# AN INNOVATIVE METHOD TO OBSERVE RFQ VANES MOTION WITH FULL-SCALE RF POWER AND WATER COOLING

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## Abstract

The design of high current RFQ's is heavily strained by thermo-mechanical considerations, which eventually have an impact on machining costs, cooling systems, etc. A 1meter long copper prototype of the SPIRAL2 RFQ has been specifically built to corroborate design options. An innovative method has been developed, allowing realtime observation of mechanical deformations of RFQ vanes, with full-scale RF power and water cooling. Digital images are acquired by a CCD camera, and processed by a dedicated software. Processing includes contrast stretching, low-pass filtering, and blockcorrelation followed by interpolation. Sub-pixel relative motions of RFQ electrode ends are clearly detected and measured, with RMS errors in the range 0.6 to 1.8 micron.

# **INTRODUCTION**

The SPIRAL2 RFQ prototype (length 1 m, inner diameter 702.4 mm) has been designed to operate at 88 MHz with 40 kW full-power. RFQ copper tube and electrodes are cooled by independent water circuits, and thermo-mechanical simulations have shown that a proper selection of circuit temperatures are required to leave the geometry of axial region (vane tips) unchanged when full RF power is applied, thus saving RFQ room-temperature tuning. One main objective of prototype experiments was to measure the deformations of axial region vs. temperatures and RF power [1]. Variations of a few microns to a few tens of microns were expected.

## **PROPOSED METHOD**

The proposed non-intrusive method consists in acquiring images of the RFQ vanes ends with a CCD camera, and using digital processing to detect motion between each "current" frame and some "reference" frame. Since only deformations are sought, no attempt has been made to relate camera axes to RFQ axes: the four vane ends just need to be present in each camera frame. Flat vane ends are lit and observed under nearly normal incidence. Rounded edges make precise detection of edge position almost impossible. Using surface texture to detect motion is also difficult, because polished copper is highly reflective. However some artificial etching (here a hand-made grid pattern) can satisfactorily enhance contrast.

Three main categories of algorithms may be used for motion detection. In group I, intensity f vs. position M and motion  $\Delta$  are approximated up to 2<sup>nd</sup> order

$$f(M + \Delta) = f(M) + J^{T}\Delta + \frac{1}{2}\Delta^{T}H\Delta$$
,

the Jacobian J and Hessian H being estimated from pixel intensities by finite differences. Hessian is used to select plane and tilted intensity facets, and Jacobian to detect X and Y motions of facets. These methods detect largely sub-pixel motions, but require complicated iterative algorithms [2] in case of multi-pixel motion. In group II, digital normalized cross-correlation of "reference" and "current" image is calculated, followed by an interpolator to estimate precise peak position These methods are sensitive and robust; frame partitioning helps eliminate false correlation peaks and derive to accuracy [3]. Algorithms based on phase tilt of 2D Fourier transforms [4] are to be placed in the same group (position - spatial frequency duality). In group III, edge detection algorithms are used to extract texture features [5], and pattern recognition yields X and Y motions, rotation and magnification.

A method of group I has been successfully programmed, tested, and finally abandoned, because experiments showed multi-pixel motions. Group III has been explored, but pattern recognition turned out to be quite complicated because many surface defects survive to edge detection. Finally, the correlator + interpolator method was selected.

## **EXPERIMENTAL SETUP**

Electrode ends are observed by reflection in a mirror (Figure 1), thus leaving the camera in a region less exposed to intense axial X-rays. Direct lighting of electrodes does not work, because many caustics build-up in the vacuum window assembly, resulting in over-contrasted images. Rather, a white paper sheet glued to the mirror is used as a diffusive reflector for the optical fibre lighting system, and a small cardboard diaphragm placed against the vacuum window. The camera is a LightWise LW-1.3-S-1394, with a 2048  $\times$  1536 CCD detector, and FireWire link for acquisition. Lead protection is added everywhere it can be.



Figure 1: Experimental setup.

## **DIGITAL PROCESSING**

# Data Flow

Raw RGB images from the camera (without any color or contrast correction that might induce errors in subsequent processing) are first cropped into four  $220 \times 220$  sub-frames, one per electrode (Figure 2). Each subframe is converted into luminance image, using

$$Y = 0.30 R + 0.59 G + 0.11 B.$$

Luminance histogram is computed (64 bins), and contrast is linearly stretched over full range, i.e. lowest intensity maps to 0 and highest intensity maps to 1 (Figure 3). Then a low-pass filter (3  $\times$  3 Gaussian mask,  $\sigma_x = \sigma_y =$ 0.6 pix) is used to smooth out defective pixels. All these operations must be *rigorously* identically performed on all images in a motion detection sequence to prevent any fake motion detection. Sub-frames of "reference" and "current" images are then presented to cross-correlatorsinterpolators for X and Y motion detection. Data is displayed after compensation of general X and Y drifts, thus only saving relative motions of electrodes. Interelectrode distance variations are finally computed, and expressed into RFQ coordinates, a set of linear combinations directly related to RFQ frequency and voltage perturbations.



Figure 2: Left: camera frame, with pixel  $\{1,1\}$  at upperleft and pixel  $\{1536,2048\}$  at bottom-right. Right:  $220 \times 220$  sub-frame.



Figure 3: Contrast enhancement.

#### Image Scaling

Pixel size is derived from grid pattern known metric size (4 × 4 mm) and observed size in pixel units (averaged over the four electrode sub-frames). With given optics and geometry, pattern size is about  $140 \times 140$ , and pixel size is ~ 28.6 µm.

#### Normalized Cross-Correlation

Let A(p,q) and B(p,q) two intensity images in the range [0,1]. Normalized cross-correlation is defined as

$$\chi(i, j) := \sum_{p=1}^{P} \sum_{q=1}^{Q} A'(p+i, q+j).B'(p,q)$$

where A' and B' are normalized zero-mean images

$$\begin{split} \langle \mathbf{A} \rangle &= \frac{1}{PQ} \sum_{p=1}^{P} \sum_{q=1}^{Q} \mathbf{A}(p+i,q+j), \quad \mathbf{A}' = \frac{\mathbf{A} - \langle \mathbf{A} \rangle}{\|\mathbf{A} - \langle \mathbf{A} \rangle\|_{2}} ,\\ \langle \mathbf{B} \rangle &= \frac{1}{PQ} \sum_{p=1}^{P} \sum_{q=1}^{Q} \mathbf{B}(p,q), \quad \mathbf{B}' = \frac{\mathbf{B} - \langle \mathbf{B} \rangle}{\|\mathbf{B} - \langle \mathbf{B} \rangle\|_{2}} \,. \end{split}$$

Let A be the "current" image, and B the "reference". X and Y motions are given by the peak position.  $\chi$  is usually computed over a small mask, to save computation time (here 11 × 11 typ.). For non-integer motion,  $\chi$  is approximated by a second degree polynomial, whose coefficients are derived by least-square fit over the correlator output. Eigen-values  $\lambda_{1,2}$  of the Hessian of  $\chi$  are used to estimate full-width half maximums (FWHM) of correlation peak  $w_{1,2} = [2/|\lambda_{1,2}|]^{1/2}$ , and eigen-vectors give their orientation in image plane.

#### Partitioned Images

Electrode sub-frames are first partitioned in  $5 \times 5$  blocks, and cross-correlation is performed for the 25 pairs of "reference" and "current" blocks. Motion estimate is taken to be the mean of all valid correlator-interpolator outputs (i.e. satisfying  $\lambda_1 < 0$  and  $\lambda_2 < 0$ ). Note that with proper electrode lighting, correlation peak is always > 0.90, and all blocks are valid.

Typical standard deviation over 25 blocks is  $\sigma_{X,Y} = 0.1$  to 0.3 pix. Standard deviation of the estimate of the mean is then  $\sigma_{X,Y}/\text{sqrt}(25) = 0.02$  to 0.06 pix, i.e. 0.6 to 1.8 µm.



Figure 4: Example of warp functions, showing consistent motion over partition blocks.

## Drift Compensation and RFQ Coordinates

Detected motions  $\{u_n, v_n\}$  are added to coordinates of grating centers in "reference" frame for initial display (Figure 5, left). Erratic aspect comes from uncontrolled movements of optics table relative to RFQ, likely due to poor floor stability, vibrations, and temperature differences. Things look better (Figure 5, right) after subtracting X and Y drifts (mean of motion over 4 electrodes).



Figure 5: Motion of grating centers in frame coordinates before (left) and after (right) drift compensation. X and Y in meter units. "Reference" frame data at true coordinates; subsequent "current" frame motion amplified 200×.



Figure 6: Motion displayed in RFQ coordinates (meter units), vs. frame index (one frame every 5 minutes). Same color code as in Figure 5.

Data in Figure 5 is presented using 8 parameters per frame; however, relative positions of 4 points in a plane are fully described by only 5. Proposed data reduction uses knowledge of RFQ electrical behavior. Let

$$u_{12} = +U_Q + U_S, u_{23} = -U_Q + U_T, u_{34} = +U_Q - U_S, u_{41} = -U_Q - U_T,$$

where  $u_{mn}$  is voltage difference from electrode #m to electrode #n,  $U_Q$  is the quadrupole accelerating voltage, and  $U_S$ ,  $U_T$  the (unwanted) dipole components (note that the quasi-static behavior of RFQ axial region implies  $u_{12}+u_{23}+u_{34}+u_{41}=0$ ). At first order,

 $\begin{array}{l} \Delta U_Q \sim (\Delta C_{12} + \Delta C_{23} + \Delta C_{34} + \Delta C_{41})/4 \\ \Delta U_S \sim (\Delta C_{12} - \Delta C_{34})/2, \quad \Delta U_S \sim (\Delta C_{41} - \Delta C_{23})/2 \end{array}$ 

where  $\Delta C_{mn}$  is the capacitance variation between electrodes #m and #n. Since capacitances are roughly inversely proportional to electrode separation, we define the following *RFQ coordinates:* 

$$\begin{array}{ll} d_{QQ} := (d_{12} + d_{23} + d_{34} + d_{41})/4, & d_{SSTT} := (d_{12} - d_{23} + d_{34} - d_{41})/4, \\ d_{SQ} := (d_{12} - d_{34})/2, & d_{SS} & := (d_{24} + d_{13})/2, \\ d_{TQ} := (d_{41} - d_{23})/2, & d_{ST} & := (-d_{24} + d_{13})/2, \end{array}$$

any 5 of them fully describing the electrode relative positions (Figure 6). Variations of  $d_{QQ}$ ,  $d_{SQ}$  and  $d_{TQ}$  directly relate to RFQ voltage perturbations.

## METRICS

Side of etched patterns is measured using manual graphics tools; uncertainty is estimated to be  $\pm 2$  pix; hence <u>Pixel Size Error</u> is lower than  $2/140 = 1.4 \ 10^{-2}$ . Pole distance variations are obtained by projecting X and Y motions on the line joining pattern centers. Pole-center to pattern-center is never greater than 50 pix, and center-to-center distance is about 750 pix. Hence pole-to-pole axis angular error is  $\vartheta \leq \tan 50/750 = 3.8 \ \text{deg}$ , and <u>Pole-to-Pole Distance Projection Error</u> is smaller than  $1-\cos\vartheta = 2.2 \ 10^{-3}$ . Optical axis has been aligned using vacuum port located on other end of RFQ, hence tilt angle is bounded by  $\alpha \leq \tan 0.02/1.00 = 1.14 \ \text{deg}$ , and <u>Ellipticity Ratio</u> in camera focal plane is smaller than  $1-\cos\alpha = 2 \ 10^{-4}$ . Clearly, overall metrics error could be reduced with high precision pattern etching.

## LIGHTS IN THE NIGHT

CCD camera has also captured many bright lightemitting spots, generally showing-up at 20 kW and above (Figure 7). Most of these are located at 45° angle on electrode tips, where electric field is a maximum. They remained quite stable throughout experiments in 2005 and 2006 [1], and are likely related to local surface defects.



Figure 7: Light emissions on upper (at left) and lower (at right) vanes, as observed from RFQ output. These are color-enhanced images, with R, G and B contrasts linearly stretched as explained in Figure 3. Light emission looks white because it saturates the CCD.

#### REFERENCES

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