

Modeling ECRIS Using a 1D Multi-Fluid Code

Michael Stalder

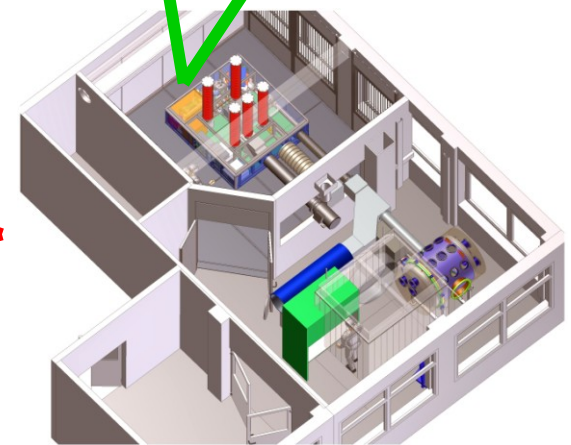
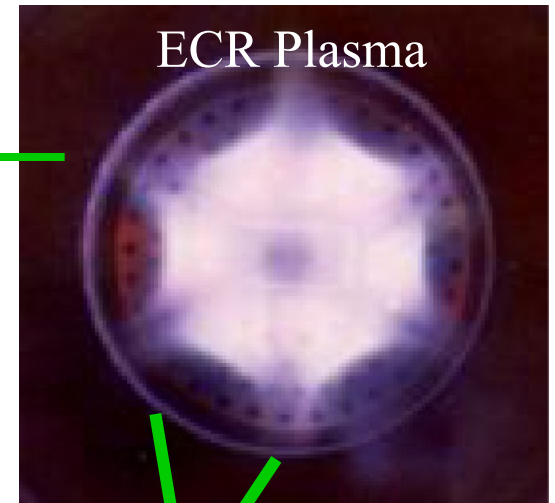
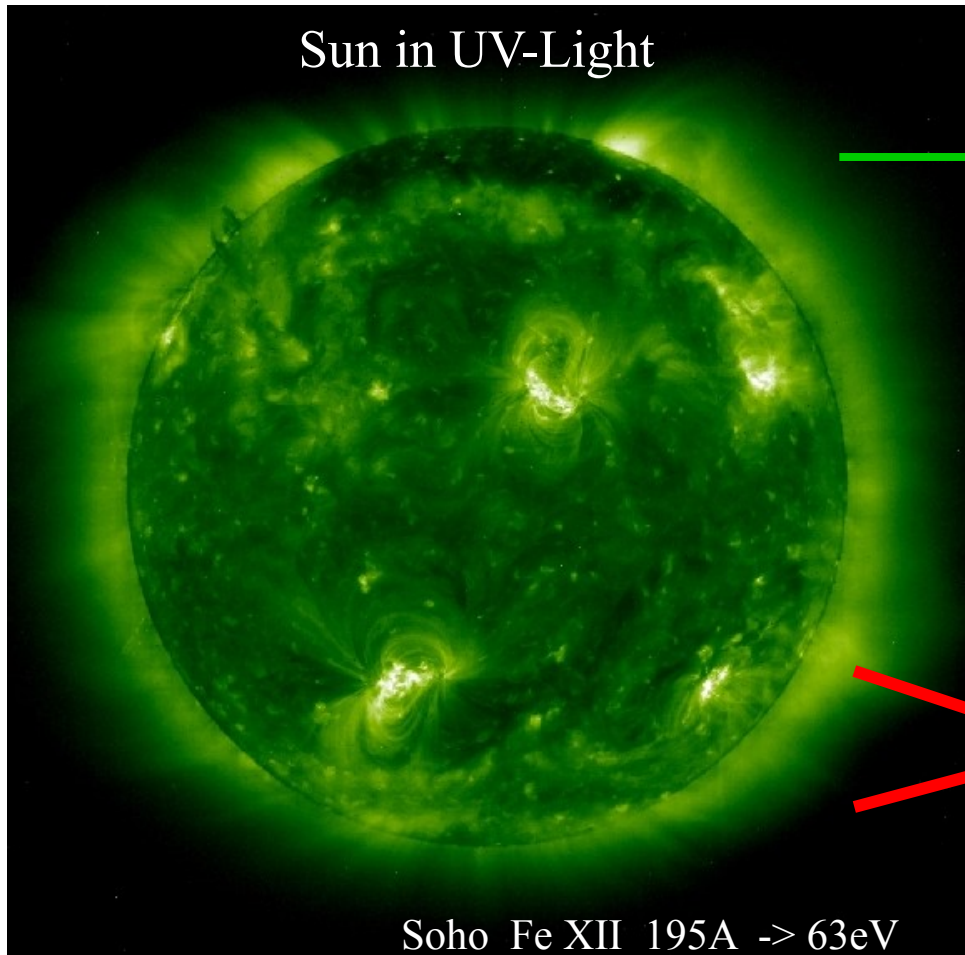
Extraterrestrische Physik
Universität Kiel

Grenoble, 24 Aug. 2010

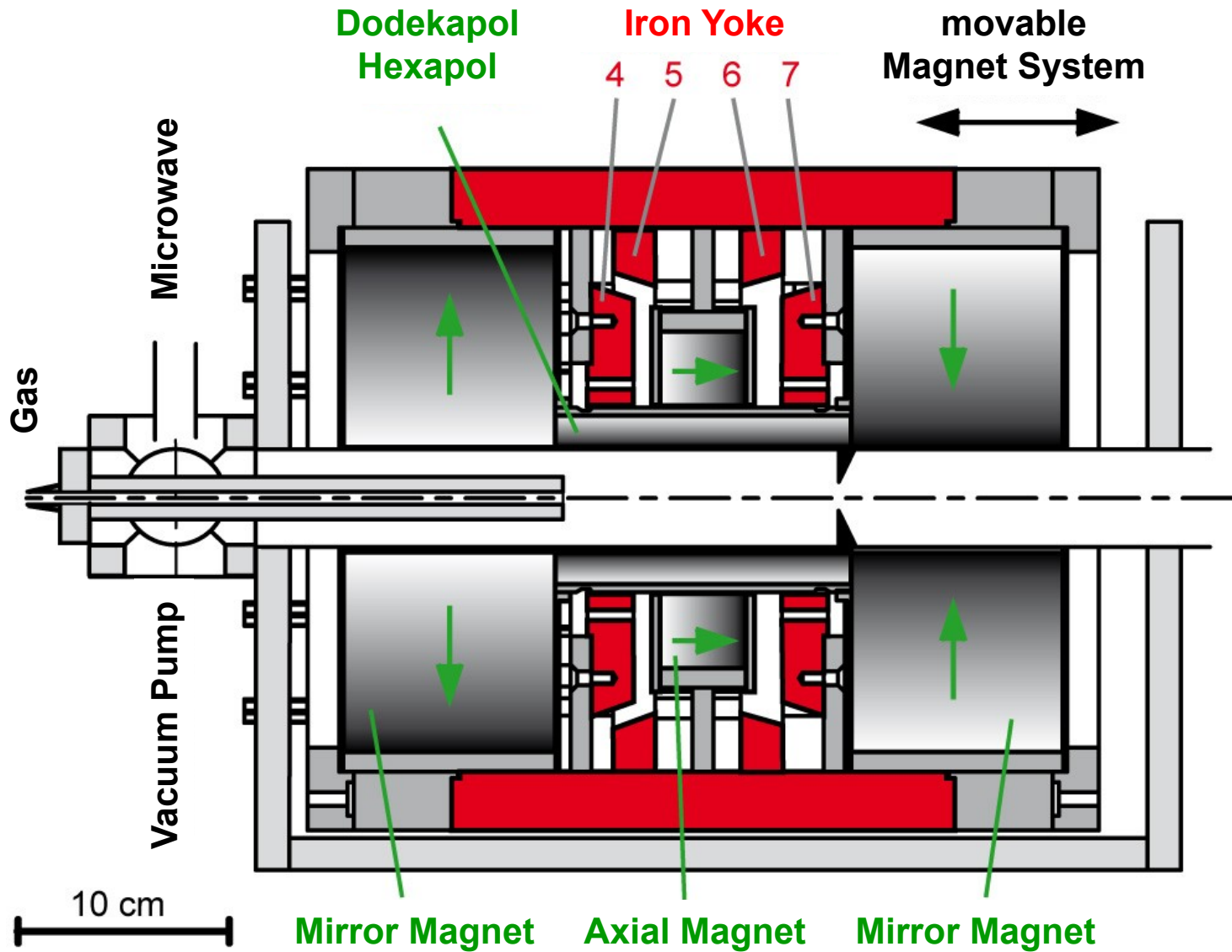
Outline

- Introduction
- The 1D Multi-Fluid Model
- Characteristic Charge State Distributions
- The Influence of the Ion-Temperature T_i
- Conclusions

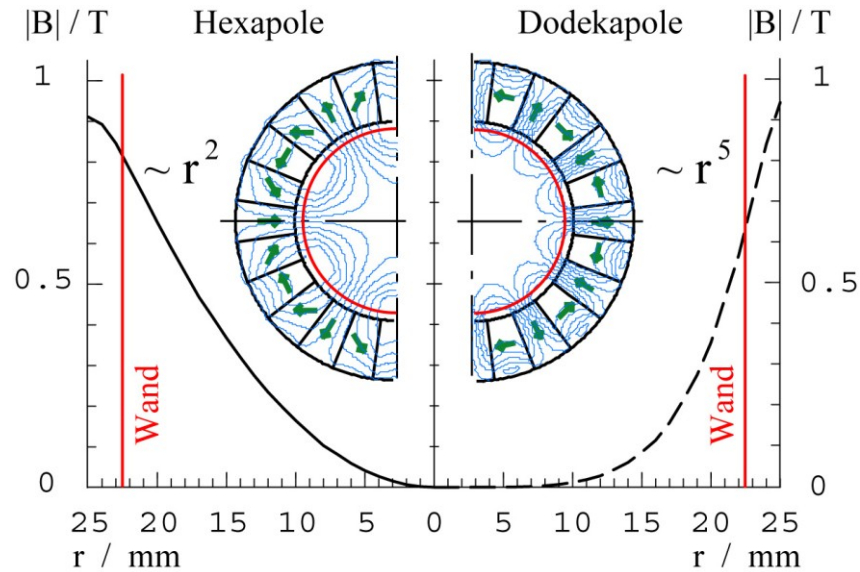
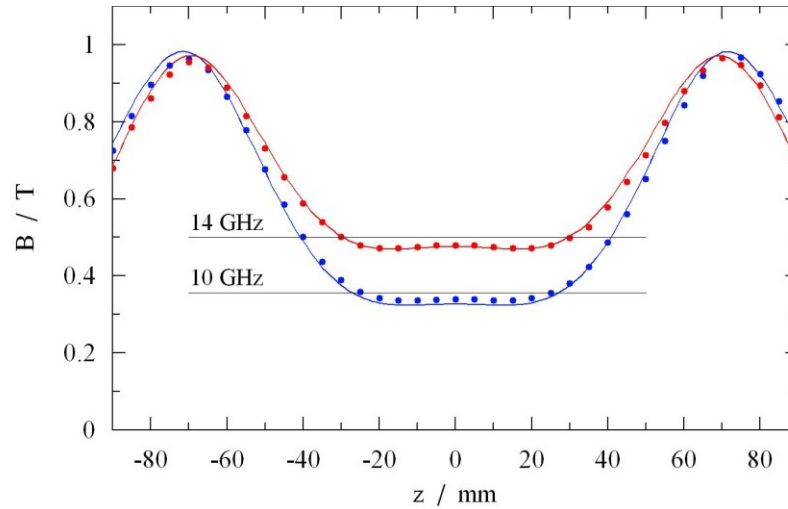
The Solar Wind Calibration Facility



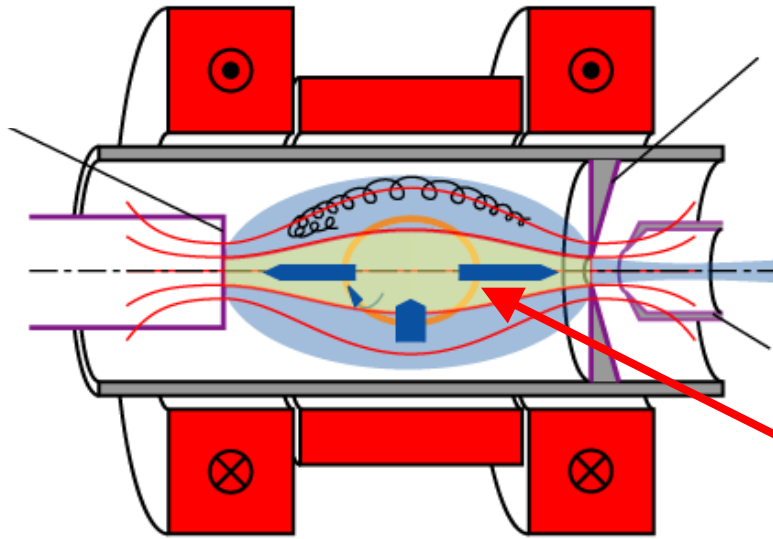
The Kiel ECRIS



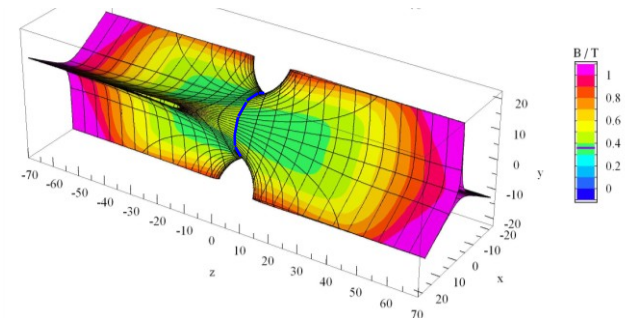
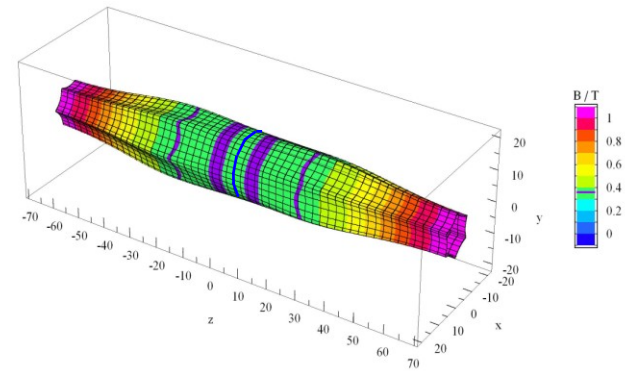
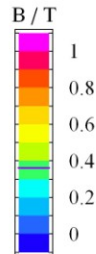
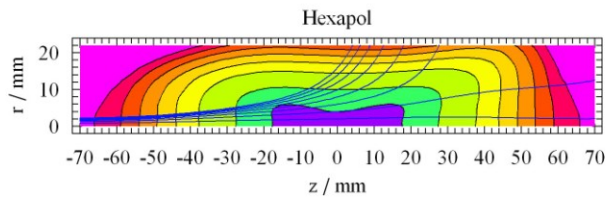
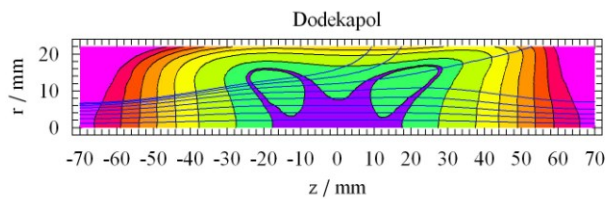
B-Field Simulation and Measurement



Plasma Confinement / B-Field Configuration



- Hot Electrons
trapped magnetically
- Cold Electrons
trapped magnetically and electrically
- Ions
trapped by quasineutrality



The 1D Multi-Fluid Simulation

How is the measured chargestate distribution connected to the plasma parameters?

- What is the influence of the size of the ECRIS
- What is the influence of the drift between the individual ion fluids and of the ion temperature T_i

Basic assumptions for the 1D multi-fluid model:

- Collision-dominated, isotropic ion-populations with constant temperature T_i are treated as individual fluids with interactions caused by friction forces.
- The electron distribution function $f(z,E)$, and the neutral gas pressure n_0 are chosen as free start parameters \rightarrow this model is not selfconsistent!

Simplicity \leftrightarrow Information about the coupling

\rightarrow See the results of Edgell et. al. 2002 (1D); Zaho et. Al. 2007 (2D);

Transport Equations for the 1D Multi-Fluid Simulation

Continuity Equations

$$\begin{aligned}\frac{\partial}{\partial t} n_i(z, t) &= -\frac{1}{A(z)} \frac{\partial}{\partial x} (A(z) n_i(z, t) u_i(z, t)) \\ &\quad + S_{i-1}(z, t) n_e(z, t) n_{i-1}(z, t) - S_i(z, t) n_e(z, t) n_i(z, t) \\ &\quad - R_i n_0 n_i(z, t) + R_{i+1} n_0 n_{i+1}(z, t)\end{aligned}$$

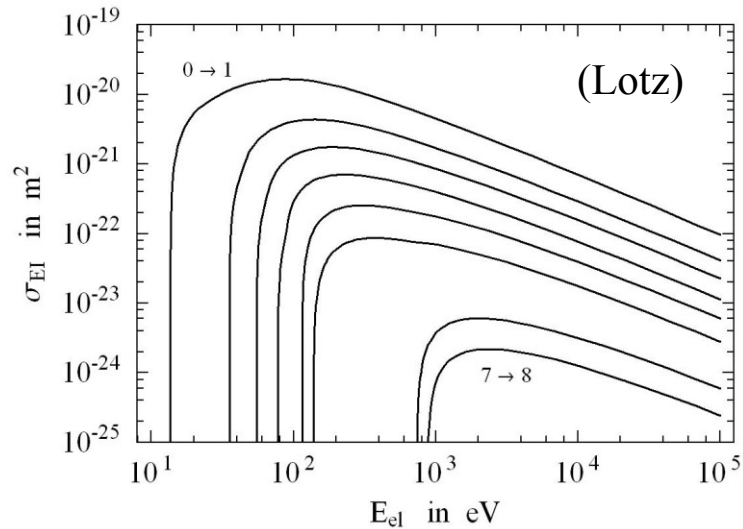
Momentum-Conservation Equations

$$\begin{aligned}m_i n_i(z, t) \frac{\partial}{\partial t} u_i(z, t) &= -\frac{m_i}{A(z)} \frac{\partial}{\partial x} (A(z) n_i(z, t) u_i^2(z, t)) \\ &\quad - \frac{\partial}{\partial x} P_i - q z_i n_i(z, t) \frac{\partial}{\partial x} U \\ &\quad + m_i \sum_j Q_j(z, t) (u_j(z, t) - u_i(z, t)) \\ &\quad + \sum_j R_{i,j} n_i(z, t) n_j(z, t) z_i^2 z_j^2 (u_j(z, t) - u_i(z, t))\end{aligned}$$

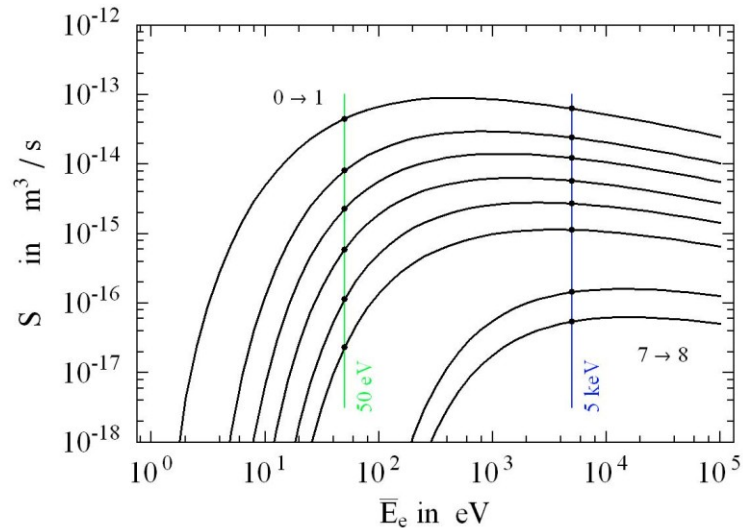
$$\frac{\partial}{\partial x} E(z, t) = -\frac{\partial^2}{\partial x^2} U(z, t) = \frac{1}{\epsilon} \rho(z, t) = \frac{1}{\epsilon} \left(\sum_j n_j(z, t) - n_e(z, t) \right)$$

Oxygen: Ionisation and Recombination

O – Ionisation Crosssections



O – Ionisation Rates



O – Recombination Crosssections

(Müller, Salzborn)

$$\sigma_{z \rightarrow z-1} = A_k z^{\alpha_k} I^{\beta_k}$$

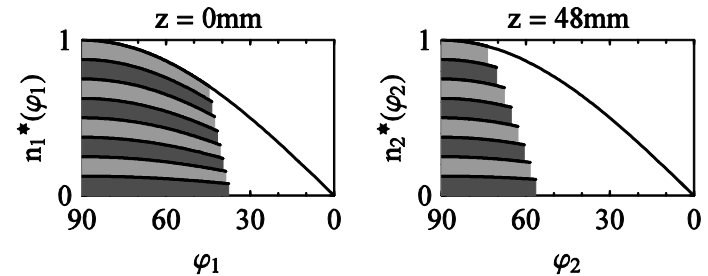
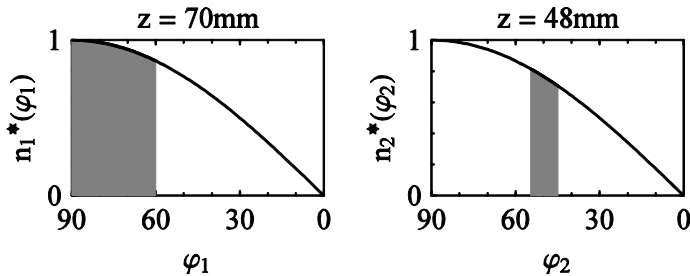
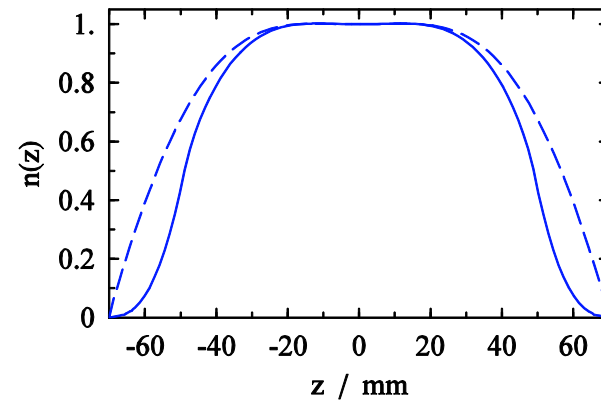
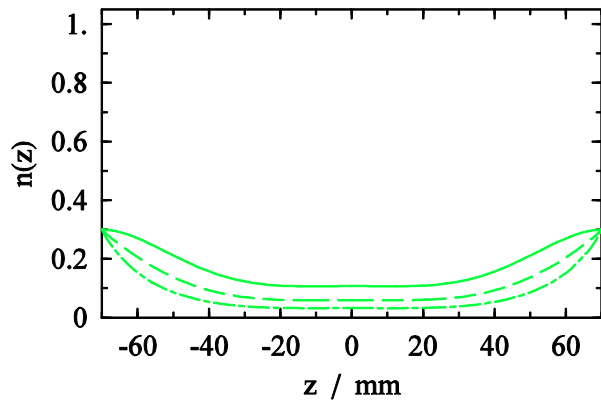
O – Recombination Rates

$$R_i = v_i \sigma_{z \rightarrow z-1} = \sqrt{\frac{2kT_i}{m_i}} \sigma_{z \rightarrow z-1}$$

Electron Density Distribution

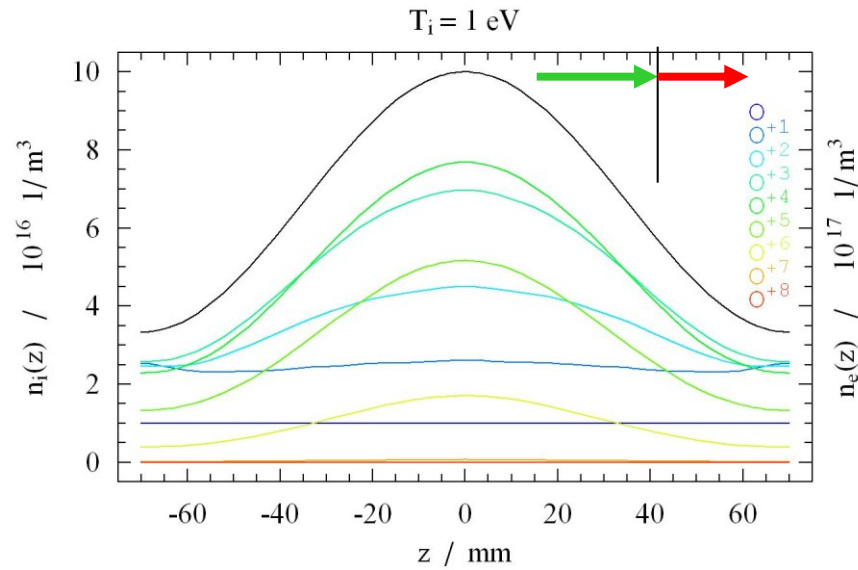
Cold Electrons: $T_e=50\text{eV}$
magnetically and electrically trapped

Hot Electrons: $T_e=5\text{keV}$
magnetically trapped



The ratio of cold to hot electrons is strongly related to the electron density ratio in the middle and at the edge of the ECRIS



Simulation Results for the Density and the Velocity

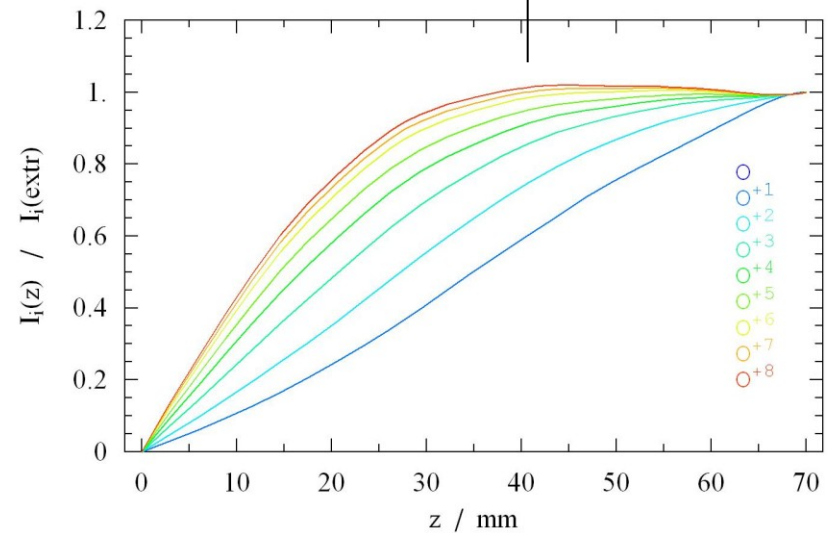
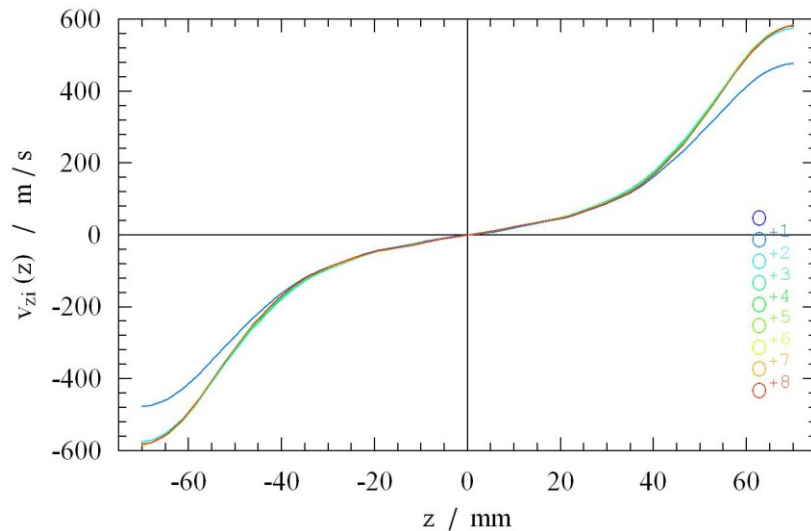


$$n_e = 10^{18} \text{ m}^{-3}$$

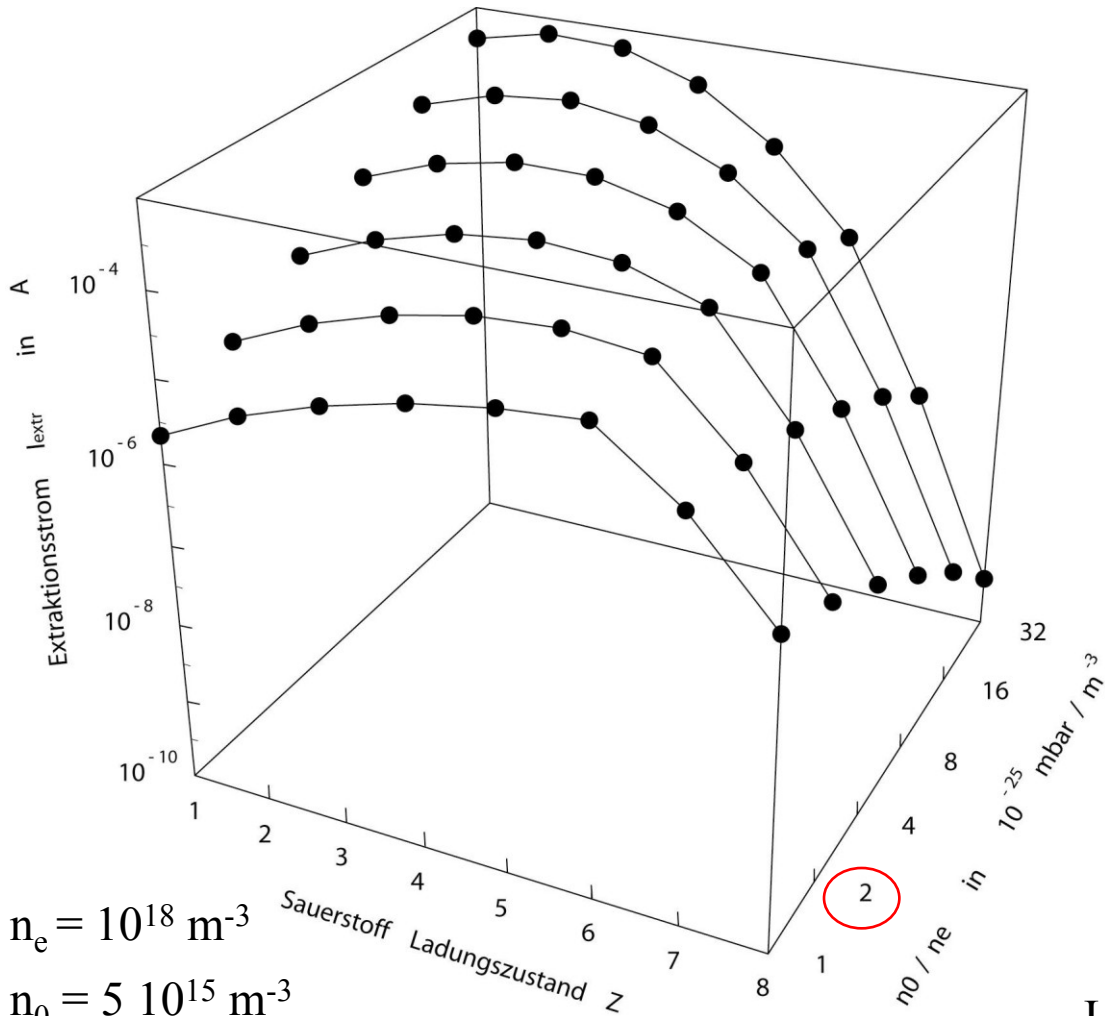
$$n_0 = 10^{16} \text{ m}^{-3}$$

$$p_0 \sim 4 \cdot 10^{-7} \text{ mbar}$$

production  **decay** 



Charge State Distribution as a Function of n_e/n_0



$n_e = 10^{18} \text{ m}^{-3}$
 $n_0 = 5 \cdot 10^{15} \text{ m}^{-3}$
 $p_0 \sim 2 \cdot 10^{-7} \text{ mbar}$

Scaling the size of $L_0 \rightarrow L_1$

$$n_{e1}(z_1) = n_{e0}(z_1 * L_0 / L_1)$$

$$n_{01}(z_1) = n_{00}(z_1 * L_0 / L_1)$$

$$\rightarrow n_{i1}(z_1) = n_{i0}(z_1 * L_0 / L_1)$$

$$\rightarrow u_1(z_1) = L_1 / L_0 * u_0(z_1 * L_0 / L_1)$$

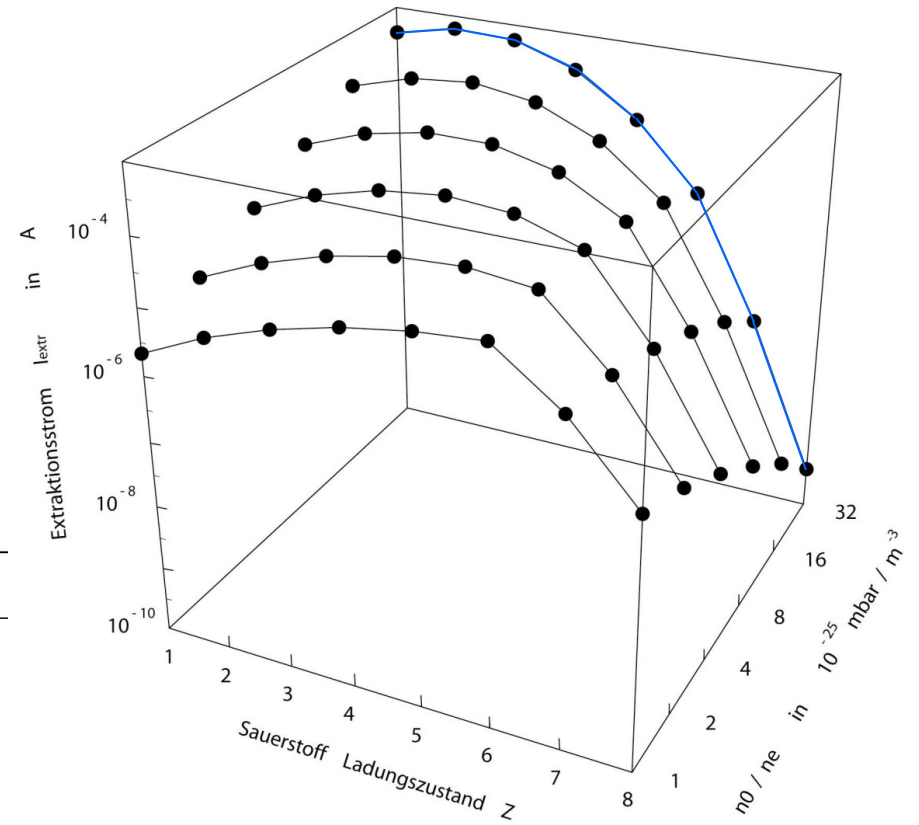
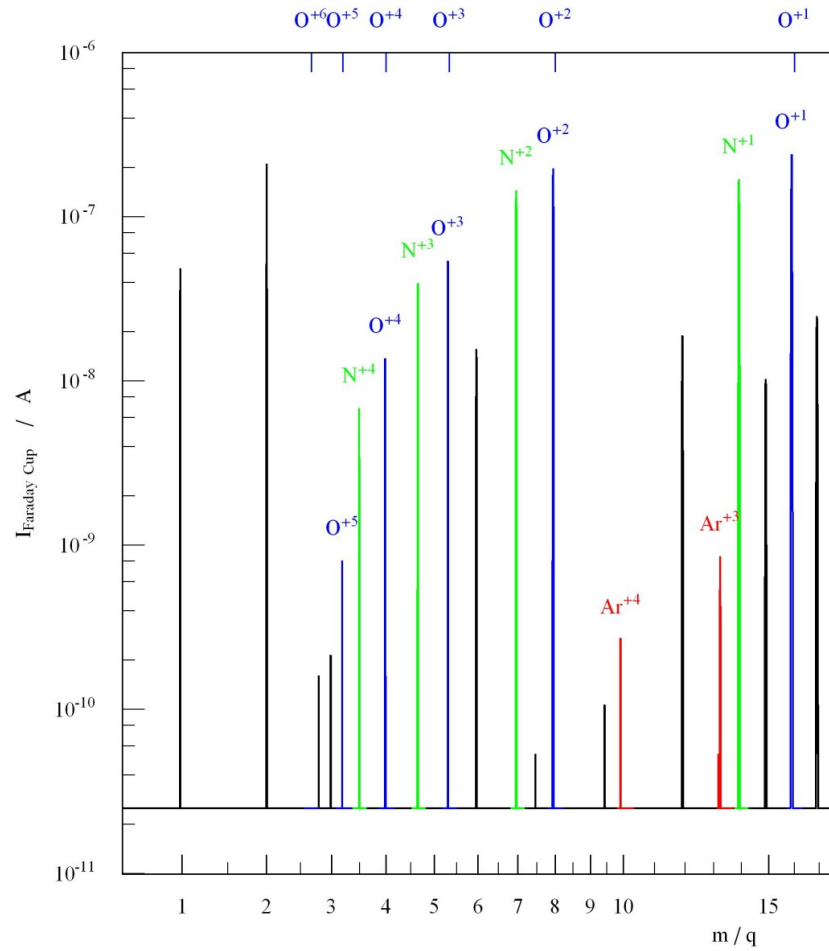
$$\rightarrow \tau_{i0} = \tau_{i1}$$

Similar scaling of the density

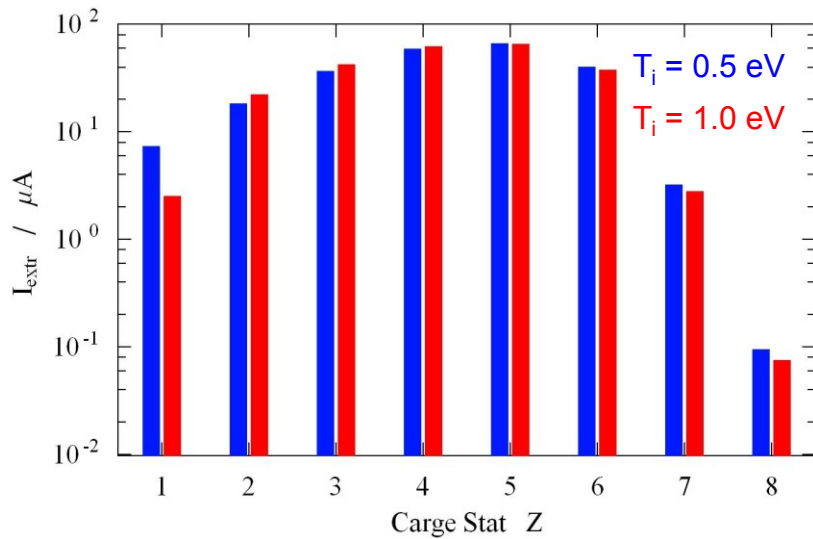
For the extracted currents:

$$I_{i_Extr\ 1} = I_{i_Extr\ 0} * L_1 / L_0 * (n_{e1} / n_{e0})^2$$

Comparison of Measurements and Simulations



The Influence of the Ion Temperature T_i

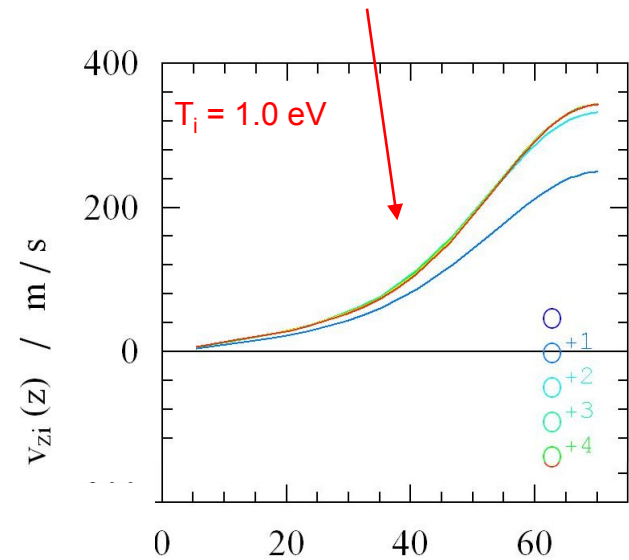
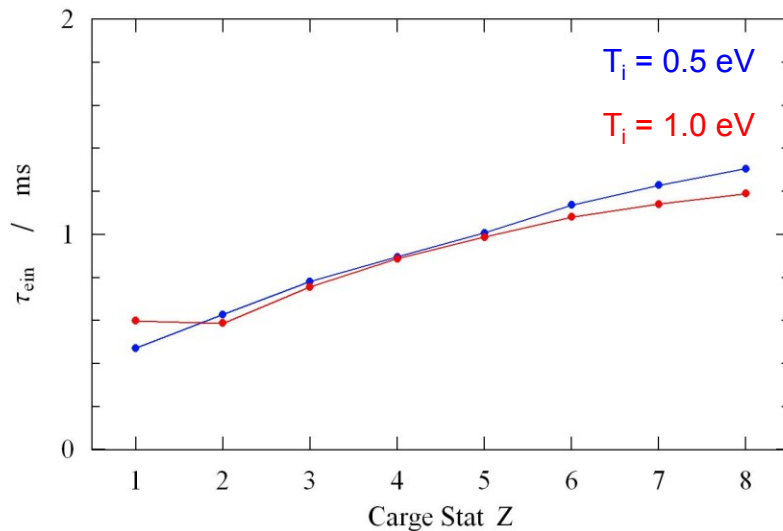


$$n_e = 10^{18} \text{ m}^{-3}$$

$$n_0 = 5 \cdot 10^{15} \text{ m}^{-3}$$

$$p_0 \sim 2 \cdot 10^{-7} \text{ mbar}$$

$$u_{di} \sim \frac{E}{R} \sim \frac{T_i}{T_i^{-3/2}} \sim T_i^{5/2}$$



Conclusions

- The simulations reproduce the expected characteristic charge state distributions
- The influence of individual fluid velocities is small but can be relevant for the higher charge states
- singly charged ions are not well modeled as a fluid
- For medium electron densities ($n_e \sim 10^{18} \text{ 1/m}^3$) ion drifts make about half of the influence of the ion temperature to the extracted currents of highly charged ions
- Very low neutral gas pressure could allow us the production of highly charged ions

Thank You for Your Attention