

# Longitudinal diagnostic scheme with sub-femtosecond resolution for high-brightness electron beams

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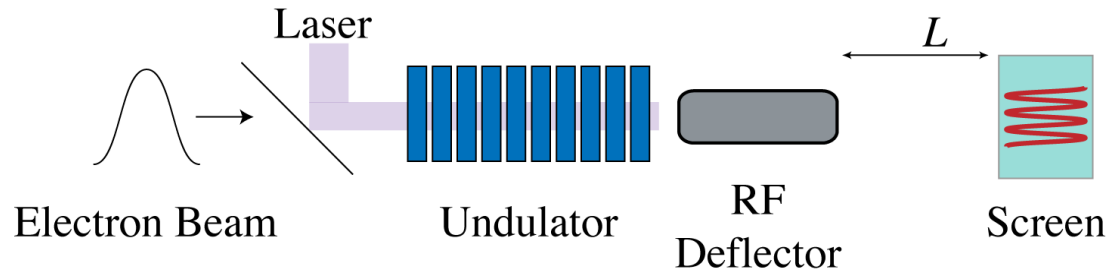
# Outline

- Motivation
- Description
  - Quasi-1D treatment
- Case studies
  - Simulations
    - UCLA Neptune
    - SLAC NLCTA (Echo Enabled FEL)
    - BNL ATF
  - Proof of Principle Experiment
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# Motivation

- Bunch length/profile measurements
  - Compression techniques to generate sub-ps pulses with high current
  - Characterization of Sub-ps pulses
  - Machine performance optimization
  - Benchmark theoretical and computational models
  - Understand beam variations in emittance, current
- Bunch length measurement techniques currently limited to  $\sim 10$  fs
  - Coherent radiation interferometry
  - Electro-Optical sampling
  - RF Deflector
  - Optical Replica Synthesizer
- Femtosecond resolution required for investigation ultra short pulses
  - Microbunching instability of COTR
  - Single-spike SASE FEL beam
  - Properties of attosecond x-ray production
  - \*Temporal properties of echo-enabled FELs

# Schematic Description



- Laser ( $TEM_{10}$  mode)/e-beam interaction in planar undulator
  - Angular modulation of beam
  - Dependent on longitudinal bunch coordinate
- RF deflector provides vertical streak to observe modulation for long bunches
- Angular modulation observable on distant screen ( $x' \rightarrow x$ )
  - Resolvable with standard optics
- Scheme provides enhanced resolution over RF deflector alone.

# General 1-D Treatment

Electron/laser interaction in undulator

Zholents and Zolotarev, NJP 10, 025005 (2008)

-Attosecond pulse lengths in a SASE FEL by selective lasing of electrons due to angular modulations.

TEM<sub>10</sub> mode (“dipole”) 
$$E_x(x, z, t) \simeq \frac{2\sqrt{2} E_0 x}{w_0 \left(1 + \frac{z^2}{z_0^2}\right)} \sin(k(z - ct) + \phi)$$

Motion in undulator 
$$\beta_x = -\frac{K}{\gamma} \sin\left(\frac{2\pi z}{\lambda_u}\right)$$

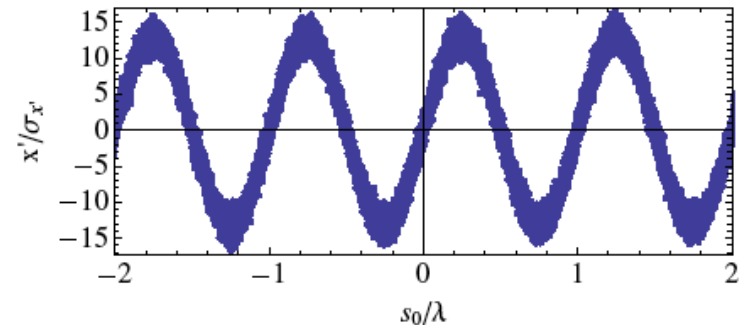
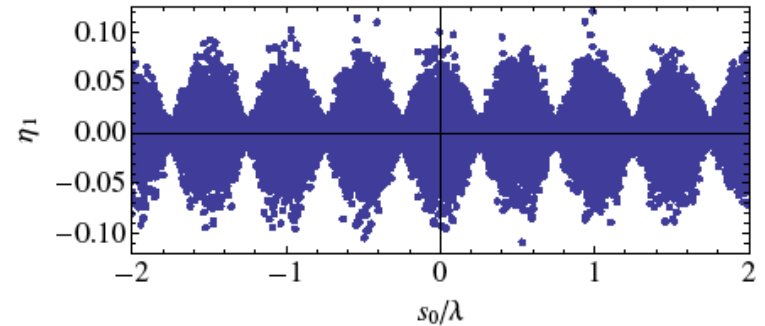
Energy exchange 
$$\frac{d\gamma}{dt} = \frac{e}{m_0 c} E_x \cdot \beta_x$$

Energy modulation 
$$\frac{\Delta\gamma}{\gamma} = \eta_1 - \eta_0 = A k x_0 \cos(k s_0)$$

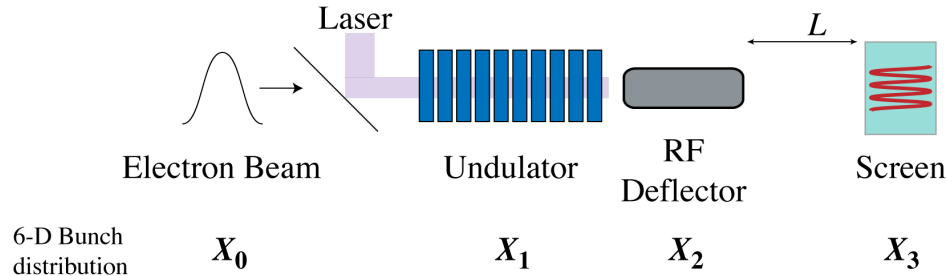
Panofsky-Wenzel Theorem 
$$\frac{\partial}{\partial x} \left( \frac{\Delta\gamma}{\gamma} \right) = \frac{\partial}{\partial S} \Delta x'$$

Angular modulation 
$$\Delta x' = A \sin(k s_0 + \phi)$$

$$A = \frac{2K}{\gamma^2} \sqrt{\frac{P_L}{P_0}} [JJ] f(L_u, z_0, \nu)$$



# Quasi 1-D Analytical Treatment



Transformation at deflector

$$y'_2 = y'_1 + A_{RF} k_{RF} s_1;$$

$$\eta_2 = \eta_1 + A_{RF} k_{RF} y_1$$

$$A_{RF} = \frac{eV_{def}}{\gamma mc^2}$$

After drift

$$x_3 = x_2 + Lx'_2 = x_0 + L(x'_0 + A \sin ks_0) \quad ;$$

$$x'_3 = x'_0 + A \sin ks_0 \quad ;$$

$$y_3 = y_2 + Ly'_2 = y_0 + L(y_0 + A_{RF} k_{RF} ks_0) \quad ;$$

$$y'_3 = y'_0 + A_{RF} k_{RF} ks_0 \quad ;$$

$$s_3 = s_2 + \frac{L\eta_2}{\gamma^2} = s_0 + \frac{L}{\gamma^2} (\eta_0 + Akx_0 \cos ks_0 + A_{RF} k_{RF} y_0) \quad ;$$

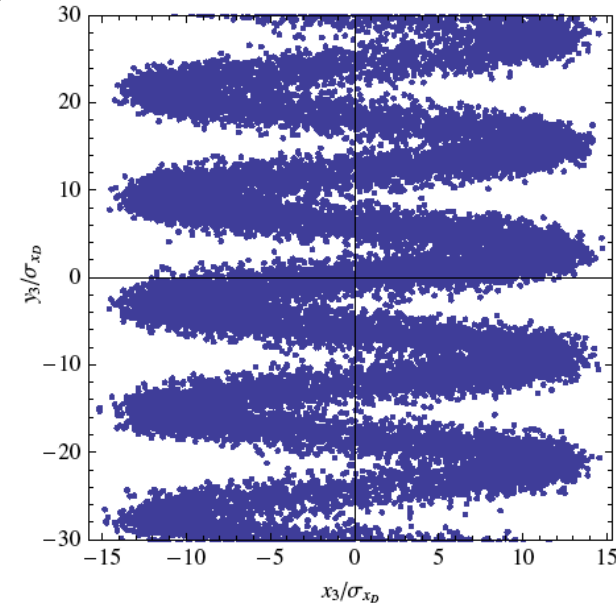
$$\eta_3 = \eta_0 + Akx_0 \cos ks_0 + A_{RF} k_{RF} y_0.$$

Initial Beam Distribution

$$f_0 = \frac{1}{(2\pi)^3 \sigma_x^2 \sigma_{x'}^2 \sigma_z \sigma_y} \text{Exp} \left[ -\frac{x_0^2 + y_0^2}{2\sigma_x^2} - \frac{x_0'^2 + y_0'^2}{2\sigma_{x'}^2} - \frac{s_0^2}{2\sigma_z^2} - \frac{\eta_0^2}{2\sigma_y^2} \right]$$

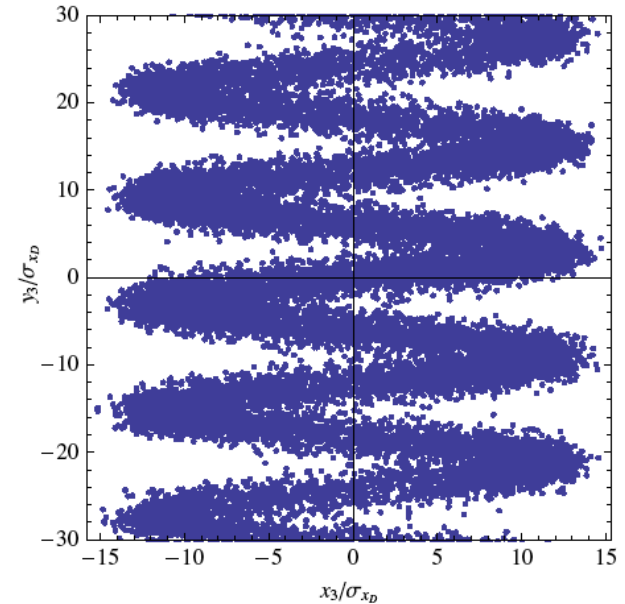
Beam Distribution at screen

$$f_0(x_3, y_3, s_0) = \frac{1}{(2\pi)^{3/2} \sigma_{x_D}^2 \sigma_z} \text{Exp} \left[ -\frac{(x_3 - AL \sin ks_0)^2}{2\sigma_{x_D}^2} - \frac{(y_3 - A_{RF} k_{RF} Ls_0)^2}{2\sigma_{x_D}^2} - \frac{s_0^2}{2\sigma_z^2} \right]$$



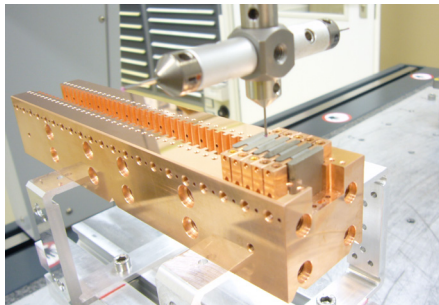
# Bunch length diagnostic

- Resolution set by magnitude of imprinted angular modulation
  - Constraint: must be larger than intrinsic beam divergence
- Practical diagnostic resolution set by angular modulation by each component in scheme
  - RF deflector
  - Optical modulator (undulator)
  - Ability to resolve screen
- Constraints
  - Angular modulation must be larger than intrinsic beam divergence
  - Imposed beam deflections must be larger than “unperturbed” beam size at screen
  - May require collimators (loss of charge)
- Resolution enhancement
  - Dynamic range enhancement



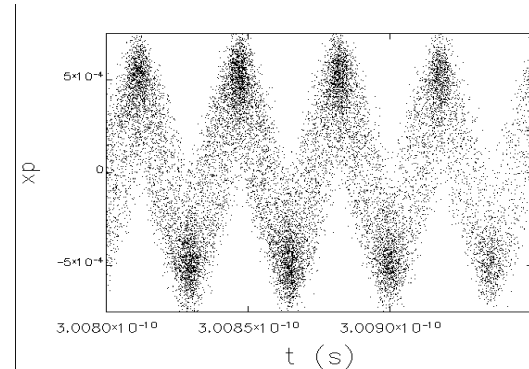
# Example: UCLA Neptune

- Neptune injector facility
  - Experience in laser – e-beam interactions (IFEL, harmonic microbunching)
  - High-brightness injector
    - $E = 13 \text{ MeV}$
    - $\varepsilon_n = 1 \text{ mm-mrad}$
    - $Q = 500 \text{ pC}$
  - TW-class CO<sub>2</sub> laser
    - $\lambda = 10.6 \mu\text{m}$ ,  $P_L = 300 \text{ MW}$  (for simulation)
- Undulator
  - PrFeB (cryo cooled to 30K)
  - 9mm period,  $K=1.7$ ,  $g=2\text{mm}$
- Deflector (simulation)
  - $V_d = 6 \text{ MV}$ ,  $\lambda_{\text{RF}} = 2.6 \text{ cm}$
- Angular modulation  $\sim 7 \text{ mrad}$ 
  - Resolution  $\sim 0.3 \text{ fs}$  (simulation)

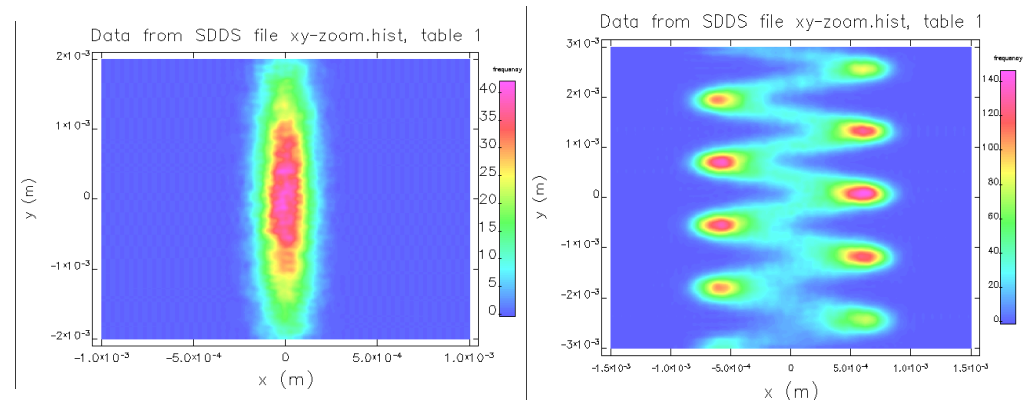


F. O'Shea, PRSTAB 13, 070702 (2010)

Simulations performed with Elegant



Angular modulation after undulator (sim)



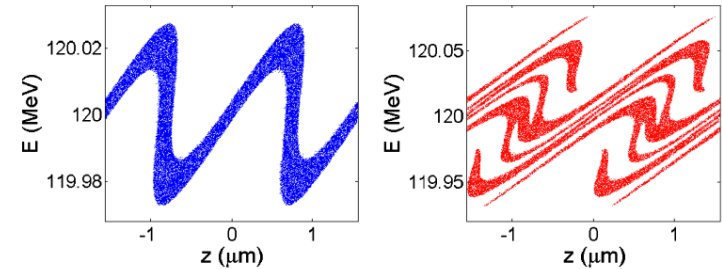
Simulated Transverse distribution on screen ( $L=1\text{m}$ ) with:  
 -only deflector on (left)  
 -deflector and optical modulator on (right)



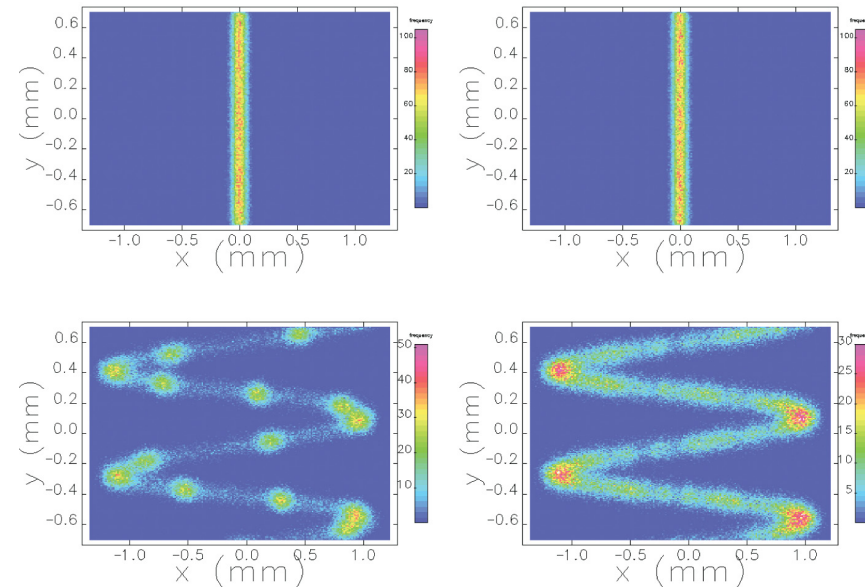
# Echo-enabled FEL at SLAC NLCTA

- Experiment conducted at NLCTA (D.Xiang, et al., SLAC)
  - E-beam modulation provided by  $\sim 800\text{nm}$  laser and first undulator
  - Sent through chicane with large R56
    - Fine longitudinal structure imposed
  - E-beam modulated by  $\sim 1600\text{nm}$  laser in second undulator
  - Density modulation at short wavelength in second chicane
- Diagnostic
  - Coherent radiation at harmonics of seed lasers
  - Not trivial to determine if the radiation is from interplay of two lasers or individual laser
  - Time-domain measurement provides straightforward evidence of EEHG
- Parameters (simulation)
  - $E = 120\text{MeV}$ ,  $\varepsilon_n = 1\text{mm-mrad}$
  - $V_d = 8\text{MV}$ ,  $\lambda_{\text{RF}} = 2.6\text{ cm}$
  - $K = 6.0$ ,  $N_U = 3$ ,  $\lambda_U = 6\text{ cm}$
  - $\lambda = 10.6\mu\text{m}$ ,  $P_L = 500\text{GW}$
  - Resolution  $\sim .6\text{fs}$

Simulations performed with Elegant



Phase Space after last chicane for  $\sim 1600\text{nm}$  laser only (left) and for interplay of two lasers (right)

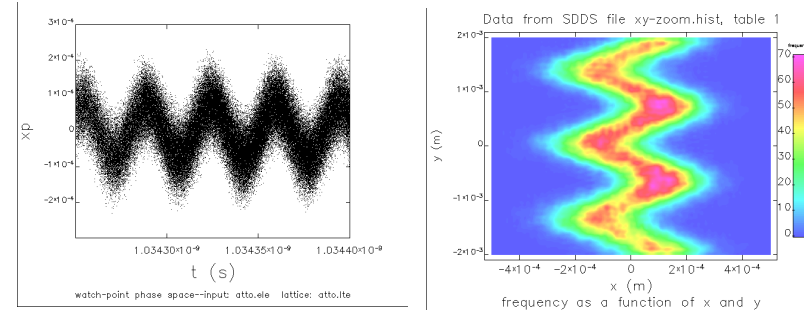


Transverse distribution at screen. TOP: Only deflector turned on. BOTTOM: Deflector and laser modulation on.

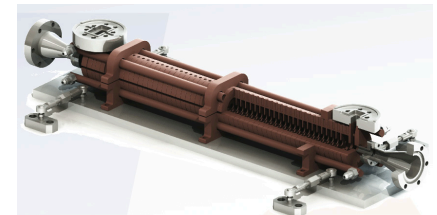
# POP at BNL ATF

- High brightness user facility
  - CO2 laser e-beam interactions
- Parameters (simulation)
  - $E = 44 \text{ MeV}$ ,  $Q = 500 \text{ pC}$ ,  $\epsilon_n = 1 \text{ mm-mrad}$
  - $\lambda_u = 3 \text{ cm}$ ,  $N = 10$ ,  $B_0 = 1.0 \text{ T}$ ,  $K = 3.0$
  - $\lambda = 10.6 \text{ }\mu\text{m}$ ,  $P_L = 300 \text{ MW}$
  - $V_d = 10 \text{ MV}$ ,  $L_d = 46 \text{ cm}$
- X-band deflector
  - Built by RadiaBeam for BNL ATF
  - Optimized for  $\sim 100 \text{ MeV}$  beams
  - Freq. =  $11.424 \text{ GHz}$
  - $< 10 \text{ fs}$  temporal resolution
  - Install in 2012
- TEM<sub>10</sub> laser mode
  - Previous experience from Inverse Cerenkov Acceleration experiment
    - W. Kimura, PRL 74,546 (1994)
    - Required radial polarization
  - Purity of mode
  - Splitting TEM<sub>00</sub> mode and introduce  $\pi$  phase delay
  - Upgrade to TW
- Undulator
  - Design

Simulations performed with Elegant



Angular modulation (left) and beam distribution at screen (right)



$\sqrt{Z} = E_e / P^{1/2}$ [kV/mW <sup>1/2</sup> ]	$\alpha$	$v_e/c$	$E_{max} / P^{1/2}$ [kV/mW <sup>1/2</sup> ]	$L_{10T}$ [m]	$E_{max}$ [MV/m]	$\tau_F$ [ns]	$N_e$	$P_{out} / P_{in}$
8.48	0.66	0.0267	20.57	0.46	92	57	53	0.55

Rendering of XTD for  $\sim 10 \text{ fs}$  temporal resolution at BNL ATF (L. Faillace)

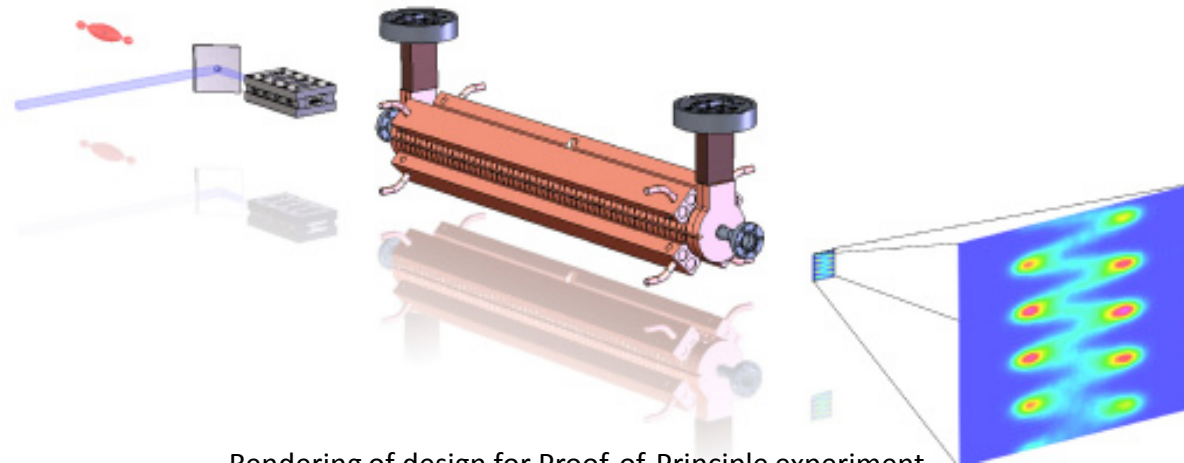


TEM<sub>10</sub>-like mode simulated (left) and imaged (right) at BNL ATF

# Challenges

- Nonlinear resolution
  - Resolution at turning points is “smeared”
  - Try to move beam away from “low-resolution” part of curve to linear (“high-resolution”)
  - Shift laser phase by  $\pi/2$
  - Multi-shot statistics
- Diagnostic is better for lower energy beam in current scheme
  - Modulation scaling  $\sim 1/\gamma^2$
- Diagnostic favors long wavelength, high power laser
  - Scaling  $\sim P_L^{1/2}$
  - BNL ATF, UCLA Neptune
  - Fundamental laser mode suppression
    - Leakage could cause regenerative amplification and smear desired effect
- Demanding beam properties
  - Emittance, spot size
  - Requires beam collimators which may reduce total detectable signal at screen

# Summary



Rendering of design for Proof-of-Principle experiment

- Bunch length resolution on sub-fs is plausible with existing technologies
  - Enhanced resolution over deflector alone
- Alternative schemes to address open questions
  - Helical undulator
  - Undulator with harmonics
  - “Micro”-undulator
- Next step: Proof of principle experiment at BNL ATF
  - Beam diagnostics, X-band infrastructure, CO<sub>2</sub> laser experience