

ADVANCED ELECTRIC AND MAGNETIC MATERIAL MODELS FOR FDTD ELECTROMAGNETIC CODES *

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Abstract

The modeling of dielectric and magnetic materials in the time domain is required for pulse power applications, pulsed induction accelerators, and advanced transmission lines. For example, most induction accelerator modules require the use of magnetic materials to provide adequate Volt-sec during the acceleration pulse. These models require hysteresis and saturation to simulate the saturation wavefront in a multipulse environment. In high voltage transmission line applications such as shock or soliton lines the dielectric is operating in a highly nonlinear regime, which require nonlinear models. Simple 1-D models are developed for fast parameterization of transmission line structures. In the case of nonlinear dielectrics, a simple analytic model describing the permittivity in terms of electric field is used in a 3-D finite difference time domain code (FDTD). In the case of magnetic materials, both rate independent and rate dependent Hodgdon magnetic material models have been implemented into 3-D FDTD codes and 1-D codes.

INTRODUCTION

The interaction of transient high power electromagnetic pulses with materials requires the inclusion of nonlinear effects in the constitutive relation for the material. For example, nonlinear dielectrics or nonlinear ferrites are utilized in electromagnetic shock lines to sharpen the leading edge of a pulse [1]. Nonlinear materials can also be used in periodic arrays in transmission lines to generate solitons where the “balance” of dispersion and nonlinearity is used to propagate pulses with minimal distortion [2]. Understanding the effect of saturation and hysteresis in a magnetic ferrite is of importance in the design of induction accelerator cells in order to insure a minimal leakage current. In this paper we discuss the inclusion of a simple nonlinear permittivity model and the Hodgdon magnetic material model [3] into a FDTD electromagnetic code.

MODELING

The inclusion of realistic models of the constitutive properties of electric and magnetic materials is a requisite for the proper design of electromagnetic structures. For pulse power applications, when dealing with short high amplitude electromagnetic pulses it is required to incorporate nonlinear models of the materials into modeling codes. The electromagnetic modeling code

XFDTD [4] has been used extensively for modeling transient linear electromagnetics. It incorporates the unique feature of allowing lumped circuit elements, including resistors, capacitors, inductors, and opening and closing switches to be incorporated into the model making it a useful tool for pulse power applications. The code includes models for, lossy anisotropic dielectrics, and Debye and Lorentzian dielectric dispersion. Magnetic models include magnetized ferrites, and Debye dispersion. For high field applications models for nonlinear anisotropic dielectrics and saturable magnetic materials with hysteresis were developed for XFDTD. Several test problems were set up in XFDTD in a geometry that approximated a 1-D problem. Doing this allowed us to use the 1-D PDE solver, FEMLAB [5] to compare solutions from the two independent solvers to check the validity of the implementation in XFDTD.

Nonlinear Dielectric Materials

Eq.1 defines the nonlinear permittivity function implemented in XFDTD. It was chosen to provide a sufficient number of free parameters to model a variety of dielectric materials,

$$\epsilon_r = \epsilon_{r2} + \frac{\epsilon_{r1} - \epsilon_{r2}}{1 + a_1 (E/E_0)^2 + a_2 (E/E_0)^4 + a_3 (E/E_0)^6} \quad (1)$$

where ϵ_1 , ϵ_2 , E_0 , and a_i are parameters used to define the nonlinear function.

Figure 1 shows a simple classical problem consisting of a parallel plate transmission line with a block of nonlinear material inserted between the plates.

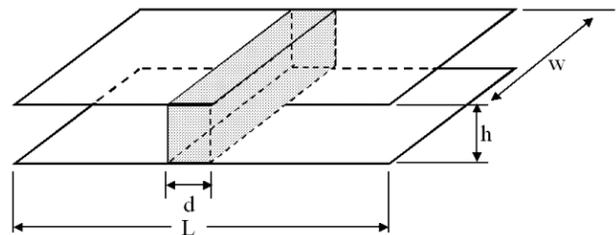


Figure 1: Stripline with block of nonlinear dielectric.

If the plates are sufficiently wide compared with the distance between the plates, the problem is approximately 1-D and can be modeled by 1-D Maxwell equations. The dimensions of the stripline are; $L = 400$ cm, $d = 50$ cm, $w = 9$ cm, and $h = 3$ mm. The parameters for the dielectric material are; $\epsilon_1 = 4$, $\epsilon_2 = 1$, $a_1 = 1$, $a_2 = a_3 = 0$, and $E_0 = 100$ kV/m. Figure 2 shows a plot of the nonlinear

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dielectric function. The line is driven with a 100 kV/m Gaussian pulse with a FWHM of 1 ns at the left end of the transmission line.

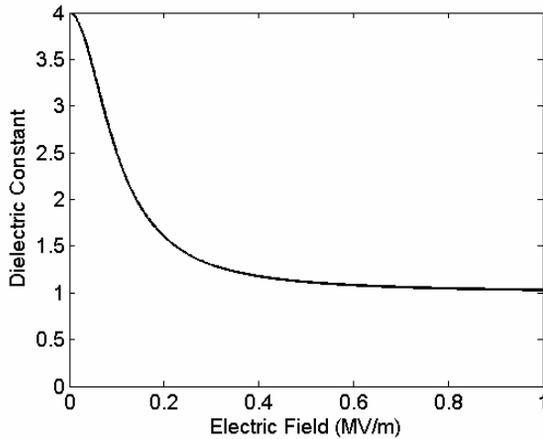


Figure 2: Nonlinear dielectric function for test problem.

Figures 3 and 4 show the temporal evolution of the electric field pulse 25 cm before and after the material. Figure 3 shows the 100 kV/m incident pulse along with reflections from the front and back edges of the material. The reflection from the back surface shows the shock front produced by traversal through the material.

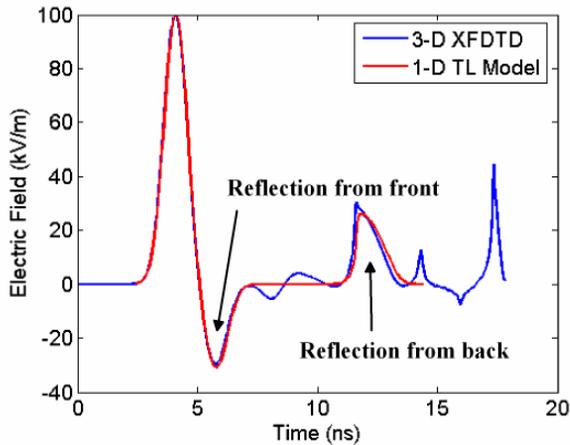


Figure 3: Electric field 25 cm before dielectric insert.

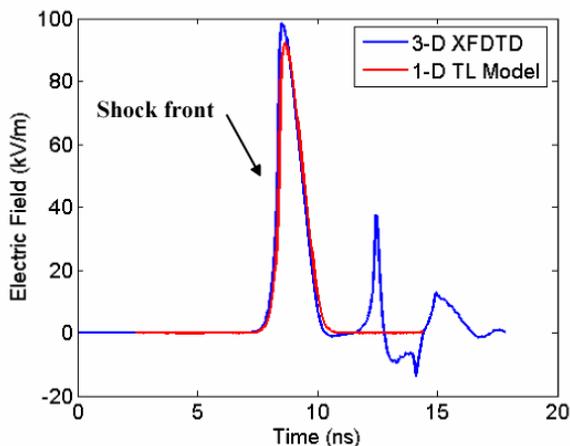


Figure 4: Electric field 25 cm after dielectric insert.

Figure 4 again clearly shows the development of the sharpened rise time produced by the nonlinear dielectric. The late time behavior in the 3-D results from a poorly matched load at the right side of the transmission line. The 1-D calculations are useful to parameterize or optimize a system before utilizing a full 3-D description of the problem since the 3-D calculations take a substantially longer time.

Saturable Magnetic Materials and Hysteresis

To model ferromagnetic hysteresis, both the rate independent and rate dependent Hodgdon magnetic material models [3] were implemented into the XFDTD code. The implementation of the Hodgdon material model is substantially more difficult than the nonlinear dielectric model, since in that case the dielectric permittivity is expressed explicitly as a function of the electric field while in the case of the Hodgdon model, the permeability is described by a nonlinear differential equation in terms of the magnetic field and the magnetic flux vector. Eq. 2 defines the permeability in terms of B , H , and \dot{B} .

$$\mu(B, H, \dot{B}) = \left\{ \alpha \operatorname{sgn}(\dot{B}) [f(B) - H] + g(B, \dot{B}) \right\}^{-1} \quad (2)$$

where

$$f(B) = \begin{cases} A_1 \tan A_2 B, & |B| \leq B_{bp} \\ A_1 \tan A_2 B_{bp} + (B - B_{bp})/\mu_s, & B > B_{bp} \\ -A_1 \tan A_2 B_{bp} + (B + B_{bp})/\mu_s, & B < -B_{bp} \end{cases}$$

and

$$g(B, \dot{B}) = f'(B) \left[1 - A_3 c(\dot{B}) \exp\left(-\frac{A_4 |B|}{B_{cl} - |B|}\right) \right]$$

if $|B| \leq B_{cl}$ and $g(B, \dot{B}) = f'(B)$ otherwise. The term, $c(\dot{B})$ is defined by

$$c(\dot{B}) = \begin{cases} 1 + c_1 |\dot{B}|, & |\dot{B}| < \dot{B}_1 \\ 1 + c_1 \dot{B}_1 + c_2 (|\dot{B}| - \dot{B}_1), & \dot{B}_1 \leq |\dot{B}| \leq \dot{B}_2 \\ 1 + c_1 \dot{B}_1 + c_2 (\dot{B}_2 - \dot{B}_1) \\ \quad + c_3 (|\dot{B}| - \dot{B}_2), & |\dot{B}| > \dot{B}_2 \end{cases}$$

Here the constants α , μ_s , A_i , B_{bp} , B_{cl} , and the function $c(\dot{B})$ are material parameters as described in

[3]. The function $c(\dot{B})$ defines whether the model is rate independent ($c_i = 0$) or rate dependent ($c_i \neq 0$).

Figure 5 shows a simple coaxial geometry with a 2 cm thick ferrite disk inserted into the transmission line. The code simulations were done for CN20 ferrite. The inner and outer radius of the line is 8 cm and 10 cm respectively.

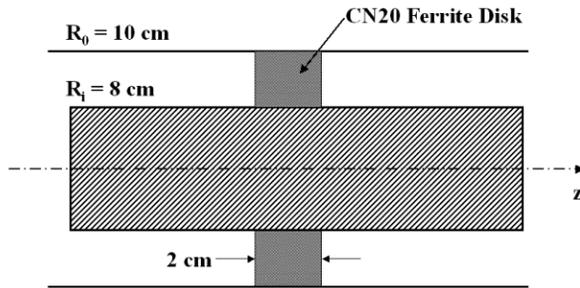


Figure 5: Coaxial transmission line with ferrite insert.

A reasonable 1-D approximation for this problem can be made since the magnetic flux lines close within the material and the ratio of outer to inner conductor radius is only slightly larger than unity. This last approximation is required to insure that the fields are relatively uniform across the radius and hence remain primarily TEM in the structure. The rate independent parameters for CN20 ferrite are; $B_{cl} = 0.4$ T, $B_{pp} = .4103$ T, $H_{cl} = 397.9$ A/m, $\mu_s = 2\mu_0$, $\alpha = 10$ T⁻¹, $A_1 = 21.19$ Amp/m, $A_2 = 3.794$ T⁻¹, $A_3 = -4.489$, and $A_4 = .3046$. The rate dependent parameters are; $c_1 = 13.3 \times 10^{-7}$ (T/s)⁻¹, $c_2 = 8 \times 10^{-7}$ (T/s)⁻¹, $\dot{B}_1 = 7.5 \times 10^5$ (T/s) and $\dot{B}_2 \rightarrow \infty$. A TEM Gaussian pulse of approximate amplitude 314 kV/m and FWHM of 6.65 ns is incident on the ferrite from the left. Figure 6 shows a plot of the hysteresis loop determined by direct integration of Eq. 2.

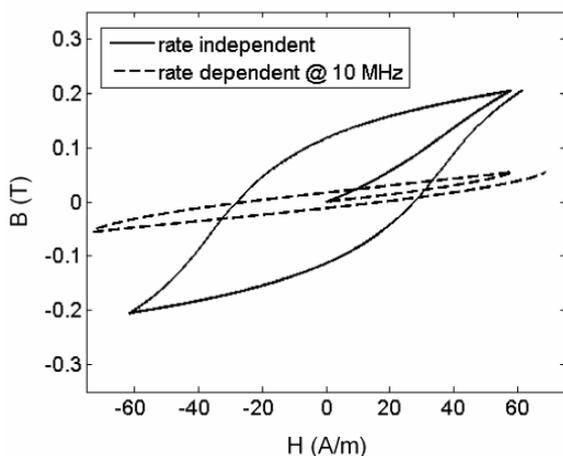


Figure 6: Hysteresis curves for CN20 ferrite.

In the linear regime, the material exhibits a permeability of approximately 1800 for the rate independent calculation and 497 at 10MHz. Similar calculations show a permeability of 228 at 80 MHz. The

rate dependent results clearly show a dramatic effect in the reduction of the permeability. Figure 7 shows the transmitted pulse through the geometry shown in Fig. 5 for the 1-D and 3-D rate independent calculations. Figure 8 shows a comparison of the permeability calculation for the rate independent and rate dependent cases. The rate dependent calculation produces a significantly lower permeability than the rate independent case.

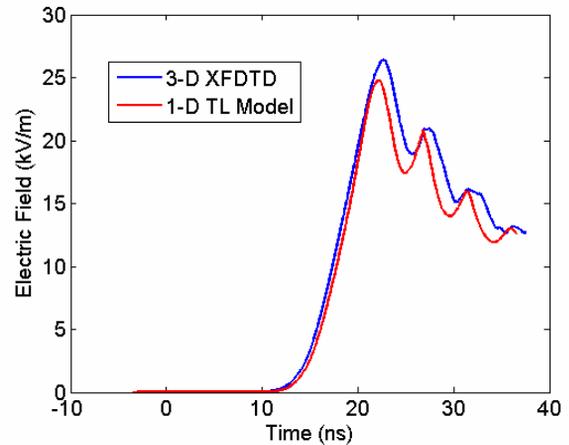


Figure 7: Electric field 1.1 cm after ferrite insert.

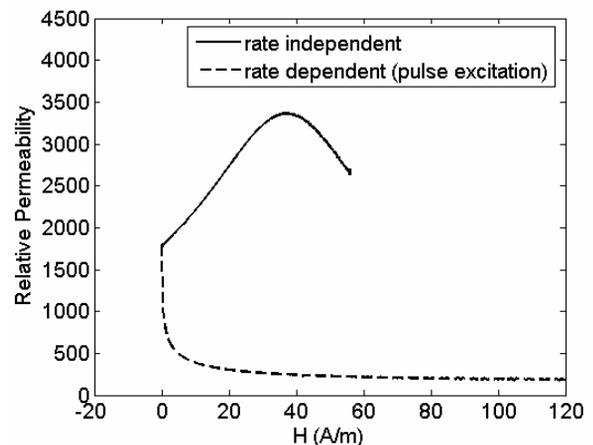


Figure 8: CN20 permeability from XFDTD code.

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