

CHARGE-CHANGING COLLISIONS

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Abstract

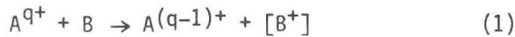
Recent results for charge-changing collisions of interest for cyclotrons and other particle accelerators are presented. Scaling rules, where available, are emphasized.

Introduction

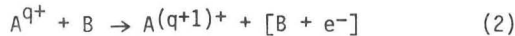
Information on atomic charge-changing collisions is important for the design and operation of cyclotrons and other particle accelerators.^{1,2} Collisions can occur in an external ion source, during beam transport and injection, and during acceleration. Particles which change their charge are lost, thereby attenuating the output beam. Particles which are lost to the beam may strike the cyclotron and cause radioactivation³ with attendant health hazards. As heavier ions are accelerated in cyclotrons, the vacuum requirements become more stringent, and additional charge-changing information is required.

The purpose of this paper is to review recent results of charge-changing processes relevant to cyclotrons and other particle accelerators. The energy range included is from eV/u to hundreds of MeV/u, projectiles from the entire periodic table (Li to U), and the total range of charge states for which information is available. Various targets are considered, especially H, H₂, and He; although these are not predominant in the entire periodic table in a cyclotron, they have been more thoroughly studied than CO, CO₂, H₂O, O₂, N₂, and hydrocarbons likely to be found in the residual gas in a cyclotron. I shall be especially concerned with scaling rules applicable for a wide variety of projectile-target systems, as data for a particular collision system of interest are normally not available.

Two processes dominate charge-changing collisions in accelerators: single-electron capture (electron pickup)



and single-electron loss (stripping)



where A and B are projectile ion and target atom, and q⁺ is the charge state of the ion before the collision. The brackets indicate that the target charge state is undetermined. Cross sections for two-electron transfer are generally an order of magnitude smaller than for one-electron transfer; two-electron-loss cross sections can be appreciable for very fast projectiles in low charge states.

Electron Capture at Low Energies

Low energy is used here to mean that the projectile velocity v is much less than the orbital

velocity of the electron being captured - usually from the outer shell of the target. For the hydrogen-atom ground state the velocity of the electron is v₀ = 2.2 x 10⁸cm/s or about 25 keV/u. Electron-capture cross sections for low-energy multiply charged ions have been extensively studied, especially by Salzborn's group⁴ in Giessen. Cross sections are generally independent of velocity, and directly proportional to the charge of the projectile. An approximate scaling rule⁴ can be used for this velocity range:

$$\sigma_{q,q-1} = 1.43 * 10^{-12} * q^{1.17} * I^{-2.76} \text{ cm}^2$$
 (3)

where $\sigma_{q,q-1}$ is the electron-capture cross section in cm², q is the projectile charge state, and I is the first ionization potential of the target in eV. The same experimenters⁴ subsequently extended the range of target I, finding an I⁻² behavior for smaller values of I. Typical results⁵ are shown in Figs. 1 and 2.

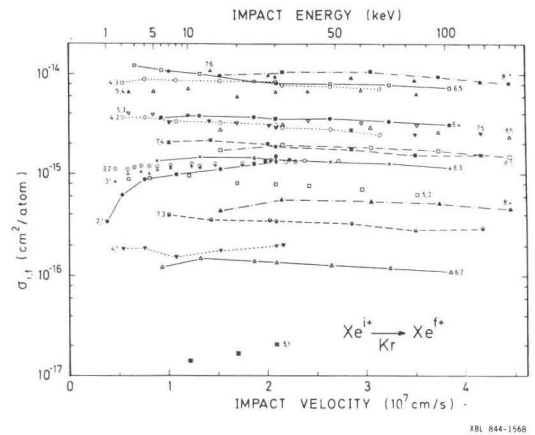


Fig. 1 Electron-capture cross sections for low-energy Xe ions in a Kr target, from measurements by Salzborn and Müller.^{4,5}

Measurements have been carried to lower energies by use of special sources of ions: a laser-produced plasma,⁶ and recoil ions produced by a fast ion beam and stored in an ion trap.⁷ Phaneuf⁶ has measured electron capture for Fe^{q+} ions (q < 3 < 14) in H and H₂ at energies in the range 10-95 eV/u. For Fe⁵⁺ and Fe⁶⁺, for which higher-energy data exist, the cross section for electron capture is essentially independent of velocity over the energy range 17-2000 eV/u. Vane, Marrus, and Prior⁷ at LBL have measured electron-capture cross sections for highly stripped Ne ions stored in an electrostatic trap. They found that the electron-capture cross section for 7-45 eV Ne¹⁰⁺ in Ne is velocity independent; however, other collision partners, e.g., Ne⁷⁺ in Ne and Xe, showed a cross section decreasing with increasing velocity in the energy range 1-70 eV.

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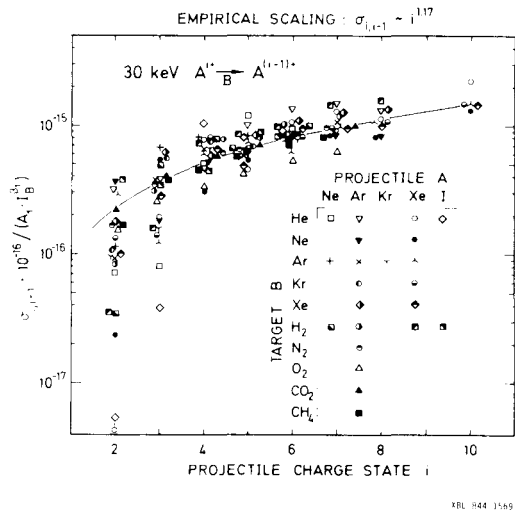


Fig. 2 Scaled one-electron-capture cross sections for various 30-keV projectile-target combinations (Eq. 3), by Salzborn and Müller.^{4,5}

Electron Capture at High Energies

Electron capture for fast projectiles ($v > v_0$) has been extensively studied. Recent measurements with cyclotrons and linacs have extended the range of projectiles studied to high energies and charge states.⁸ Most measurements are at energies lower than 10 MeV/u; a notable exception is a recent measurement at 962 MeV/u using the LBL Bevalac.⁹

An apparatus used by the LBL group⁸ for measuring charge-transfer cross sections (electron capture and loss) is shown in Fig. 3. A beam of ions from the LBL SuperHILAC is incident on a thin carbon foil. Ions in a single charge state are selected by a magnet located downbeam from the foil, and, after suitable collimation, pass through a differentially pumped gas target in which the pressure is measured with a capacitance manometer. Ions in the initial charge state as well as those which capture or lose one or two electrons are analyzed in a second magnet and are detected with solid-state detectors. Cross sections are determined from the rate of growth of the signals for ions which change charge in the gas cell. Cross sections are readily determined to an approximate accuracy⁸ of ± 20 percent. Sample cross sections^{8,10} are shown in Figs. 4 and 5.

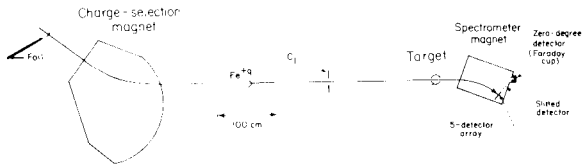


Fig. 3 Schematic diagram of apparatus used by the LBL group to measure charge-transfer cross sections.⁸ A beam of ions from the SuperHILAC was incident from the left.

A considerable number of cross sections for electron capture have been measured for multiply charged ions incident on H and H₂ at intermediate energies, i.e., typically at velocities up to 3

v_0 . For example, the Oak Ridge group¹¹ has made measurements for a variety of ions, including Fe^{q+} ($4 \leq q \leq 15$). The Belfast group has also reported¹² many measurements in H and H₂ targets, e.g., B and C ions. Olson and co-workers¹³ have had considerable success in calculating electron-capture cross sections at intermediate velocities using the classical trajectory Monte Carlo method.

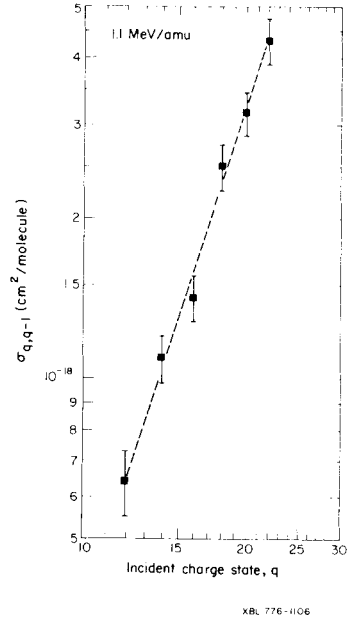


Fig. 4 Electron-capture cross sections for 1.1 MeV/u Fe^{q+} ($q = 12-22$) ions in an H₂ target, measured by the LBL group.⁸ The line is $\sigma = 2.6 \times 10^{-22} q^{3.15}$.

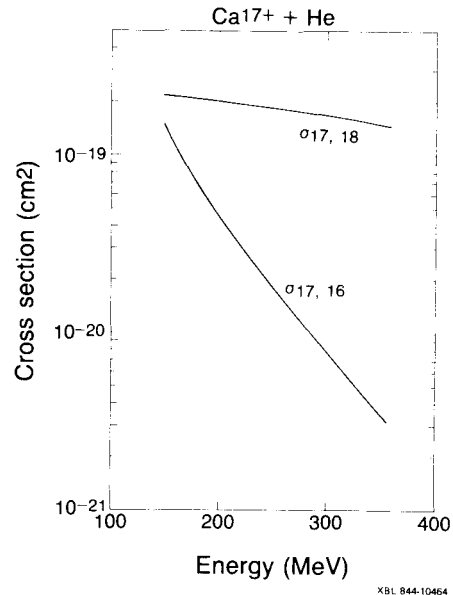


Fig. 5 Electron-capture and -loss cross sections for Ca¹⁷⁺ ions in a He target, measured by the LBL group.¹⁰

Cross sections for electron capture by a fast projectile are rarely available for the desired projectile specie and charge state in the desired target over a large energy range. There has therefore been considerable interest in scaling of electron-capture cross sections with these parameters. Berkner et al. found a scaling rule⁶ for electron capture by fast highly charged iron ions in an H₂ target. The electron-capture cross section σ was described by

$$\sigma = 1.2 \times 10^{-8} q^{3.15} E^{-4.48} \text{ cm}^2 \quad (4)$$

for projectile energies greater than 275 keV/u, where E is the energy of the iron projectile in keV/u and q is the projectile charge state. Alonso and Gould¹⁴ found, for fast lead and xenon ions in N₂, a q dependence of approximately 2.9-3.3; in addition, these authors found a velocity dependence of about $v^{-5.8}$ or $E^{-2.9}$, based on data over a limited range of velocities. Knudsen et al.¹⁵ found that electron-capture cross sections scale in reduced coordinates σ/q and $E/q^{4/7}$ in a given target; based on the Lenz-Jensen atomic model, cross sections could be described in reduced coordinates $\sigma Z^{2/3}/q$ and $E/(q^{4/7} Z^{16/21})$, where Z is the target atomic number. Ryufuku¹⁶ has found that cross sections in atomic hydrogen could be scaled in the reduced coordinates $\sigma/q^{1.07}$ and $E/q^{0.35}$, while Janev et al.¹⁷ found $E/q^{0.5}$ to be a suitable scaling parameter for electron capture from inner shells of Ar atom targets.

Schlachter et al.¹⁸ took a generalized approach to scaling electron-capture cross sections for a large variety of projectiles and targets. A non-linear least-squares fitting routine was used to adjust a multi-parameter formula to selected electron-capture cross-section data.^{8,19-21} The best values for the reduced parameters were found to be

$$\begin{aligned} \tilde{\sigma} &= \sigma Z^{1.8} / q^{0.5} \\ \tilde{E} &= E / (Z^{1.25} q^{0.7}) \end{aligned} \quad (5)$$

where σ is the electron-capture cross section in cm², q is the projectile charge state, E is the projectile energy in keV/u, and Z is the atomic number of the target. The best fit to the data in reduced coordinates is

$$\begin{aligned} \tilde{\sigma} &= \frac{1.1 \times 10^{-8}}{\tilde{E}^{4.8}} \left[1 - \exp(-0.037 \tilde{E}^{2.2}) \right] \\ &\quad * \left[1 - \exp(-2.44 \times 10^{-5} \tilde{E}^{2.6}) \right]. \end{aligned} \quad (6)$$

Cross-section data in reduced coordinates for a wide variety of targets are shown in Figs. 6 and 7; the curve is the representation of Eq. 6. Approximately 70 percent of all data tested lie within a factor of 2 of the curve, subject to several restrictions:

$$10 < \tilde{E} \quad (7a)$$

where \tilde{E} is defined in Eq. 5, with energy E in keV/u;

$$q \geq 3 \quad (7b)$$

$$\text{and} \quad \tilde{E} < 1000. \quad (7c)$$

It is possible that the curve will continue to bend with increasing steepness for higher values of \tilde{E} .

At high reduced energies, Eq. 6 asymptotically approaches

$$\sigma = 1.1 \times 10^{-8} q^{3.9} Z^{4.2} / E^{4.8} \quad (8)$$

in normal coordinates. The target atomic-number dependence allows prediction of electron-capture cross sections for many targets.

Crothers and Todd²² have shown that semiclassical theory accounts for q^3 scaling in electron capture in atomic hydrogen at intermediate energies, and that semiclassical OBK, eikonal, continuum intermediate-state and continuum distorted-wave theories all lead to q^3 scaling. In the limit of high velocities, OBK and more modern theories²³ predict a q^5 dependence. The asymptotic charge-state dependence observed in the present result is $q^{3.9}$.

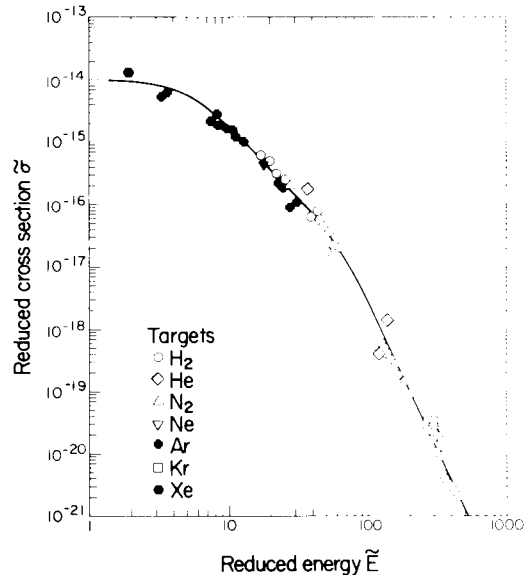


Fig. 6 Reduced plot of electron-capture cross sections¹⁸ for fast highly charged ions in gas targets, in scaled coordinates (Eq. 5). The line is Eq. 6.

Eichler and Narumi²⁴ have compared the Born approximation with the classical-trajectory eikonal approximation: the second Born approximation gives rise to a v^{-11} term ($E^{-5.5}$), which will dominate the first Born term, which varies as v^{-12} (E^{-6}), while the classical-trajectory eikonal approximation only predicts the v^{-12} (E^{-6}) velocity dependence. The scaling rule shows a $v^{-9.6}$ dependence on velocity for large velocities, rather than the theoretically expected v^{-11} or v^{-12} . It seems likely that, were data to exist for much higher reduced energies, the asymptotic behavior observed (Eq. 8) would have to be modified. The q dependence may approach q^5 and the velocity dependence v^{-12} .

Application of the scaling rule to molecular targets is not clear. Data for H₂ and N₂ were fit successfully by dividing the molecular cross section by 2 and then using the atomic number Z. This procedure is approximate at best, and is probably not applicable to molecules such as CO₂ or hydrocarbons. The projectile charge state and velocity or energy scaling, however, will nonetheless probably scale successfully.

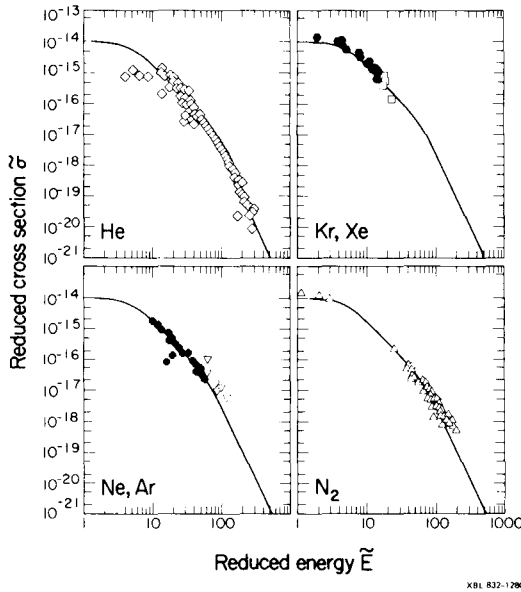


Fig. 7 Reduced plot of electron-capture cross sections¹⁸ for fast highly charged ions in gas targets, in scaled coordinates (Eq. 5). The line is Eq. 6.

Electron Loss

There are considerably less data for electron loss than for electron capture. This renders more difficult the task of calculating the attenuation of a beam, especially for high velocities or low charge states, where electron loss generally exceeds electron capture. Furthermore, electron loss is sensitive to the binding energy of the electron to be removed, hence to the shell structure of the ion.

The electron-loss cross sections for a given ion has only a weak energy dependence. Measurements show a broad maximum with energy, peaked at a velocity of 1 to 2 times the velocity of the electron being removed,^{20,21,25-27} as predicted by Bohr and Lindhard. The cross section is predicted by the Born approximation to decrease as $1/v^2$ for very high velocity,²⁸ although a slower decrease is often observed,¹³ perhaps because the velocity is not sufficiently high. The energy at which the maximum in the cross section occurs increases with increasing charge state of the ion. Sample data are shown in Figs. 5 and 8.^{10,21}

A very strong charge-state dependence is observed in electron loss. For a charge-state dependence

$$\sigma_{q,q+1} = \sigma_0 q^{-\alpha} \quad (9)$$

the LBL group⁸ has observed values of α as large as 9-12 for $q > 10$ for fast Fe, Nb, and Pb ions; values of 2-4 are observed for different projectile-target systems. Sample data are shown in Fig. 9.⁸

Alonso and Gould⁸ have found a semiclassical model, based on Bohr's formula. Agreement with experiment is roughly within a factor of 2. Alton and colleagues²⁵ discuss a different modified Bohr formula, which agrees quite well with experiment.

$$\sigma_{q,q+1} (\text{cm}^2) = N_j \left(\frac{13.6}{I_j} \right) \left(\frac{v_0}{v} \right)^2 * \left(Z_1^{1/3} + Z_2^{1/3} \right)^2 \pi a_0^2 \quad (10)$$

where N_j is the number of electrons in a given subshell.

Discontinuities are observed in electron loss when a new shell is reached,⁸ as in Fig. 10, which shows data for highly stripped iron ions in H_2 ; the abrupt decrease in cross section is due to the greatly increased binding energy of the K-shell electron to be removed, relative to the ease of removal of electrons from the L-shell.

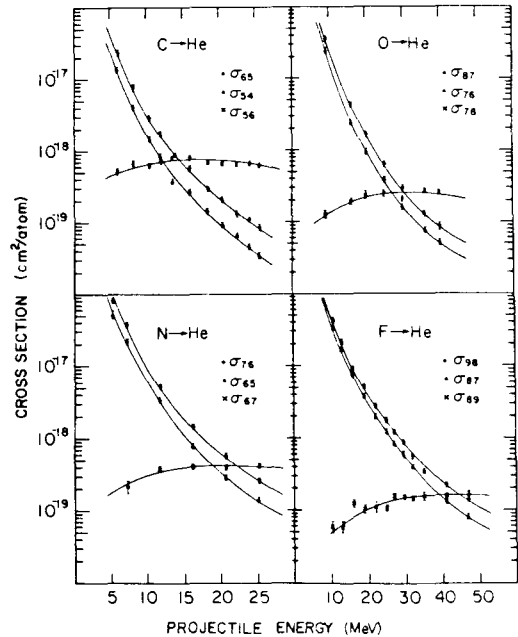


Fig. 8 Electron-capture and -loss cross sections for C, N, O, and F ions in a He target, measured by Dillingham et al.²¹

Theoretical calculations which can be compared with experimental results for fast highly stripped projectiles are generally restricted to hydrogen-like ions.²⁹⁻³¹ Calculations based on the Born approximation for atomic-hydrogen targets are generally in agreement with experimental cross sections for high velocities.³² Born calculations for non-hydrogen-like ions generally underestimate experimental results by more than an order of magnitude.

The Bohr theory³³ often overestimates single-electron-loss cross sections. It does, however, provide a good first-order estimate.^{25,32} Cross sections for electron loss generally increase with increasing atomic number Z of the target. Knudsen et al.³² have shown that, for heavy gas targets at low energies and charge states, the Bohr theory gives quite good target-gas dependence. For targets heavier than nitrogen, measurements for 4.66 MeV/amu Pb^{54+} show a $Z^{0.47 \pm 0.02}$ dependence.⁸ The Bohr theory³³ predicts a $Z^{0.67}$ dependence at higher energies. Other discussions of Born calculations²⁸ and comparison with experiment have been presented.^{8,14,21,26,29} Target gas dependence is shown in Fig. 11.³⁵

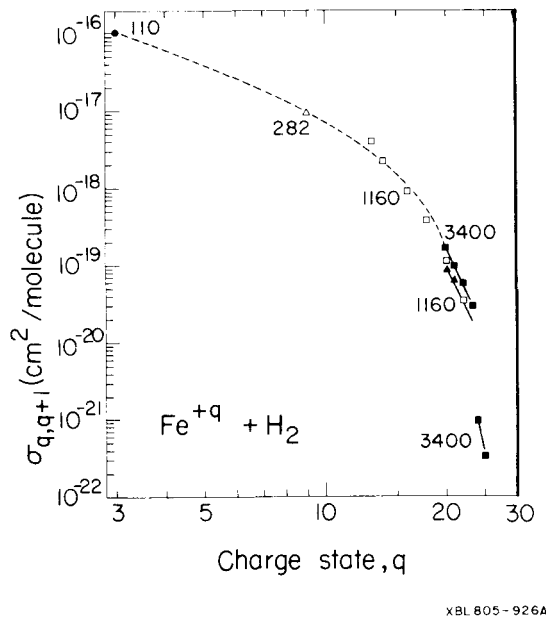


Fig. 9 Electron-loss cross sections for Fe^{q+} ions in an H_2 target, measured by the LBL group.⁸ The numbers on the figure are energy in keV/u.

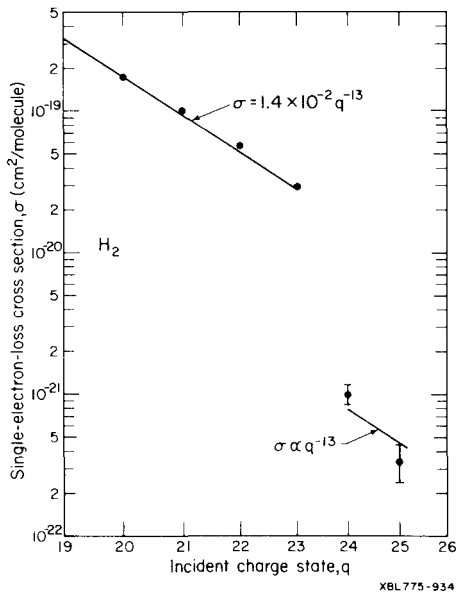


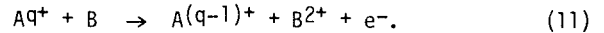
Fig. 10 Electron-loss cross sections for 3.4 MeV/u Fe^{q+} ions in H_2 , from measurements by the LBL group,⁸ illustrating the effect of shell structure in electron loss.

Knudsen et al.³⁴ have shown, for 20 MeV Fe^{4+} in gases, that multiple electron loss can be an important process for a fast, low-charge-state, heavy projectile.

Transfer Ionization

An interesting collision process which has

received considerable attention recently is transfer ionization: a collision in which more electrons are lost by the target than are captured by the projectile. In its simplest form, it can be represented by:



The effect is that two-electron transfer to an auto-ionizing state appears as single-electron capture, rendering comparison of theory and experiment difficult.

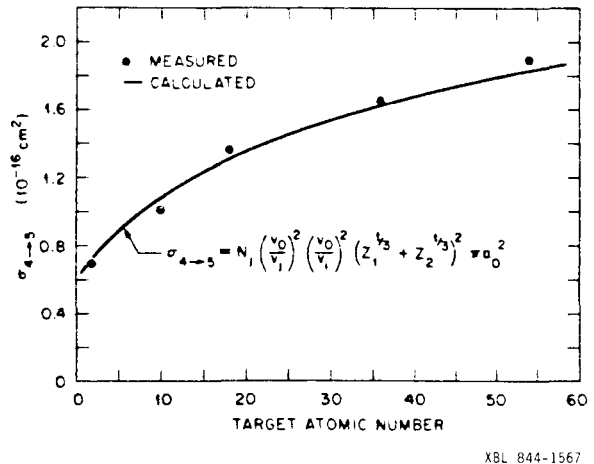


Fig. 11 Electron-loss cross sections for 20-MeV Fe^{4+} in various target gases, from measurements by Alton et al.²⁵ The line is Eq. 10.

Transfer ionization can be very important in slow ($v < v_0$) collisions of multiply charged ions in multi-electron targets.^{35,36} These collisions have been studied by coincidence techniques, in which the target recoil ion is detected in coincidence with the charge-transferred projectile. The charge state of the recoil ion is generally determined by its time-of-flight. A slow Kr^{10+} ion can produce Xe recoil ions four- and five-times ionized. These collisions generally depend upon the internal potential energy of the collision system rather than on the projectile kinetic energy. Capture by the projectile of two or more electrons can produce even higher-charge-state recoil ions, because more potential energy is available for the release of additional target electrons.

Transfer ionization is also important in fast collisions,^{37,38} in which projectile kinetic energy does play a role. For high-charge-state projectiles, transfer ionization can be of the same magnitude as single-electron capture, and much larger than double-electron capture. Thus single-electron capture accompanied by ejection of a second electron from the target is an important collision process.³⁸

Additional Data

Results for charge-changing collisions have been summarized in several references. The review of Betz¹⁹ is useful, although it is no longer up to date. Considerable current information can be found in publications^{39,40} by the Institute of Plasma Physics, Nagoya University. Electron capture by multiply charged ions has been discussed in a

symposium at the Kyoto ICPEAC meeting in 1979,⁴¹ and in a symposium on collisions of multicharged ions with atoms at the 1981 Gatlinburg ICPEAC meeting.⁴² Janev and Presnyakov have published an extensive report⁴³ entitled "Collision processes of multiply charged ions with atoms." Additional information can be found in the proceedings of the 1982 Stockholm conference on production and physics of highly charged ions,⁴⁴ or in deHeer's review⁴⁵ on electron capture and ionization.

Acknowledgements

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References

1. R. A. Gough and M. L. Mallory, "Charge-exchange losses during cyclotron acceleration: experiment and theory," IEEE Trans. Nucl. Sci. NS-26, 2384 (1979); M. L. Mallory, "A method for calculating the vacuum requirements of heavy-ion cyclotrons," MSU Cyclotron Laboratory Annual Report (East Lansing, 1979), p. 132.
2. D. Elo, D. Morris, D. J. Clark, and R. A. Gough, "Cryogenic vacuum pumping at the LBL 88-inch cyclotron," IEEE Trans. Nucl. Sci. NS-26, 2179 (1979).
3. M. L. Mallory, T. Antaya, F. Marti, and P. Miller, "Radioactivation of a heavy ion cyclotron central region," MSUCL-425, June 1983.
4. H. Klinger, A. Müller, and E. Salzborn, "Electron capture cross sections for multiply charged argon ions passing through nitrogen and krypton targets at energies from 10 to 110 keV," J. Chem. Phys. 65, 3427 (1976); "Electron-capture processes of multiply charged argon ions in argon at energies from 10 to 90 keV," J. Phys. B 8, 230 (1975); A. Müller and E. Salzborn, "Scaling of cross sections for multiple electron transfer to highly charged ions colliding with atoms and molecules," Phys. Lett. 62A, 391 (1977); A. Müller, C. Achenbach, and E. Salzborn, "Dependence of the charge transfer between atoms and highly charged ions on the ionization potential of the atoms," Phys. Lett. 70A, 410 (1977).
5. E. Salzborn and A. Müller, "Electron capture by multi-charged ions colliding with multi-electron targets," in Ref. 43, pp. 407-426 (1980).
6. R. A. Phaneuf, "Electron capture by slow Fe^{q+} ions from hydrogen atoms and molecules," Phys. Rev. A 28, 1310 (1983); "Electron capture in very slow C^{q+} + H collisions," Phys. Rev. A 24, 1138 (1981); R. A. Phaneuf, I. Alvarez, F. W. Meyer, and D. H. Crandall, "Electron capture in low-energy collisions of C^{q+} and O^{q+} with H and H₂," Phys. Rev. A 26, 1892 (1982).
7. C. R. Vane, M. H. Prior, and R. Marrus, "Electron capture by Ne¹⁰⁺ trapped at very low energies," Phys. Rev. Lett. 46, 107 (1981); M. H. Prior, R. Marrus, and C. R. Vane, "Electron capture by trapped Ne^{q+} ions at very low energies," Phys. Rev. A 28, 141 (1983).
8. K. H. Berkner, W. G. Graham, R. V. Pyle, A. S. Schlachter, and J. W. Stearns, "Single-electron capture and loss cross sections for highly stripped Fe ions in hydrogen at 3.4 MeV/nucleon," Phys. Lett. 62A, 407 (1977); K. H. Berkner, W. G. Graham, R. V. Pyle, A. S. Schlachter, J. W. Stearns, and R. E. Olson, "Electron-capture and impact-ionization cross sections for partially stripped iron ions colliding with atomic and molecular hydrogen," J. Phys. B 11, 875 (1978); K. H. Berkner, W. G. Graham, R. V. Pyle, A. S. Schlachter, and J. W. Stearns, "Electron-capture, electron-loss, and impact-ionization cross sections for 103- to 3400-keV/amu multicharged iron ions colliding with molecular hydrogen," Phys. Rev. A 23, 2891 (1981); W. G. Graham, K. H. Berkner, R. V. Pyle, A. S. Schlachter, J. W. Stearns, and J. A. Tanis, "Charge-transfer cross sections for multiply charged ions colliding with gaseous targets at energies from 310 keV/amu to 8.5 MeV/amu," submitted to Phys. Rev. A.
9. H. Gould, D. Greiner, P. Lindstrom, T. J. M. Symons, and H. Crawford, "Electron capture by U⁹¹⁺ and U⁹²⁺ and ionization of U⁹⁰⁺ and U⁹¹⁺," Phys. Rev. Lett. 52, 180 (1984).
10. J. A. Tanis, E. M. Bernstein, M. Clark, R. H. McFarland, T. J. Morgan, A. S. Schlachter, and J. W. Stearns (unpublished).
11. F. W. Meyer, R. A. Phaneuf, H. J. Kim, P. Hvelplund, and P. H. Stelson, "Single-electron-capture cross sections for multiply charged O, Fe, Mo, Ta, W, and Au ions incident on H and H₂ at intermediate velocities," Phys. Rev. A 19, 515 (1979); H. J. Kim, R. A. Phaneuf, F. W. Meyer and P. H. Stelson, "Single electron capture by multiply charged²⁸ Si ions in atomic and molecular hydrogen," Phys. Rev. A 17, 854 (1978); R. A. Phaneuf, F. W. Meyer, and R. H. McKnight, "Single-electron capture by multiply charged ions of carbon, nitrogen, and oxygen in atomic and molecular hydrogen," Phys. Rev. A 17, 534 (1978).
12. T. V. Goffe, M. B. Shah, and H. B. Gilbody, "One-electron capture and loss by fast multiply charged boron and carbon ions in H and H₂," J. Phys. B 12, 3763 (1979).
13. R. E. Olson and A. Salop, "Electron transfer between multicharged ions and neutral species," Phys. Rev. A 14, 579 (1976); E. J. Shipsey, J. C. Browne, and R. E. Olson, "Electron capture and ionization in C⁵⁺, N⁵⁺, O⁶⁺ + H collisions," J. Phys. B 14, 869 (1981).
14. J. Alonso and H. Gould, "Charge-changing cross sections for Pb and Xe ions at velocities up to 4 x 10⁹ cm/sec," Phys. Rev. A 26, 1134 (1982).
15. H. Knudsen, H. K. Haugen, and P. Hvelplund, "Single-electron-capture cross section for medium- and high-velocity, highly charged ions colliding with atoms," Phys. Rev. A 23, 597 (1981).
16. H. Ryufuku, "Ionization, excitation, and charge transfer for impacts of H⁺, Li³⁺, B⁵⁺, C⁶⁺, and Si¹⁴⁺ ions on atomic hydrogen," Phys. Rev. A 25, 720 (1982).
17. R. K. Janev, L. P. Presnyakov, and V. P. Shevelko, "One-electron capture from the inner shells in atom-multicharged ion collisions," Phys. Lett. 76A, 121 (1980).
18. A. S. Schlachter, J. W. Stearns, W. G. Graham, K. H. Berkner, R. V. Pyle, and J. A. Tanis, "Electron capture for fast highly charged ions

- in gas targets: An empirical scaling rule," *Phys. Rev. A* 27, 3372 (1983).
19. H. D. Betz, "Charge states and charge-changing cross sections for fast heavy ions penetrating through gaseous and solid media," *Rev. Mod. Phys.* 44, 465 (1972).
 20. T. Tonuma, I. Kohno, Y. Miyazawa, F. Yoshida, T. Karasawa, T. Takahashi, and S. Konno, "Charge changing of energetic heavy ions in gases," *J. Phys. Soc. Jpn.* 34, 148 (1973); J. Alonso, D. Dietrich, and H. Gould, "Charge changing cross sections for heavy ions at energies to 8.5 MeV/amu," *IEEE Trans. Nucl. Sci.* NS-26, 3686 (1979); J. A. Tanis, E. M. Bernstein, M. P. Stockli, W. G. Graham, K. H. Berkner, D. J. Markevich, R. H. McFarland, R. V. Pyle, J. W. Stearns, and J. E. Willis, *Phys. Rev. A* (in press); S. M. Ferguson, J. R. Macdonald, T. Chiao, L. D. Ellsworth, and S. A. Savoy, "Experimental electron-transfer cross sections for fluorine ions in argon at energies from 8 to 54 MeV," *Phys. Rev. A* 8, 2417 (1973); S. Datz, H. O. Lutz, L. B. Bridwell, C. D. Moak, H. D. Betz, and L. D. Ellsworth, "Electron capture and loss cross sections of fast bromine ions in gases," *Phys. Rev. A* 2, 430 (1970); V. S. Nikolaev, I. S. Dmitriev, L. N. Fateeva, and Ya. A. Teplova, "Experimental investigation of electron capture by multiply charged ions," *Zh. Eksp. Teor. Fiz.* 40, 989 (1967). [*Sov. Phys. - JETP* 13, 695 (1967)]; J. A. Tanis, E. M. Bernstein, W. G. Graham, M. Clark, S. M. Shafroth, B. M. Johnson, K. W. Jones, and M. Meron, "Resonant behavior in the projectile x-ray yield associated with electron capture in S⁺ Ar collisions," *Phys. Rev. Lett.* 49, 1325 (1982).
 21. T. R. Dillingham, J. R. Macdonald, and P. Richard, "Ionization of one-electron ions and capture by bare and one-electron ions of C, N, V, and F on He," *Phys. Rev. A* 24, 1237 (1981).
 22. D. S. F. Crothers and N. R. Todd, "One-electron capture by fast multiply charged ions in H: q³ scaling," *J. Phys. B* 13, 2277 (1980).
 23. J. R. Oppenheimer, "On the quantum theory of the capture of electrons," *Phys. Rev.* 31, 349 (1928); H. C. Brinkman and H. A. Kramers, "Capture of electrons by α -particles," *Proc. Acad. Sci. Amsterdam* 33, 973 (1930); J. S. Briggs, *J. Phys. B* 10, 3075 (1977); J. H. Macek and S. Alston, *Phys. Rev. A* 26, 250 (1982); J. H. McGuire, "The strong potential approximation with non-orthogonality terms," *IEEE Trans. Nucl. Sci.* NS-30, 1100 (1983).
 24. J. Eichler and H. Narumi, "On the classical-trajectory eikonal approximation for electron capture into multicharged ions," *Z. Phys. A* 295, 209 (1980); and references therein.
 25. G. D. Alton, L. B. Bridwell, M. Lucas, C. D. Moak, P. D. Miller, C. M. Jones, Q. C. Kessel, A. A. Antar, and M. D. Brown, "Single- and multiple-electron-loss-cross-section measurements from 20-MeV Fe⁴⁺ on this gaseous targets," *Phys. Rev. A* 23, 1073 (1981).
 26. J. R. Macdonald, S. M. Ferguson, F. Chiao, L. D. Ellsworth, and S. A. Savoy, "Experimental determination of electron-transfer cross sections for fluorine ions in nitrogen at energies from 4 to 54 MeV," *Phys. Rev. A* 5, 1188 (1972).
 27. G. D. Alton, "Single and multiple electron loss processes in MeV heavy ion-target collisions," *IEEE Trans. Nucl. Sci.* NS-28, 1043 (1981).
 28. G. H. Gillespie, "A comparison between sum-rule Born cross sections and the DZT semi-empirical calculations for electron-loss from fast heavy ions in nitrogen," *Nucl. Instrum. Methods* 176, 611 (1980).
 29. I. S. Dmitriev, Ya. M. Zhileikin and V. S. Nikolaev, "Calculation of the effective cross section for the loss of K electrons by fast hydrogen-like ions during encounters with hydrogen and helium atoms," *Zh. Eksp. Teor. Fiz.* 49, 500 (1965), [*Sov. Phys. JETP* 22, 352 (1966)].
 30. V. S. Nikolaev, V. S. Senashenko and V. Yu. Shafer, "The effect of the electron bound state structure on ionization cross sections in atomic collisions," *J. Phys. B* 6, 1779 (1973).
 31. T. Shirai, K. Igauchi and T. Watanabe, "Charge-stripping processes of hydrogen-like ions by collisions with neutral hydrogen atoms," *J. Phys. Soc. Jpn.* 42, 238 (1977).
 32. H. Knudsen, L. H. Andersen, H. K. Haugen, and P. Hvelplund, "Electron loss from fast one-electron ions colliding with He, N₂, and Ar," *Physica Scripta* 26, 132 (1982).
 33. N. Bohr, *Dan. Vidensk. Selsk. Mat. Fys. Medd.* 18, No. 8 (1948).
 34. H. Knudsen, C. D. Moak, C. M. Jones, P. D. Miller, R. O. Sayer, G. D. Alton, and L. B. Bridwell, "Total electron-loss cross sections and absolute charge-state yields of 20 MeV Fe ions transmitted through gaseous targets," *Phys. Rev. A* 19, 1029, (1979).
 35. W. Groh, A. Muller, C. Achenbach, A. S. Schlachter, and E. Salzborn, "Correlated capture ionization in slow collisions of multiply charged Xe ions with Xe atoms," *Phys. Lett.* 85A, 77 (1981); W. Groh, A. S. Schlachter, A. Muller, and E. Salzborn, "Transfer ionization in slow collisions of He²⁺ ions in rare gases," *J. Phys. B* 15, L207 (1982); W. Groh, A. Muller, A. S. Schlachter, and E. Salzborn, "Transfer ionization in slow collisions of multiply-charged ions with atoms," *J. Phys. B* 16, 1997 (1983).
 36. C. L. Cocke, R. DuBois, T. J. Gray, E. Justiniano, and C. Can, "Coincidence measurements of electron capture and ionization in low-energy Ar^{q+} + (He, Ne, Ar, Xe) collisions," *Phys. Rev. Lett.* 46, 1671 (1981); E. Justiniano, C. L. Cocke, T. J. Gray, R. D. DuBois, and C. Can, "Charge transfer and ionization in low-energy Ar^{q+} + Ne collisions," *Phys. Rev. A* 24, 2953 (1981).
 37. T. J. Gray, C. L. Cocke, and E. Justiniano, "Charge-state correlated cross sections for the production of low-velocity highly charged Ne ions by heavy-ion bombardment," *Phys. Rev. A* 22, 849 (1980).
 38. H. Damsgaard, H. K. Haugen, P. Hvelplund, and H. Knudsen, "Coincidence measurements of electron capture and target ionization in multiply

- charged $Au^{q+} + (He, Ne)$ collisions," *Phys. Rev. A* 27, 112 (1983).
39. K. Kuno, "Charge changing cross sections for heavy-particle collisions in the energy range from 0.1 to 10 MeV...", IPPJ-AM-9, 10 and 11 (Nagoya University, 1978).
40. H. Tawara, T. Kato, and Y. Nakai, "Electron capture and loss cross sections for collisions between heavy ions and hydrogen molecules," IPPJ-AM-28 (Nagoya University, 1983); "Cross sections for charge transfer of highly ionized ions in hydrogen molecules," IPPJ-AM-30 (Nagoya University, 1983).
41. Electronic and Atomic Collisions, Proceedings of the XIth International Conference on the Physics of Electronic and Atomic Collisions, Kyoto, August 29 - September 4, 1979, Invited Papers and Progress Reports, edited by N. Oda and K. Takayanagi (North Holland Publishing Co., 1980), pp. 387-456.
42. Physics of Electronic and Atomic Collisions, Invited papers of the XII International Conference on the Physics of Electronic and Atomic Collisions, Gatlinburg, Tennessee, 15-21 July 1981, edited by S. Datz (North Holland Publishing Co., 1982), pp. 655-718.
43. R. K. Janev and L. P. Presnyakov, "Collision processes of multiply charged ions with atoms," *Physics Reports* 70 (1981).
44. "Production and Physics of Highly Charged Ions," Proceedings of an International Symposium, Stockholm, June 1-5, 1982, edited by L. Liljeby, *Physica Scripta* T3 (1983).
45. F. J. deHeer, "Experiments on electron capture and ionization by ions," in Atomic and Molecular Processes in Controlled Thermonuclear Fusion, edited by M.R.C. McDowell and A. M. Ferendeci (Plenum Press, New York, 1980), pp. 351-390.