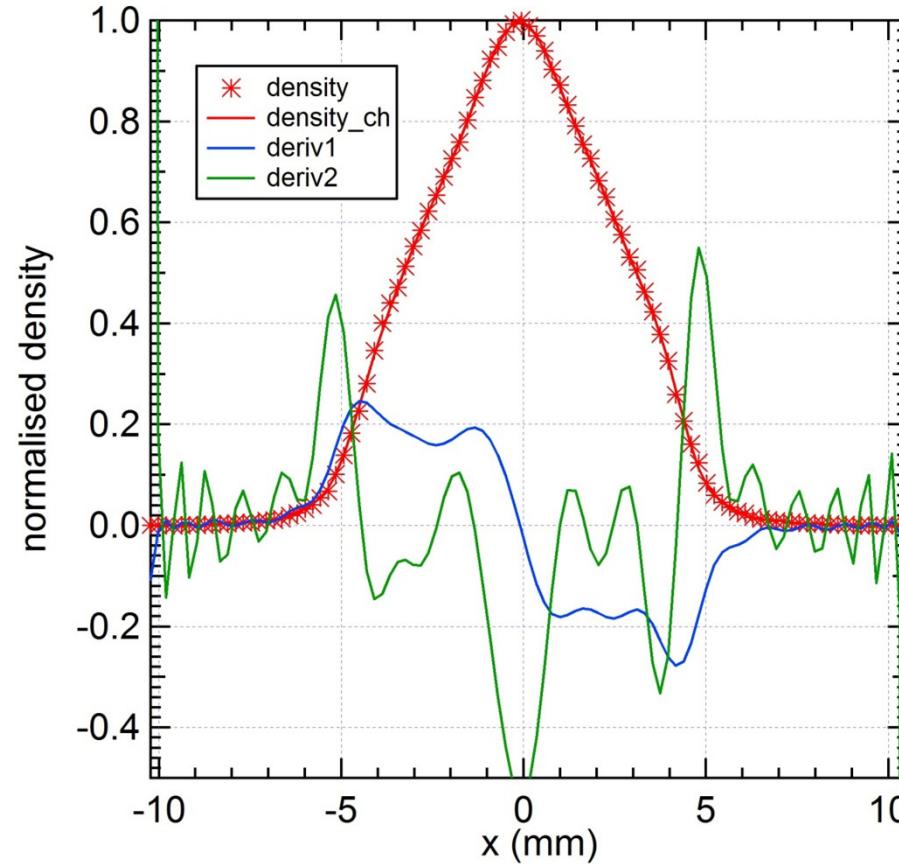
For a gas of particles where there is a slowly varying density gradient, we can consider that this gas is composed of **two** different parts: when there exists a **border** between them  
→ where the gradient variation is the steepest  
→ where the second derivative of the density is maximum.

### The diffusion equation

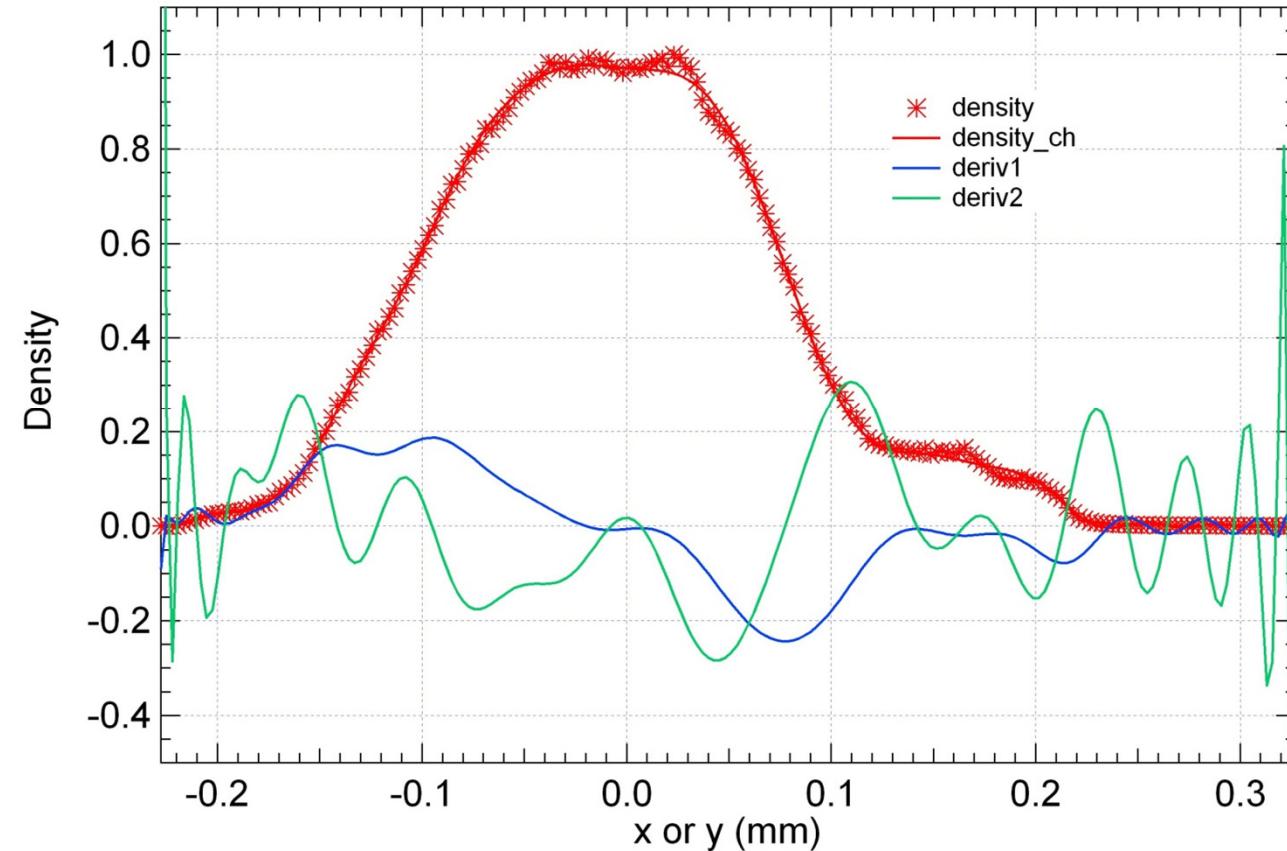
$$\frac{dn}{dt} = D \Delta n$$

states that the diffusion is maximum where the Laplacian of the density is maximum: this is the border between the two parts

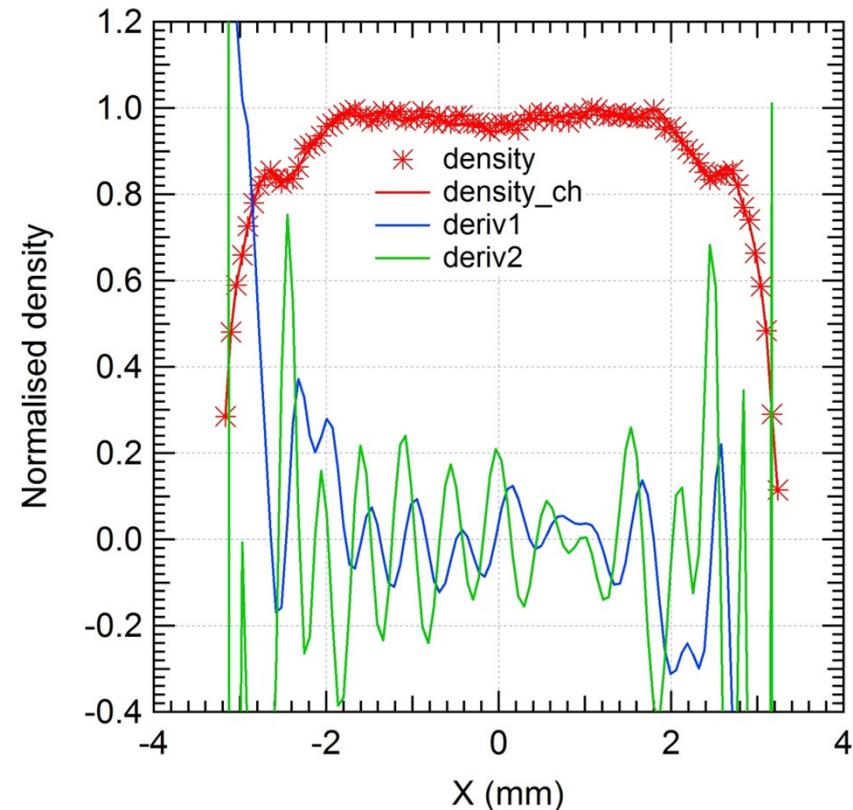
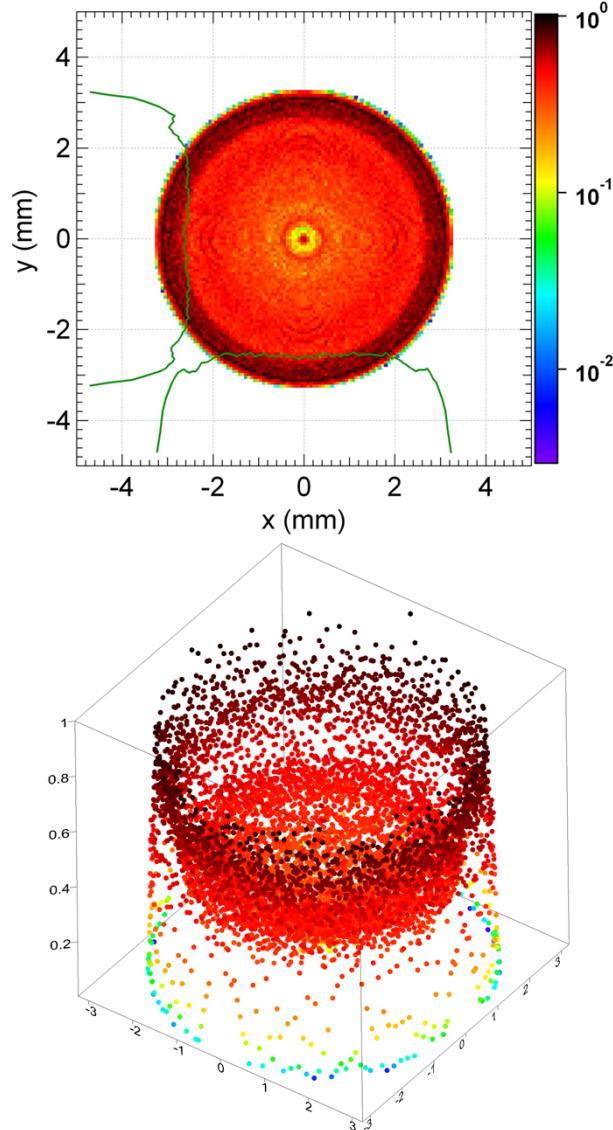
1 dimension: max of the second derivative  
n dimensions: max of the Laplacian

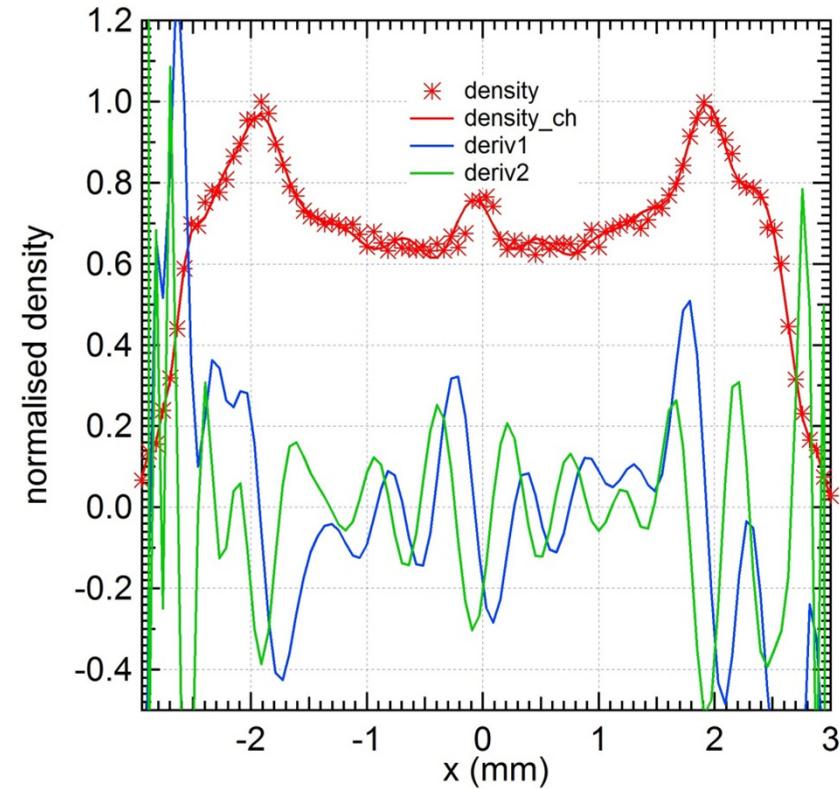
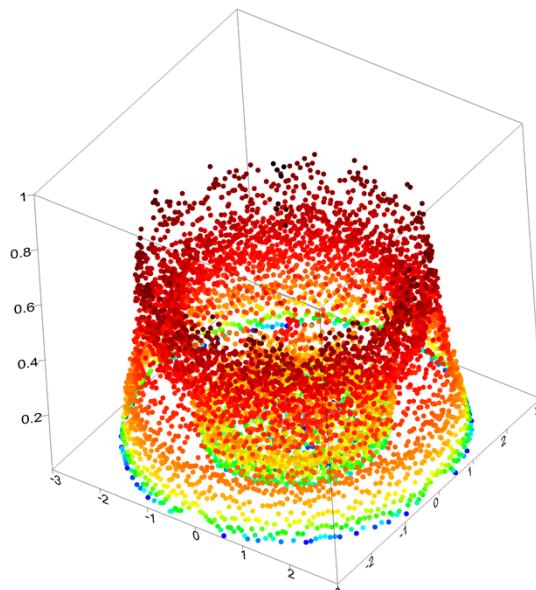
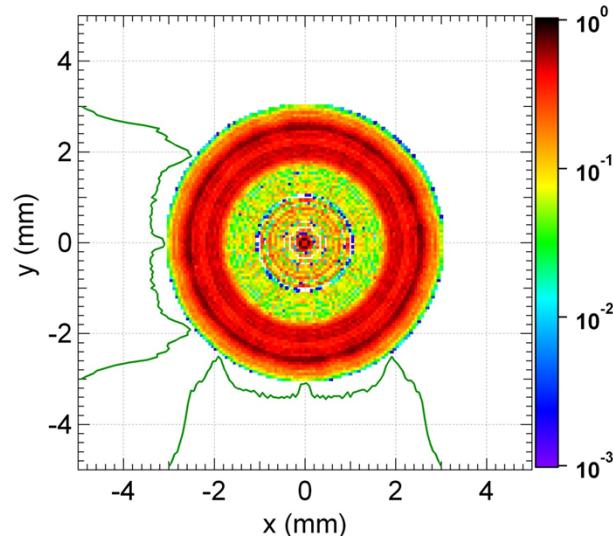


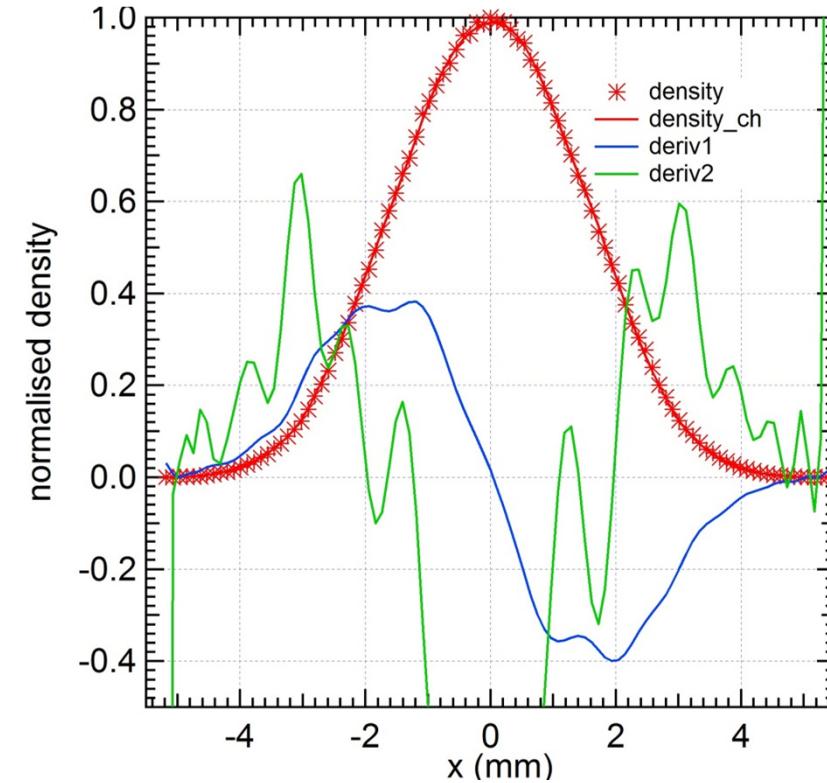
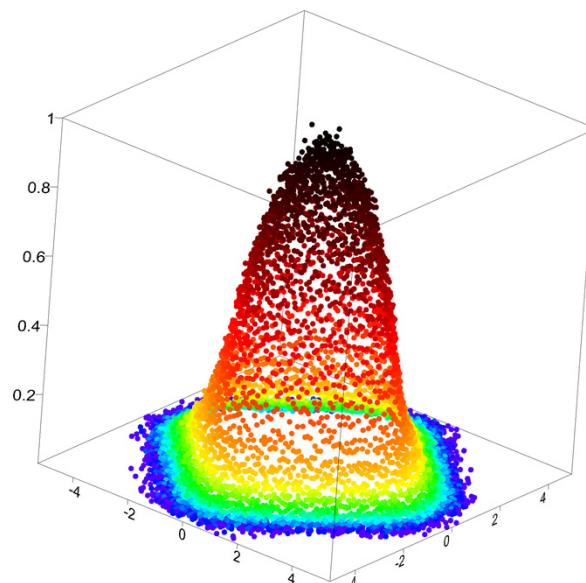
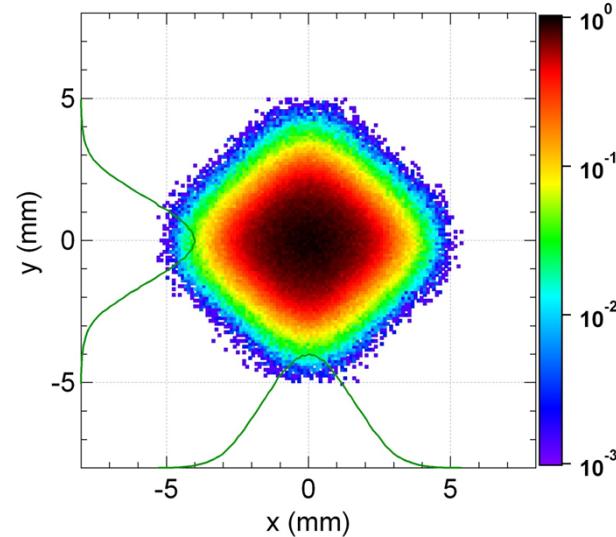
Once the limit core-halo is defined, the halo can be characterised by  
→ its size / whole size  
→ the number of particles within it / whole number of particles

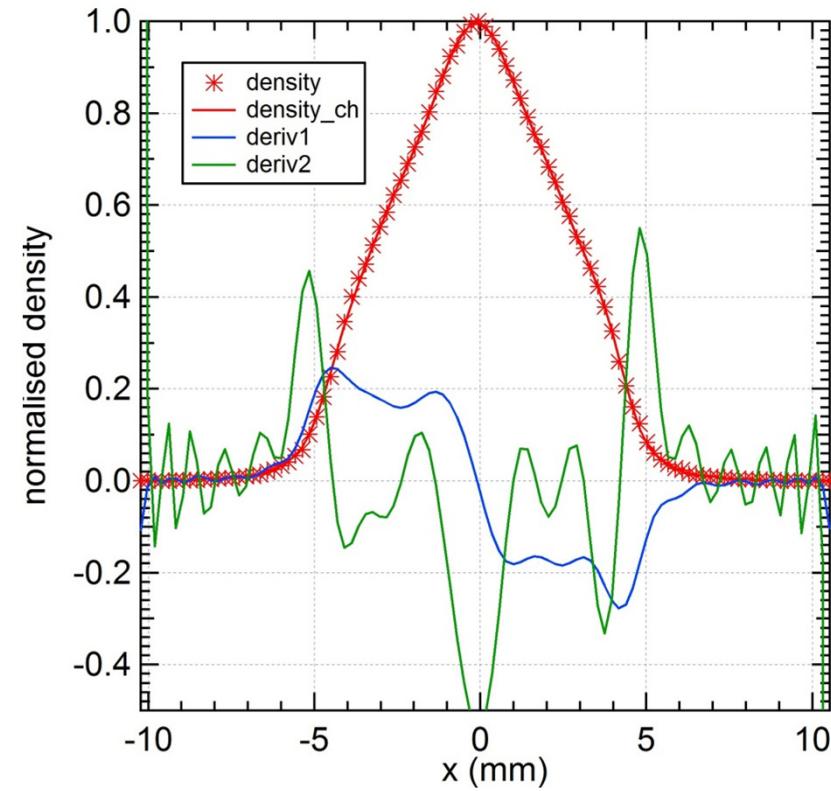
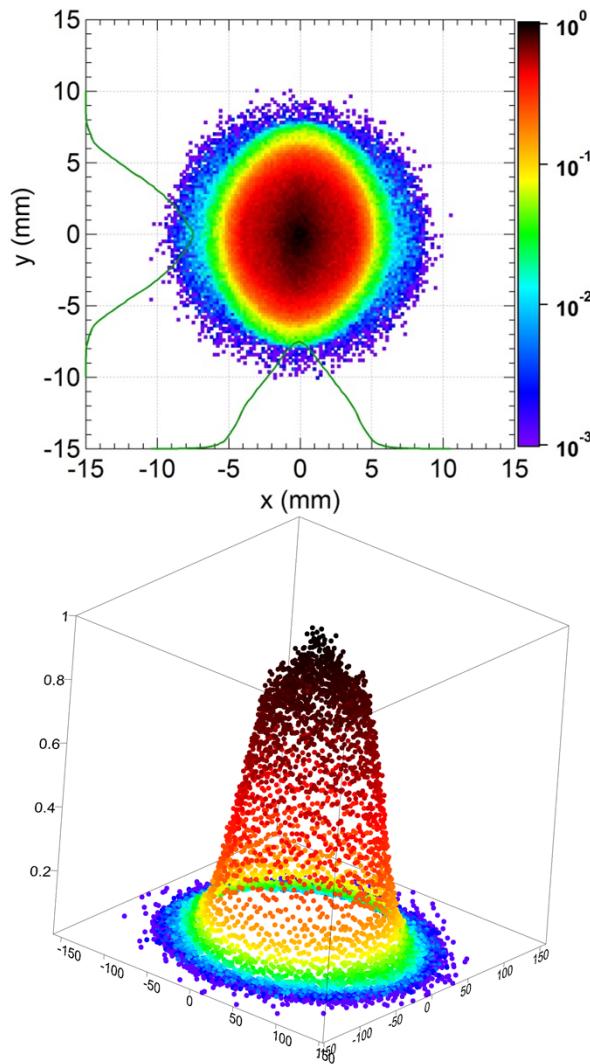


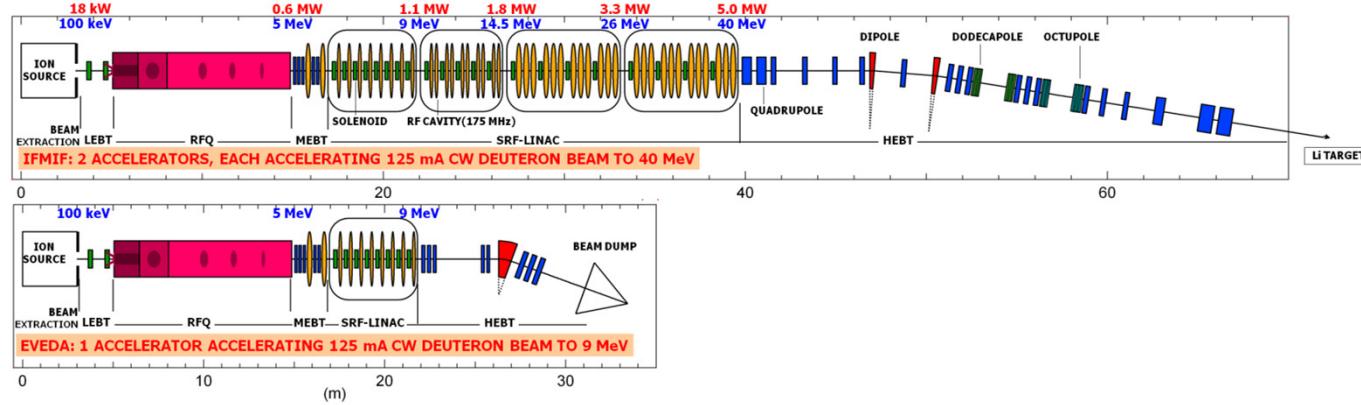
**Caution: numerical derivative ! use Spline and Chebychev**



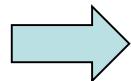






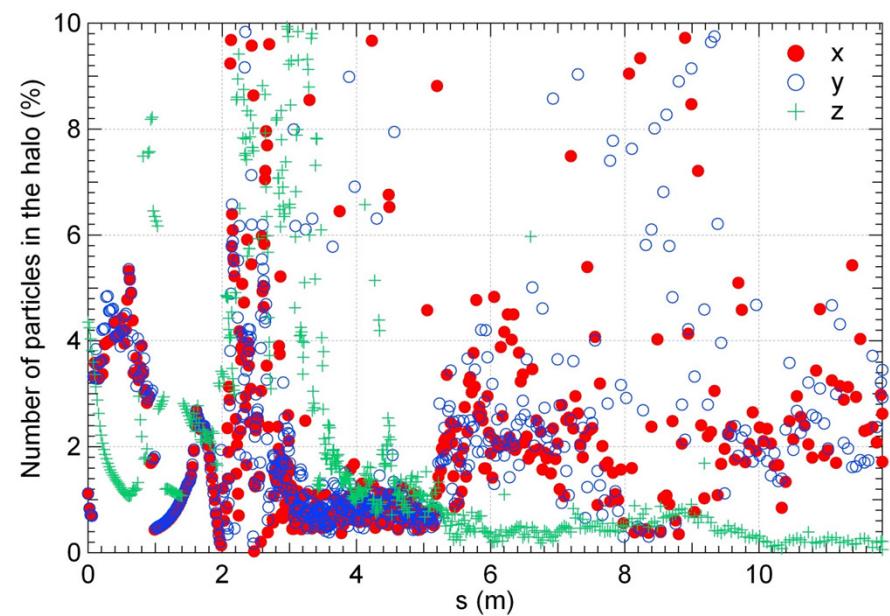
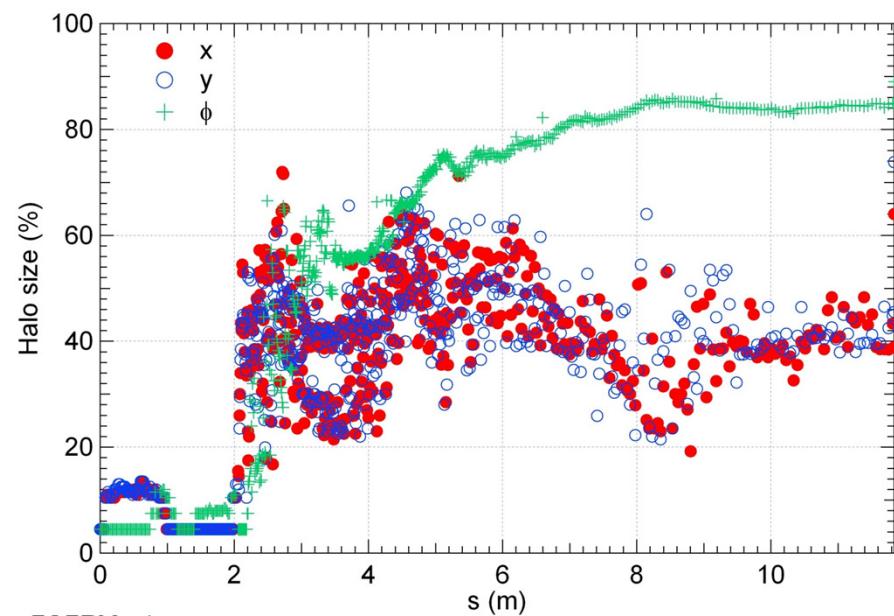
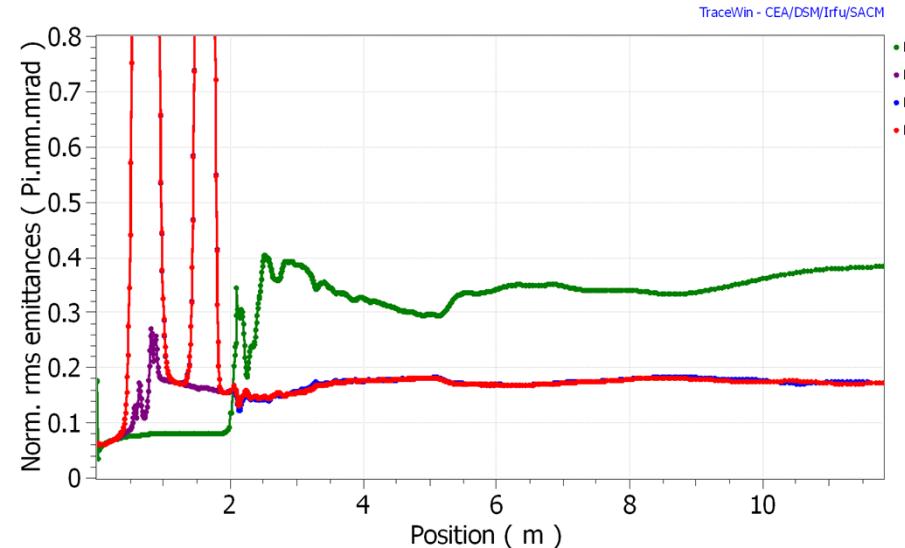
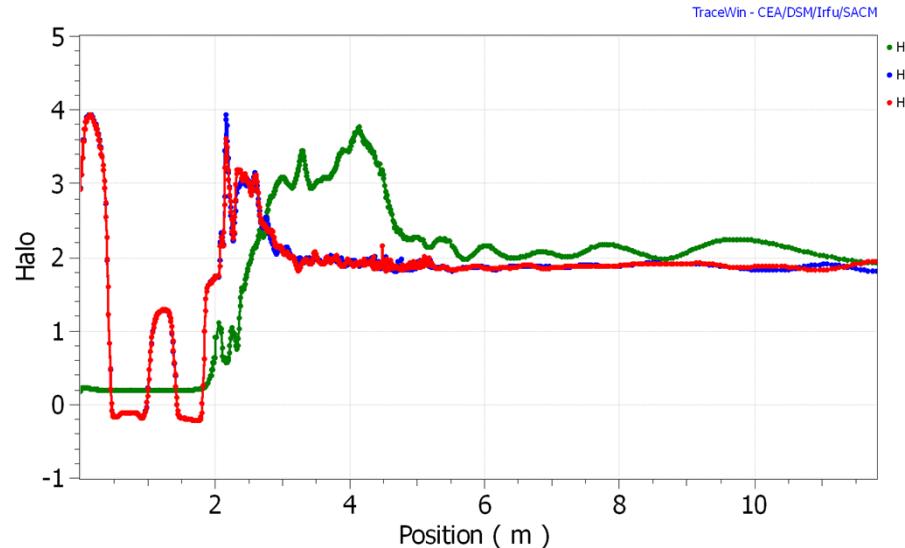


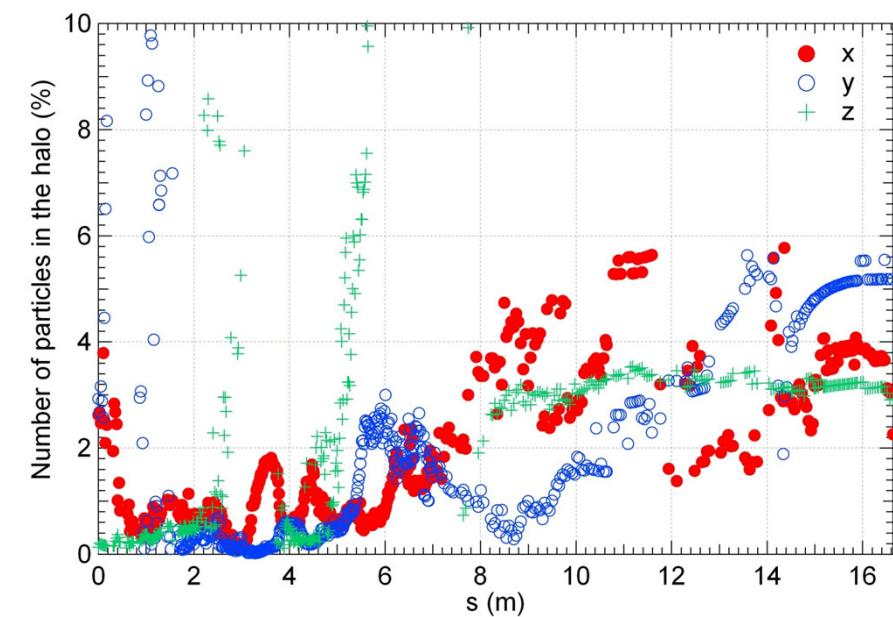
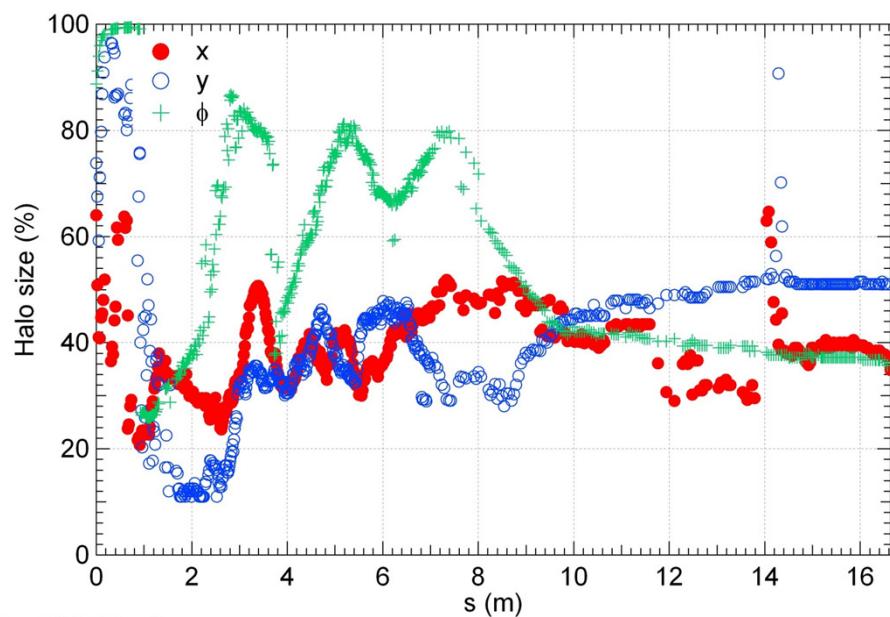
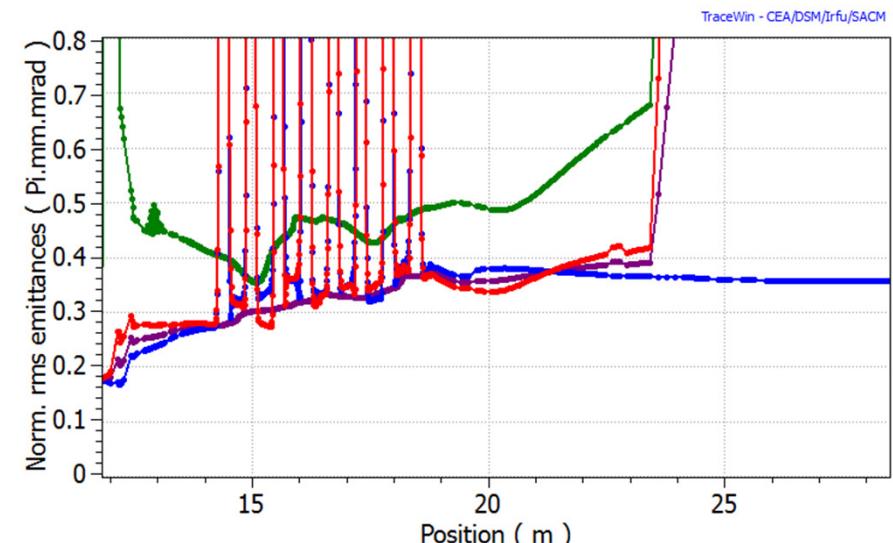
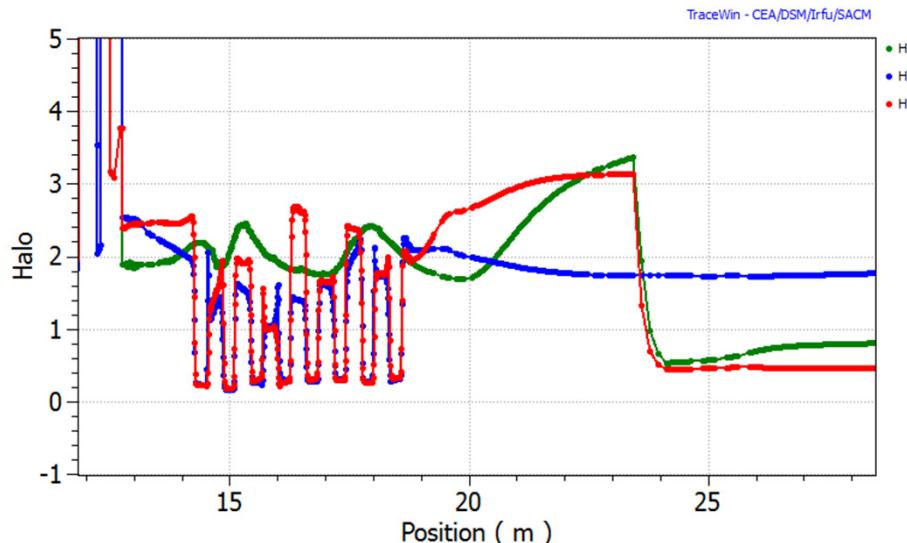
125 mA CW  
9 MeV: 1.1 MW  
40 MeV: 5 MW



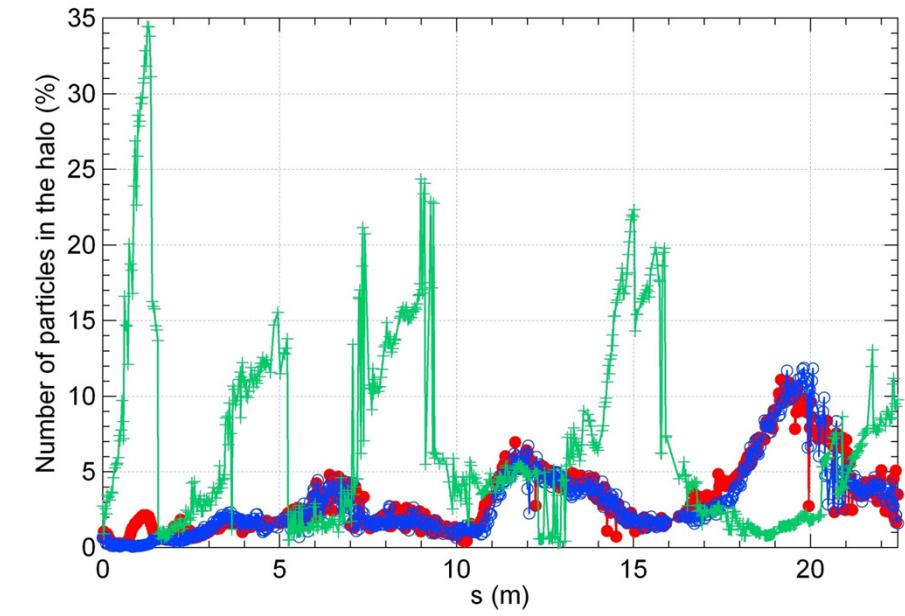
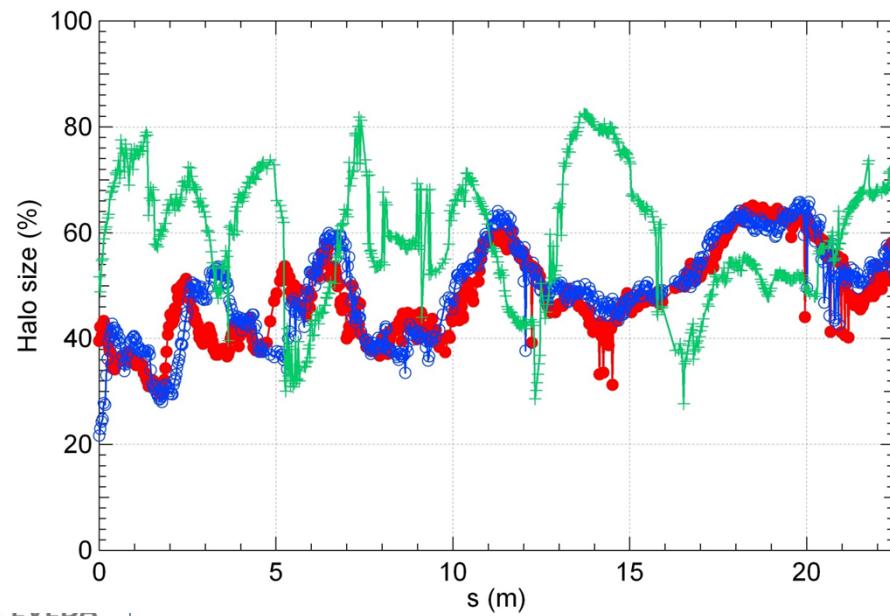
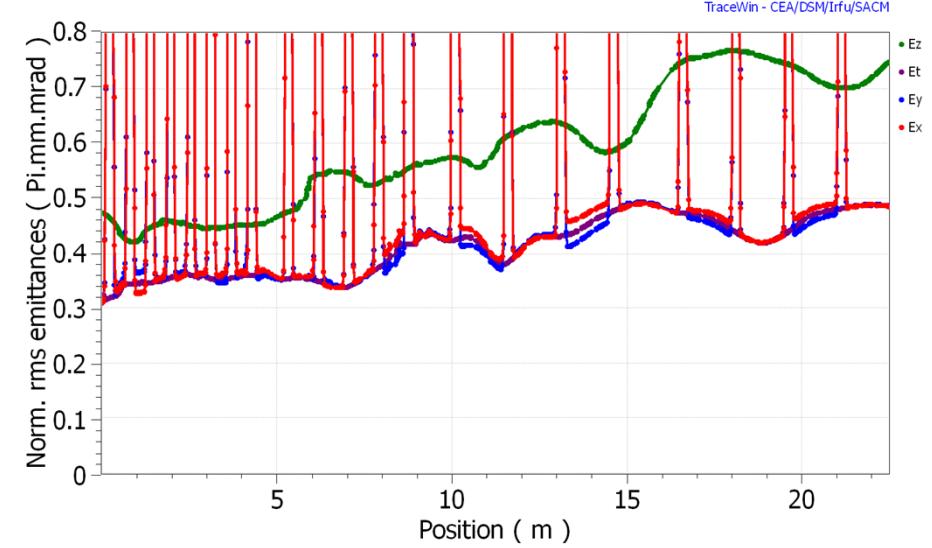
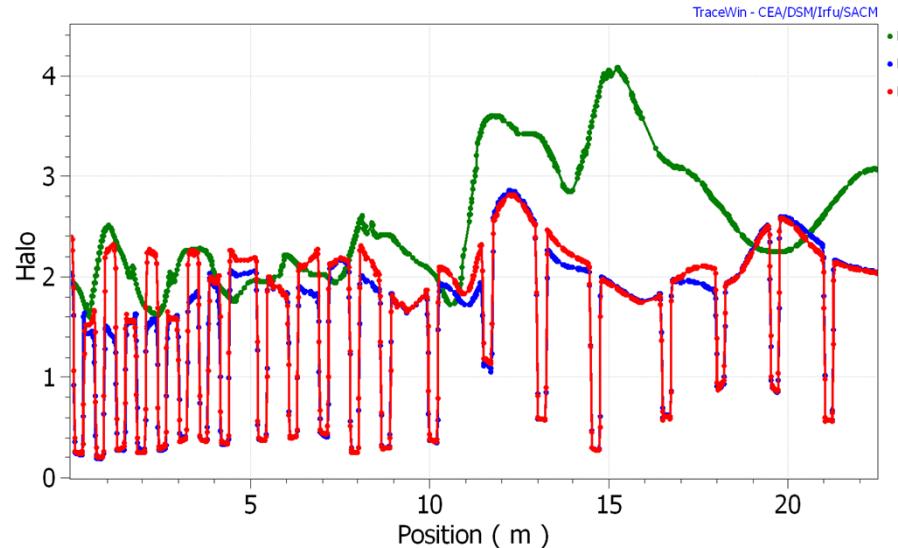
simultaneously

Very high space charge  
Very high beam power

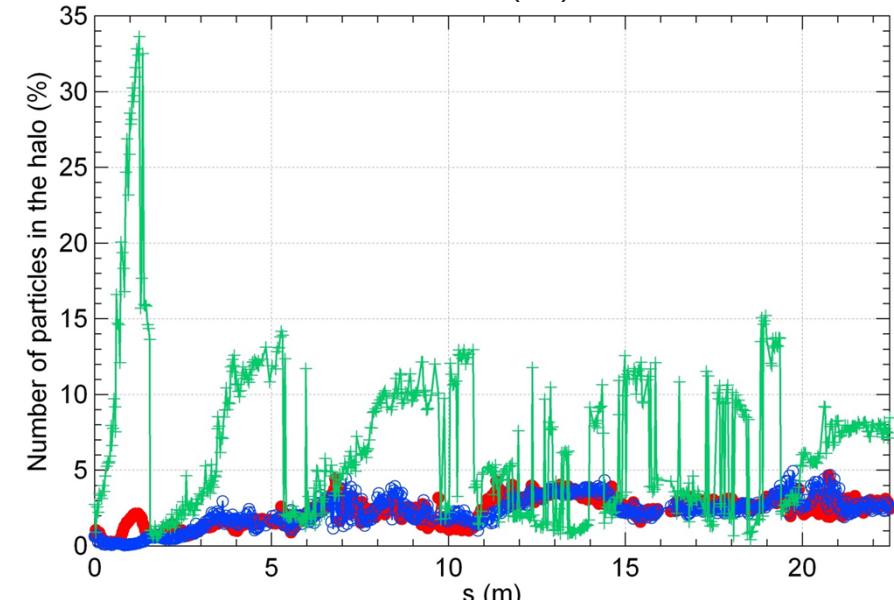
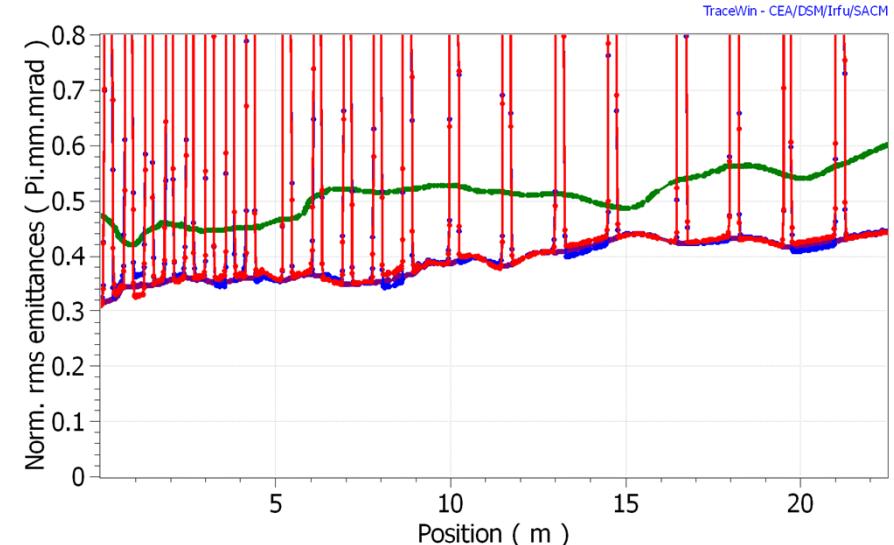
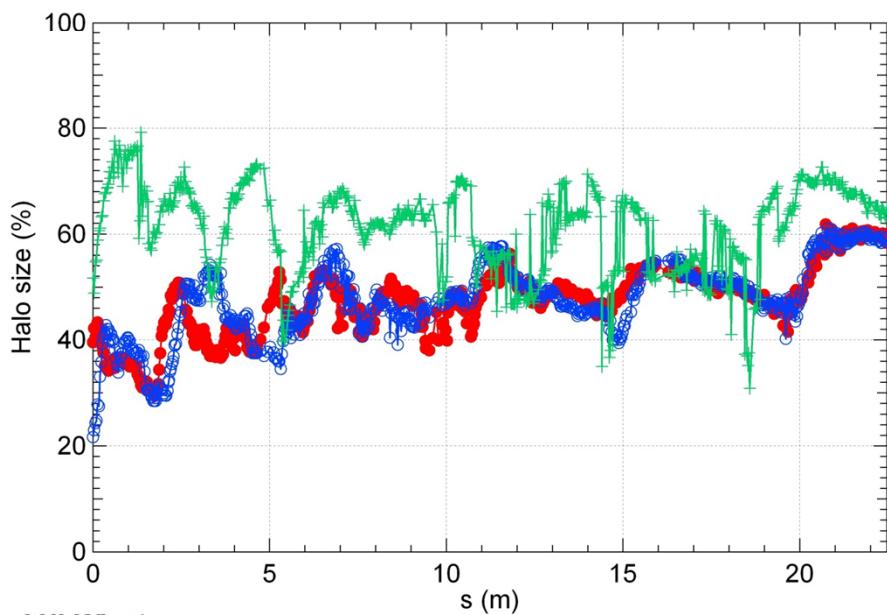
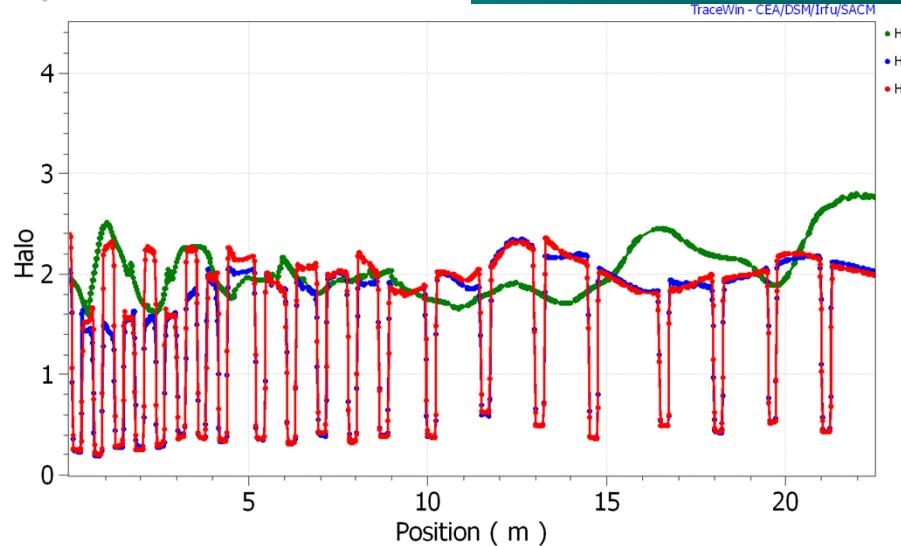




# IFMIF- SRF Linac (case 1)



# IFMIF- SRF Linac (case 2)



- Connections between Halo Parameter and Emittance are not clear
- Halo size (%) or/and NbrPart (%) seem to correspond to Emittance growth
- Even seem to be more detailed beam decscription, more pertinent than Emittance
- Noisy
- To be further explored...

- Other definitions of Halo ?
- Evidence of connections between Halo and Emittance ?
- ...