LOW EMITTANCE LATTICE FOR LEP

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Abstract
In order to obtain the largest luminosity with LEP2, it is attractive to make the beam emittance as small as possible because the beam-beam effect is not a limitation at the energy of \( E \approx 90 \) GeV for the obtained bunch currents. This can be achieved with a high tune lattice. Two possible candidates are lattices with a horizontal phase advance of 108° or 135° per cell. Both have a vertical phase advance of 60°. These lattices were developed during 1994 and the results are presented. Tests to reach high intensity for the 108° lattice were performed and the bunch current achieved is compared with expectations. For this lattice the detuning vs. intensity and several optics parameters were measured as well.

I. INTRODUCTION

The LEP machine was designed for cell phase advances of 60° and 90°. The resulting transverse beam emittance allows reaching the beam-beam limit at the energy of 85 GeV or higher only with bunch currents considerably larger than the ones possible now. It is therefore beneficial to reduce the emittance of the beam to optimize the luminosity. The smallest emittance is obtained for a cell phase advance of about 135°. The significant luminosity gain to be expected from a smaller emittance is enhanced by the smaller beam size at the collimators close to the low-\( \beta \) quadrupoles, allowing to decrease \( \beta^* \) and thus further increase the luminosity [1]. Unlike synchrotron light sources, strong chromatic aberrations are generated by the low-\( \beta \) insertions which have to be corrected by the cell sextupoles. To avoid a too strong perturbation to the beam motion, they must be arranged in pairs at an odd multiple of 180°, constraining the cell phase advance to 90°, 108° or 135°, [2]. The reduced dispersion function demands an increased strength of the sextupoles which enhances the non-linear perturbation to the beam motion. Fortunately the largest chromatic aberration is in the vertical plane, where the cell phase advance can be kept low, thereby reducing somewhat the sextupole excitation. The stronger focusing shortens the bunch length and decreases the threshold for the transverse mode coupling instability. Conversely, the RF bucket is larger, making it possible to slightly increase the beam energy in a critical range. The ultimate gain in luminosity reaching 3.5, a theoretical and experimental study was initiated to investigate the potential of a minimum emittance lattice.

II. HIGH TUNE LATTICES

A. 135/60 lattice.

In this lattice the arc FODO cells have a horizontal phase advance of 135° and a vertical phase advance of 60°. The horizontal tune is 125.28 and the vertical tune is 75.18. Given the machine super-periodicity, such tunes guarantee that no problem is expected from the non-linear chromaticity and two sextupole families are sufficient [3].

Since early runs in 1993 could not obtain a circulating beam the problems associated with this lattice were studied extensively [4] with the outcome that it is not possible to correct both the third order resonances and the derivative of the horizontal tune with respect to the horizontal emittance. The latter has a value of \(-1.6 \times 10^5\) m\(^{-1}\) for the lattice under consideration. For an rms closed orbit amplitude of 4mm at the BPM’s where \( \beta_z \) is about 10m, the associated emittance is about 1.6μrad.m, which makes an associated horizontal tune-shift of -0.26. As the fractional part of the horizontal tune of our machine is 0.28, we see that a badly corrected closed orbit can easily lead to a linear instability. In addition, the orbit excursions in the sextupoles lead to a widening of the second order stop-band which can reach a width of 0.15 for an rms closed orbit deviation of 0.5 mm.

In practice it can be observed that the horizontal tune, estimated from a Fourier analysis of the measurements over several turns, wanders considerably depending on the trajectory corrections applied. It is important to note that applying a tune-shift does not help because of these large tune changes.

In 1994 great care was taken to correct the first turn trajectory so that its r.m.s. value was between 3 and 2mm. Then the orbit closure algorithm [5] was applied and a circulating beam was obtained after having applied it iteratively and having made a systematic horizontal tune-shift of about +0.2 in order to compensate for the anharmonic effects. Another experiment devoted to accumulate more current had various troubles and only 59μA were stored with the damping wigglers on. This is not limited by collective effects.

B. 108/60 lattice

In 1994, in parallel with the analysis of the problems of the 135°/60° lattice, a 108°/60° lattice was developed from the 90°/60° lattice of 1994, which was the one used for operating LEP at this time. This 108°/60° lattice has now two horizontal and three vertical sextupole families. It was developed for machine developments purposes and is not yet optimized for pretzel or bunch train operation. The derivative of the horizontal tune with respect to the horizontal emittance was 2.26 \( 10^4 \) m\(^{-1}\) the one in the vertical plane was \( 7.37 \times 10^4 \) m\(^{-1}\), and the cross term (derivative of the vertical tune with respect to the horizontal emittance) was \(-7.97 \times 10^4 \) m\(^{-1}\). For a given orbit distortion the maximum detuning is reduced by 50% compared to the 135°/60° lattice. Although still large, it is sufficiently reduced to obtain easy injection, accumulation in the first experiment.

Five experiments were performed in order to test the performances of the 108° lattice. They were very successful and proved the easy operation of the machine with this lattice, from
the injection, accumulation to the ramp and squeeze. Various measurements were done which are developed in the following chapter.

C. Collective effects

One of the problems encountered by the high tune lattices is the small momentum compaction factor $\alpha_c$. The smaller emittance is obtained by strong focusing resulting in small values of the horizontal dispersion function $D_x$ and consequently in a reduction of the transverse quantum excitation by the emitted synchrotron radiation. This reduces also the momentum compaction $\alpha_c$ and the synchrotron tune $Q_s$. The bunch current in LEP is limited by the transverse mode coupling instability (TMI). The tunes of the different head-tail modes are separated at small current by $Q_s$. At larger current the transverse impedance causes tune shifts which can bring two modes together resulting in an instability. Obviously, a large basic separation $Q_s$ of the modes gives a higher TMI threshold. The effective impedance involved tends to increase with reduced bunch length $\sigma_s$. Since increasing $Q_s$ will at the same time decrease $\sigma_s$, the maximum bunch current improves only slowly with $Q_s$ as shown in Fig. 1. Some gain in current can be obtained with wigglers located in dispersion free sections. They increase the energy spread of the beam and therefore also the bunch length. Two groups of such wigglers are available in LEP called damping (DW) and polarization (PW) wigglers according to their original purpose. The beneficial effect of these devices is also indicated in Fig. 1.

D. Phase advance in the vertical plane

The choice of $60^\circ$ vertical phase advance per cell was motivated by the need to guarantee a good non-linear chromaticity correction and also a good vertical orbit correction for polarization. This is not without consequence for the collective effects. Moving from $90^\circ$ to $60^\circ$ in the vertical plane increases the average vertical $\beta$-function in the arcs by up to 30-40% when averaging over all the bellow positions in the arcs (e.g. when moving from a $90^\circ$ to a $135^\circ$ lattice). Since for the present bunch length the bellows represent about half of the total impedance in the vertical plane, the resulting reduction of the maximum intensity at injection (at fixed $Q_s$) would thus amount to 15-20%. This is not negligible and could even annihiliate the gain expected from the reduced emittances. In the case where a vertical phase advance of $90^\circ$ is not ruled out by polarization considerations, a $108^\circ$ lattice ($\langle \beta_y \rangle = 71.0$ m in the arcs) would become a very interesting candidate for LEP2.

III. COMPARISON OF THE DIFFERENT OPTICS

A comparison between the different optics presently considered for the operation of LEP2 is presented in Table I. It has been assumed that average $\beta$ value in the straight sections can be kept the same for all three optics and we concentrate on the variations in the arcs. Similarly, only the horizontal emittance is quoted, since the ultimate value of the vertical one will strongly depend on our ability to correct both the dispersion and the coupling.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>$90^\circ/60^\circ$</th>
<th>$108^\circ/60^\circ$</th>
<th>$135^\circ/60^\circ$</th>
</tr>
</thead>
<tbody>
<tr>
<td>integer $Q_x$</td>
<td>90</td>
<td>102</td>
<td>125</td>
</tr>
<tr>
<td>integer $Q_y$</td>
<td>76</td>
<td>76</td>
<td>75</td>
</tr>
<tr>
<td>mom. comp. $\alpha$</td>
<td>0.000186</td>
<td>0.000138</td>
<td>0.000102</td>
</tr>
<tr>
<td>$\beta_x$ in QF [m]</td>
<td>122.0</td>
<td>130.2</td>
<td>178.5</td>
</tr>
<tr>
<td>$\beta_y$ in QF [m]</td>
<td>25.5</td>
<td>18.2</td>
<td>10.2</td>
</tr>
<tr>
<td>$\beta_y$ in QD [m]</td>
<td>41.0</td>
<td>38.7</td>
<td>36.5</td>
</tr>
<tr>
<td>$\sigma_y$ in QD [m]</td>
<td>152.7</td>
<td>162.3</td>
<td>175.3</td>
</tr>
<tr>
<td>$\langle \beta_x \rangle$ in arcs [m]</td>
<td>64.1</td>
<td>63.2</td>
<td>75.4</td>
</tr>
<tr>
<td>$\langle \beta_y \rangle$ in arcs [m]</td>
<td>85.7</td>
<td>87.6</td>
<td>92.5</td>
</tr>
<tr>
<td>$D_x$ in QF [m]</td>
<td>1.13</td>
<td>0.88</td>
<td>0.68</td>
</tr>
<tr>
<td>$D_y$ in QD [m]</td>
<td>0.60</td>
<td>0.42</td>
<td>0.28</td>
</tr>
<tr>
<td>$s_y$ (90 GeV) [mm]</td>
<td>$\approx 11.0$</td>
<td>$\approx 8.2$</td>
<td>$\approx 6.0$</td>
</tr>
</tbody>
</table>

Table I

Comparison between different LEP2 optics

![Figure 1](image-url) Calculated and measured TMCI thresholds vs. $Q_s$ for two settings of damping and polarization wigglers DW and PW

IV. RESULTS FROM EXPERIMENTS FOR THE 108° LATTICE

A. Current limitations and high $Q_s$

With the damping wigglers alone and a synchrotron tune of 0.08, the maximum intensity reached was 480 $\mu$A per bunch. This limit was due to transverse mode coupling instabilities and is not much smaller than the value obtained with the $90^\circ/60^\circ$ lattice, under the same conditions. Using the polarization wigglers in addition and with a $Q_s=0.093$, the maximum intensity reached 560 $\mu$A per bunch. Increasing $Q_s$ to 0.097 gave a maximum intensity of 580 $\mu$A per bunch, which agrees well with the current of 620 $\mu$A predicted by simulation for the TMCI as shown in Fig. 1. This value is also very close to the single beam
same distortions can create relatively large spurious dispersions which one is not surprising. In a high tune lattice modest orbit

tions by the program WIGWAM [8] and listed in Table III. The

tance (to 0.07 m) gave a negative vertical chromaticity and the beam

The emittance, being a significant parameter of this lattice,

The changes of the betatron tunes with bunch current are good

During the last 1994 experiment, the beam was ramped to 46

During the ramp, it was observed that each horizontal orbit
correction led to a change of both tunes caused by the large sextupole strength as expected. This was as well the case after the
ramp and during the squeeze. After few iterations of orbit
corrections, the chromaticities were measured to be $Q'_x = 1.1$ and
$Q'_y = 1.6$. The vertical rms dispersion was found to be 6 cm.

The emittance, being a significant parameter of this lattice,

limit of 630 μA obtained presently with the 90°/60° lattice for the
same $Q_s$ [6]).

The changes of the betatron tunes with bunch current are good
measures for the effective transverse impedances and were measured to be $dQ_x / dI_b = -77 \text{ A}^{-1}$ and $dQ_y / dI_b = -130 \text{ A}^{-1}$, Fig. 2.

Table II

<table>
<thead>
<tr>
<th>$\Delta f_x$ (Hz)</th>
<th>$Q_x$</th>
<th>$Q_y$</th>
<th>$\epsilon_x$ (nm)</th>
<th>$\epsilon_y$ (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-50</td>
<td>0.259</td>
<td>0.181</td>
<td>12.15</td>
<td>1.31</td>
</tr>
<tr>
<td>0</td>
<td>0.258</td>
<td>0.179</td>
<td>9.43</td>
<td>1.24</td>
</tr>
<tr>
<td>+50</td>
<td>0.257</td>
<td>0.177</td>
<td>7.79</td>
<td>1.28</td>
</tr>
</tbody>
</table>

B. Optics and emittance measurements

During the last 1994 experiment, the beam was ramped to 46
GeV. During the ramp, it was observed that each horizontal orbit
correction led to a change of both tunes caused by the large sextupole strength as expected. This was as well the case after the
ramp and during the squeeze. After few iterations of orbit
corrections, the chromaticities were measured to be $Q'_x = 1.1$ and
$Q'_y = 1.6$. The vertical rms dispersion was found to be 6 cm.

The emittance, being a significant parameter of this lattice,

was lost. This could be corrected easily but further trials were
postpone due to lack of time. The easiness with which the ramp
and partial squeeze could be performed indicates that no prob-
lems are expected for the operations of the 108°/60° lattice.

V. CONCLUSIONS

High tune lattices giving small emittances are promising
means to obtain a high luminosity for LEP operation at 90 GeV
where the bunch current is limited by instabilities at injection
and not by the beam-beam effect in collisions. Solutions have
been worked out and tried experimentally for horizontal phase
advances per cell of 135° and 108°. The first configuration gives
about the smallest emittance possible in a regular FODO-lattice.
The strong horizontal focussing obtained in these lattices leads
to a small synchrotron tune and bunch length for a given RF-
voltage. This reduces the threshold for the transverse mode cou-
pling instability. The wiggler magnets available in LEP have to
be used to lengthen the bunch and to keep the current reduction
within limits. For the 108°-lattice a bunch current of over 0.6
mA has been achieved which is close to the expected limit. Fur-
thermore, the emittance measured at 46 GeV is not much above
the calculated value. Other parameters have been checked and the
β function in the interaction points partially reduced. These
results clearly show that high luminosity operation of LEP at 90
GeV is feasible and that the 108°/60° lattice is a good candidate
for LEP2.

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